

Chromoelectric and chromomagnetic fields for the static gluon-quark-antiquark system

Marco Cardoso*CFTP, Instituto Superior Técnico**E-mail:* mjdcc@cftp.ist.utl.pt**Nuno Cardoso****CFTP, Instituto Superior Técnico**E-mail:* nunocardoso@cftp.ist.utl.pt**Pedro Bicudo***CFTP, Instituto Superior Técnico**E-mail:* bicudo@ist.utl.pt

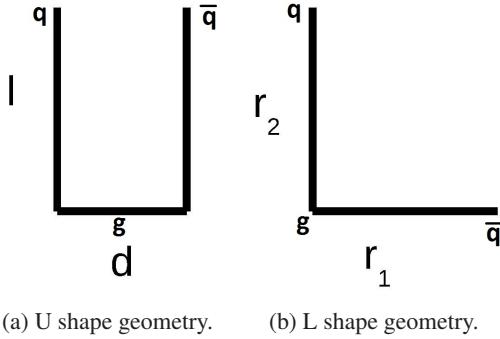
The chromoelectric and chromomagnetic fields, created by a static gluon-quark-antiquark system, are computed in the quenched approximation of lattice QCD, in a $24^3 \times 48$ lattice at $\beta = 6.2$. We study two geometries, one with a U shape and another with an L shape. The degenerate case of the two gluon glueball is also studied. This is relevant to understand the microscopic structure of hadrons, in particular of hybrids. This also contributes to understand confinement with flux tubes of the chromoelectric field, and to discriminate between the models of fundamental or adjoint tubes.

The XXVII International Symposium on Lattice Field Theory - LAT2009
July 26-31 2009
Peking University, Beijing, China

*Speaker.

1. Introduction

The aim of this work is to compute the chromoelectric and chromomagnetic fields and study the shape of the flux-tubes for the hybrid gluon-quark-antiquark system. We study two different geometries for the hybrid system, one with a U shape and another with L shape, figure. 1.



(a) U shape geometry. (b) L shape geometry.

Figure 1: gluon-quark-antiquark geometries, U and L shapes.

2. The Wilson Loops and Chromo Fields for exotic systems

In principle, any Wilson loop with a geometry similar to that represented in figure 2a, describing correctly the quantum numbers of the hybrid, is appropriate, although the signal to noise ratio may depend on the choice of the Wilson loop. A correct Wilson loop must include an SU(3) octet (the gluon), an SU(3) triplet (the quark) and an SU(3) antitriplet (the antiquark), as well as the connection between the three links of the gluon, the quark and the antiquark.

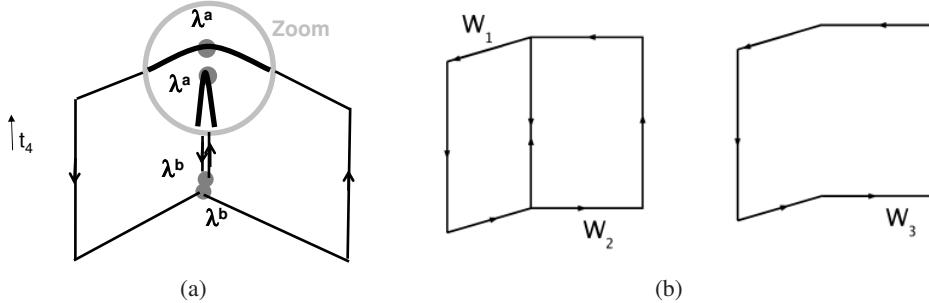


Figure 2: (a) Wilson loop for the $gq\bar{q}$ and equivalent position of the static antiquark, gluon, and quark. (b) Simple Wilson loops that make the $gq\bar{q}$ Wilson loop.

The Wilson loop for this system is given by:

$$W_{gq\bar{q}} = \frac{1}{16} Tr[\lambda^b T^+ \lambda^a T] Tr[\lambda^b S_1 \lambda^a S_2] \quad (2.1)$$

$$= W_1 W_2 - \frac{1}{3} W_3 \quad (2.2)$$

where W_1 , W_2 and W_3 are the simple Wilson loops shown in figure 2b. When $r_1 = 0$, $W_1 = 3$ and $W_2 = W_3$, the operator reduces to the mesonic Wilson loop and when $\mu = v$ and $r_1 = r_2 = r$,

$W_2 = W_1^\dagger$ and $W_3 = 3$, $W_{gq\bar{q}}$ reduces to $W_{gq\bar{q}}(r, r, t) = |W(r, t)|^2 - 1$, that is the Wilson loop in the adjoint representation used to compute the potential between two static gluons.

In order to improve the signal to noise ratio of the Wilson loop, the links are replaced by "fat links",

$$U_\mu(s) \rightarrow P_{SU(3)} \frac{1}{1+6w} \left(U_\mu(s) + w \sum_{\mu \neq v} U_v(s) U_\mu(s+v) U_v^\dagger(s+\mu) \right) \quad (2.3)$$

We use $w = 0.2$ and iterate this procedure 25 times in the spatial direction.

We obtain the chromoelectric and chromomagnetic fields on the lattice, by using:

$$\langle E^2 \rangle = \langle P_{0i} \rangle - \frac{\langle WP_{0i} \rangle}{\langle W \rangle} \quad (2.4)$$

$$\langle B^2 \rangle = \frac{\langle WP_{ij} \rangle}{\langle W \rangle} - \langle P_{ij} \rangle \quad (2.5)$$

and the plaquette is given by

$$P_{\mu\nu}(s) = 1 - \frac{1}{3} \text{ReTr} [U_\mu(s) U_\nu(s+\mu) U_\mu^\dagger(s+\nu) U_\nu^\dagger(s)] \quad (2.6)$$

We only apply the smearing technique to the Wilson loop. The relationship between various plaquettes and the field components is:

component	plaquette
E_x	P_{xt}
E_y	P_{yt}
E_z	P_{zt}
B_x	P_{yz}
B_y	P_{zx}
B_z	P_{xy}

The energy (ε) and action (γ) density is given by

$$\varepsilon = \frac{1}{2} (\langle E^2 \rangle + \langle B^2 \rangle) \quad (2.7)$$

$$\gamma = \frac{1}{2} (\langle E^2 \rangle - \langle B^2 \rangle) \quad (2.8)$$

3. Results for the gluon-quark-antiquark

Here we present the results of our simulations with $141 \times 24^3 \times 48$, $\beta = 6.2$ configurations generated with the version 6 of the MILC code [1], via a combination of Cabibbo-Mariani and overrelaxed updates. The results are presented in lattice spacing units.

In the following pictures we present the results for the chromoelectric and chromomagnetic fields and for the energy and action density. The figures 3 to 6 show the results for the U shape geometry and figures 7 to 10 the results for the L shape geometry.

In figure 11 we present the results for the U geometry along $x = 0$, this corresponds to the axis along gluon and the middle distance between quark-antiquark, and $y = 4$, this corresponds to the axis along quark-antiquark. This results show that when the quark and the antiquark are superposed the results are consistent with the degenerate case of the two gluon glueball. In figure 12 we present the results for the L geometry along the segment gluon-antiquark and along segment gluon-quark. And finally, in figure 13 we show a comparison between the results for $(r_1 = 0, r_2 = 8)$ and $(r_1 = 8, r_2 = 8)$ along segment gluon-antiquark in the L geometry, when the gluon and the antiquark are superposed this results are consistent with the static quark-antiquark case.

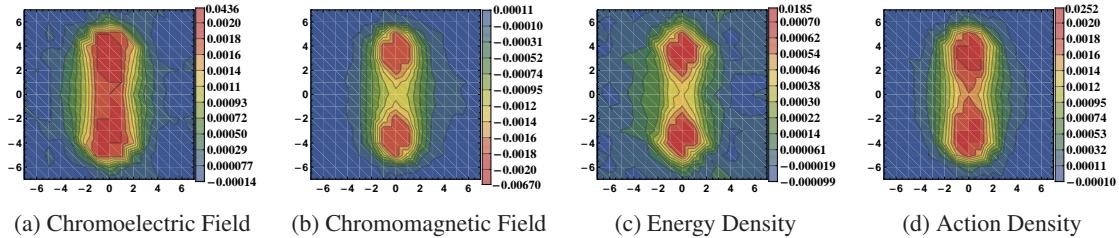


Figure 3: Results for the U geometry with $d = 0$ and $l = 8$. In this case, the quark and the antiquark are superposed and the results are consistent with the degenerate case of the two gluon glueball.

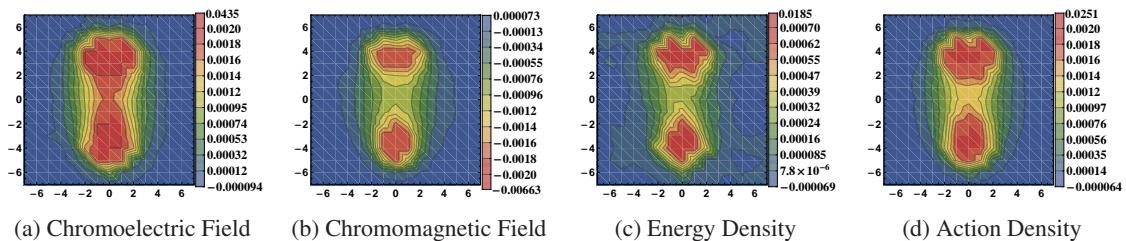


Figure 4: Results for the U geometry with $d = 2$ and $l = 8$

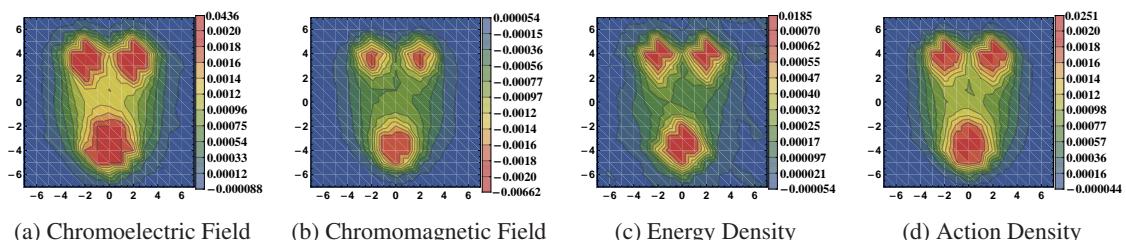
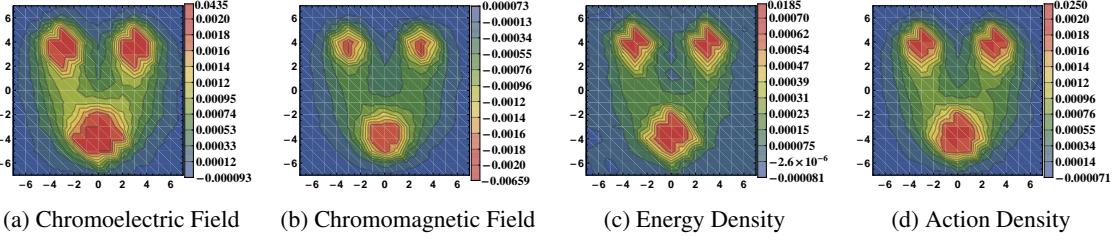
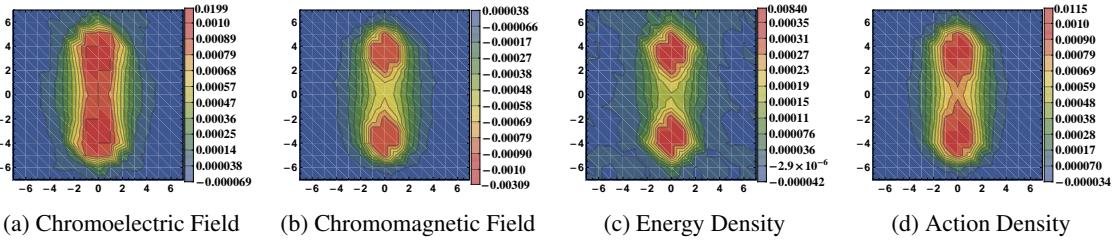
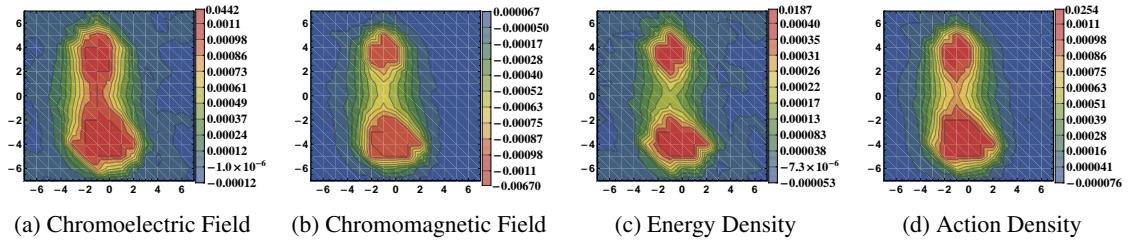
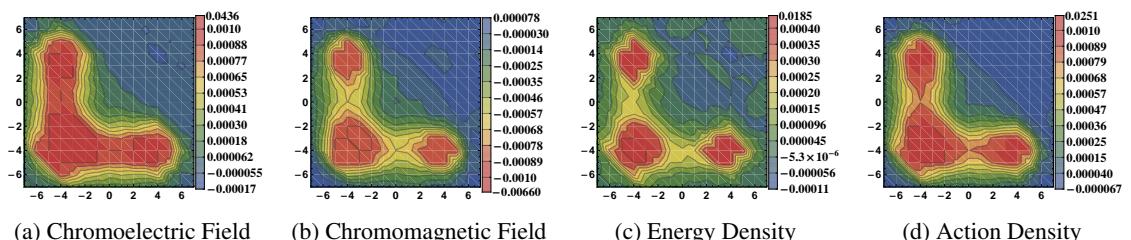


Figure 5: Results for the U geometry with $d = 4$ and $l = 8$

Figure 6: Results for the U geometry with $d = 6$ and $l = 8$ Figure 7: Results for the L geometry with $r_1 = 0$ and $r_2 = 8$. The gluon and the antiquark are superposed and the results are consistent with the static quark-antiquark case.Figure 8: Results for the L geometry with $r_1 = 2$ and $r_2 = 8$ Figure 9: Results for the L geometry with $r_1 = 8$ and $r_2 = 8$

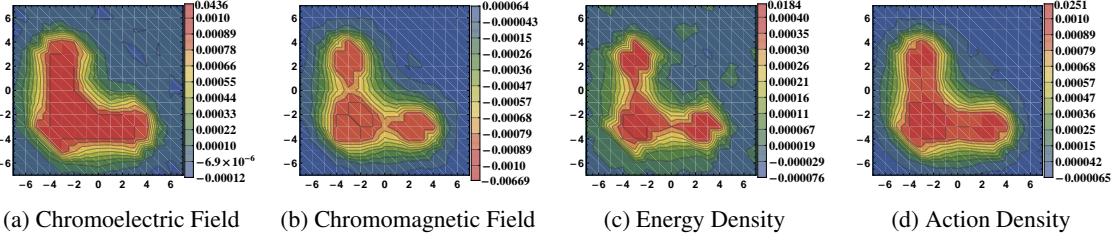
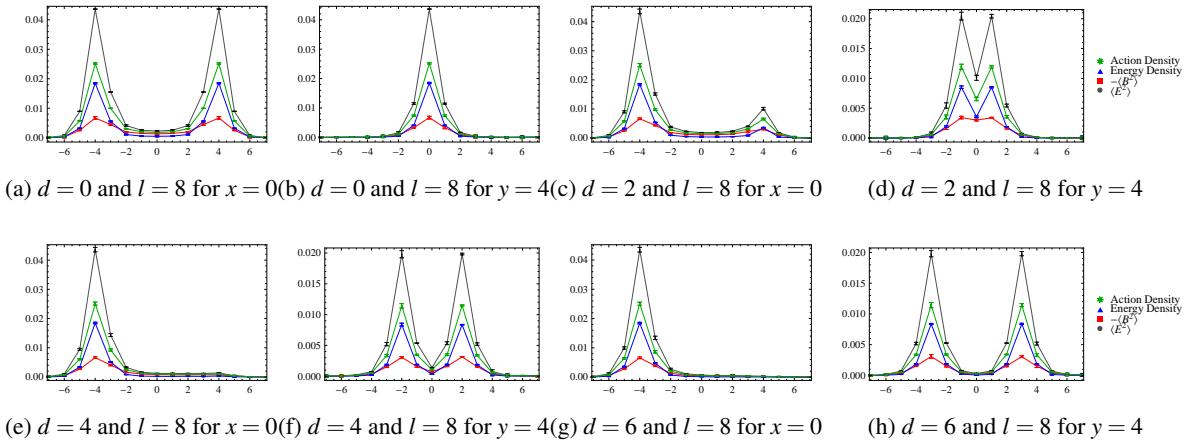

 Figure 10: Results for the L geometry with $r_1 = 6$ and $r_2 = 6$


Figure 11: Results for the U geometry.

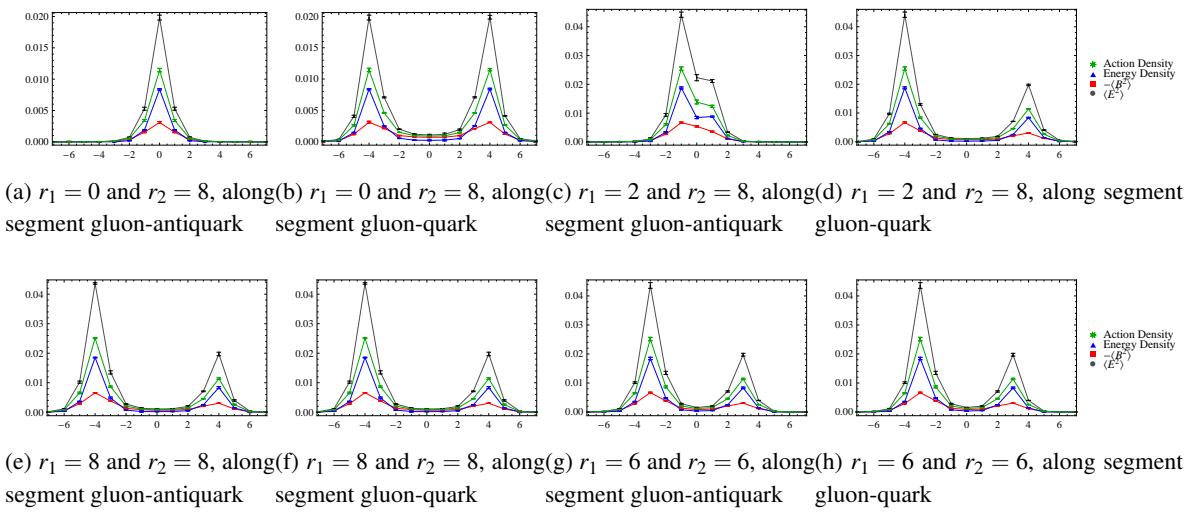


Figure 12: Results for the L geometry.

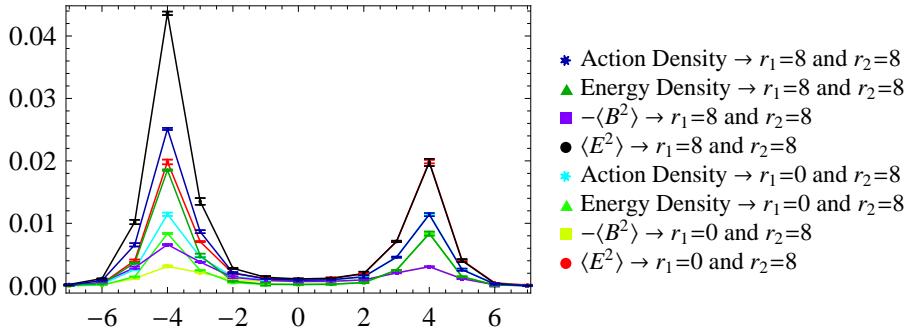


Figure 13: Comparison between the results for $(r_1 = 0; r_2 = 8)$ and $(r_1 = 8; r_2 = 8)$ along segment gluon-antiquark in the L geometry.

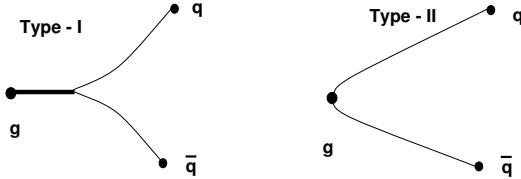


Figure 14: String attraction and fusion, and string repulsion, respectively in type I and II superconductors.

4. Conclusions

In Bicudo et al. [2] and Cardoso et al. [3] it was shown that for the static gluon-quark-antiquark potential V when the segments between gluon-quark and gluon-antiquark are perpendicular, V is compatible with confinement realized with a pair of fundamental strings, one linking the gluon to the quark and the other linking the same gluon to the antiquark. However, if the segments are parallel and superposed, the total string tension becomes larger and agrees with Casimir Scaling measured by Bali [4]. This can be interpreted with a type-II superconductor analogy for the confinement in QCD, see figure 14, with repulsion of the fundamental strings and with the string tension of the first topological excitation of the string (the adjoint string) larger than the double of the fundamental string tension.

The general shape of the flux-tubes observed here reinforce the conclusions of Bicudo et al. [2] and Cardoso et al. [3].

We study the fields with two geometries, U and L shaped for the Wilson loops. Here, the components of the chromoelectric and chromomagnetic fields around a static gluon-quark-antiquark are investigated. This allows us to determine the shape of the flux-tubes with respect both to the energy and action densities. When the quark and the antiquark are superposed the results are consistent with the degenerate case of the two gluon glueball, and when the gluon and the antiquark are superposed the results are consistent with the static quark-antiquark case. Another interesting

result is that the absolute value of the chromoelectric field dominates over the absolute value of the chromomagnetic field.

Acknowledgments

This work was financed by the FCT contracts POCI/FP/81933/2007 and CERN/FP/83582/2008. We thank Orlando Oliveira for useful discussions.

References

- [1] This work was in part based on the MILC collaboration's public lattice gauge theory code.
<http://physics.indiana.edu/~sg/milc.html>.
- [2] P. Bicudo, M. Cardoso, O. Oliveira, First study of the gluon-quark-antiquark static potential in SU(3) Lattice QCD, Phys.Rev.D77:091504.
- [3] M. Cardoso, P. Bicudo, O. Oliveira, Static potential for the quark-antiquark-gluon hybrid system in lattice QCD, [PoSLAT2007:293].
- [4] G. S. Bali, Casimir scaling of SU(3) static potentials, Phys.Rev. D62, [arXiv:hep-lat/0006022].