

Measuring Semileptonic Asymmetries in LHCb

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The CP -violating flavour-specific asymmetry in neutral b mesons provides a method for testing the Standard Model. The measurements from the D0 experiment yield values of this asymmetry that disagree with the Standard Model at a level of 3.6σ . This contribution discusses the latest LHCb measurements in this sector both from B^0 mesons (a_{sl}^d) and B_s^0 mesons (a_{sl}^s). Using their 2011 dataset, corresponding to an integrated luminosity of 1.0 fb^{-1} obtained in 2011, LHCb measured a value of $a_{sl}^s = (-0.06 \pm 0.50_{\text{stat}} \pm 0.36_{\text{syst}})\%$. Combining the 2011 and 2012 datasets, with an integrated luminosity of 3 fb^{-1} , LHCb measured $a_{sl}^d = (-0.02 \pm 0.19_{\text{stat}} \pm 0.30_{\text{syst}})\%$. These are the most precise measurements of the parameters a_{sl}^s and a_{sl}^d to date. Plans for an updated result for a_{sl}^s using the full 3 fb^{-1} dataset are discussed. This will include new methods to determine detection asymmetries which are the dominating systematic uncertainty of the 2011 measurement.

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1. Introduction to Neutral Meson Mixing and Semileptonic Asymmetries

Neutral mesons can oscillate into their own antiparticle through a second order weak amplitude; this process is called mixing. Since these processes are heavily suppressed in the Standard Model, they are sensitive to new physics. The mixing of these neutral mesons, B_q^0 , can be described by the Schrödinger equation:

$$i \frac{d}{dt} \begin{pmatrix} |B_q^0(t)\rangle \\ |\bar{B}_q^0(t)\rangle \end{pmatrix} = \left(M - \frac{i}{2} \Gamma \right) \begin{pmatrix} |B_q^0(t)\rangle \\ |\bar{B}_q^0(t)\rangle \end{pmatrix}, \quad (1.1)$$

where M and Γ represent a 2×2 complex matrix that characterises the mixing. The neutral mesons relevant for this contribution contain a b quark and are denoted by B_q^0 , where $q = \{d, s\}$. Their mass eigenstates can be described as a linear combination of the flavour eigenstates:

$$|B_L^0\rangle = p|B_q^0\rangle + q|\bar{B}_q^0\rangle \quad (1.2)$$

$$|B_H^0\rangle = p|B_q^0\rangle - q|\bar{B}_q^0\rangle, \quad (1.3)$$

where L and H indicate ‘‘light’’ and ‘‘heavy’’, and where p and q are complex coefficients satisfying $|p|^2 + |q|^2 = 1$. Mixing is characterised by the difference in mass, $\Delta m = m_H - m_L$, and decay width, $\Delta\Gamma = \Gamma_L - \Gamma_H$.

There is CP violation in mixing if $\mathcal{P}(B_q^0 \rightarrow \bar{B}_q^0) \neq \mathcal{P}(\bar{B}_q^0 \rightarrow B_q^0)$. By looking at flavour-specific decays, the amount of CP violation in mixing can be measured. The final states of these decays indicate whether the B decayed as a B_q^0 or \bar{B}_q^0 . One can measure the flavour-specific asymmetry a_{fs} , which is defined as:

$$a_{\text{fs}} = \frac{\Gamma(\bar{B}_q^0 \rightarrow B_q^0 \rightarrow f) - \Gamma(B_q^0 \rightarrow \bar{B}_q^0 \rightarrow \bar{f})}{\Gamma(\bar{B}_q^0 \rightarrow B_q^0 \rightarrow f) + \Gamma(B_q^0 \rightarrow \bar{B}_q^0 \rightarrow \bar{f})} = \frac{1 - |q/p|^4}{1 + |q/p|^4}. \quad (1.4)$$

Hence, there is CP violation in mixing when $|q/p| \neq 1$. The Standard Model predicts values of a_{fs} that are zero compared to the experimental resolution: $a_{\text{fs}}^d = (-4.1 \pm 0.6) \times 10^{-4}$ for B^0 decays and $a_{\text{fs}}^s = (1.9 \pm 0.3) \times 10^{-5}$ for B_s^0 decays [1, 2]. Semileptonic decays are flavour specific, i.e. the charge of the lepton indicates the flavour of the B , and are therefore excellent for measuring this asymmetry which is then called the semileptonic asymmetry: a_{sl} . The relevant semileptonic decays are $B_s^0 \rightarrow D_s^- \ell^+ \nu_\ell$, $B^0 \rightarrow D^- \ell^+ \nu_\ell$ and $B^0 \rightarrow D^{*-} \ell^+ \nu_\ell$.

1.1 Methods to measure a_{sl}

There are different methods to measure semileptonic asymmetries. The method used by the B-factories and the D0 experiment measures the inclusive like-sign dilepton asymmetry. Like-charge lepton pairs can be produced by $b\bar{b}$ pairs where both b hadrons decay semileptonically, but where one b forms a neutral meson that oscillates before decaying. This asymmetry is time-integrated and is defined as:

$$a_{\text{sl}} = A_{\ell\ell} = \frac{\Gamma(\ell^+\ell^+) - \Gamma(\ell^-\ell^-)}{\Gamma(\ell^+\ell^+) + \Gamma(\ell^-\ell^-)}. \quad (1.5)$$

The B-factories BaBar [3] and Belle [4] operate at an energy too low to produce B_s^0 mesons, and hence measure a_{sl}^d . For the D0 experiment, the value that is found using this method is a linear

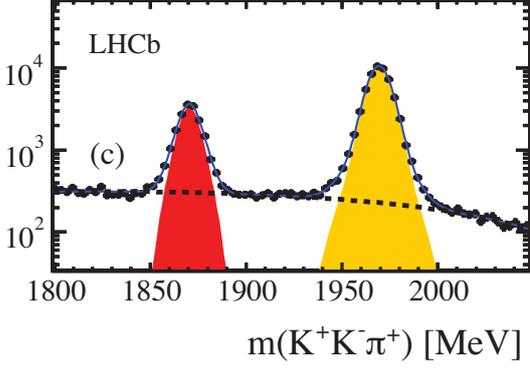


Figure 1: Invariant mass distributions for $K^+K^-\pi^+$, where the K^+K^- invariant mass is within 20 MeV of the ϕ meson mass.

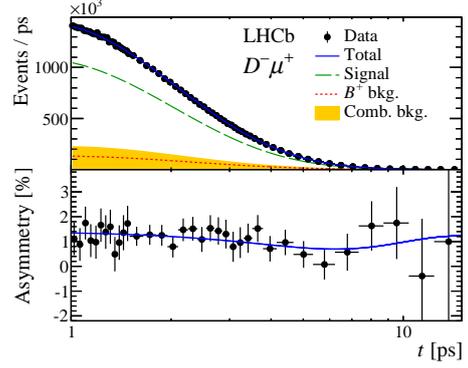


Figure 2: Decay rates and charge asymmetry versus decay time for the $D^-\mu^+$ sample used for the a_{sl}^d analysis.

combination of a_{sl}^s and a_{sl}^d , which are the corresponding contributions from B_s^0 and B^0 decays respectively. They have found a value for this of $a_{\text{sl}} = (-0.79 \pm 0.17_{\text{stat}} \pm 0.09_{\text{syst}})\%$ [5] which is 3.6σ away from the Standard Model prediction. They also measured values for a_{sl}^s [6] and a_{sl}^d [7] separately. An overview of all current measurements of a_{sl} is shown in figure 3.

In other experiments, such as LHCb, only one of the b mesons is reconstructed and a time-dependent measurement of a_{sl} is made using the following expression:

$$\frac{N(B, t) - N(\bar{B}, t)}{N(B, t) + N(\bar{B}, t)} = \frac{a_{\text{sl}}}{2} \left[1 - \frac{\cos \Delta m t}{\cosh \frac{1}{2} \Delta \Gamma t} \right]. \quad (1.6)$$

For the measurement of a_{sl}^d , the time-dependence is an important aspect of the analysis. The measured asymmetry also includes detection asymmetries, A_D , for the various final state particles, and production asymmetries, A_P , which are caused by the fact that the initial state only contains protons, and no anti-protons. Including these, the expression for the measured asymmetry in terms of a_{sl}^d is:

$$A_{\text{meas}}(t) = \frac{N(B, t) - N(\bar{B}, t)}{N(B, t) + N(\bar{B}, t)} = \frac{a_{\text{sl}}^d}{2} + A_D + \left[\frac{a_{\text{sl}}^d}{2} - A_P \right] \frac{\cos \Delta m t}{\cosh \frac{1}{2} \Delta \Gamma t}. \quad (1.7)$$

Integrating over decay time, and accounting for the detection efficiency as a function of decay time, $\epsilon(t)$, one obtains the expression for the time-integrated measured asymmetry for a_{sl}^s :

$$A_{\text{meas}} = \frac{N(\mu^+ D_s^-) - N(\mu^- D_s^+)}{N(\mu^+ D_s^-) + N(\mu^- D_s^+)} = \frac{a_{\text{sl}}^s}{2} + A_D + \left(\frac{a_{\text{sl}}^s}{2} - A_P \right) \frac{\int_0^\infty e^{-\Gamma_s t} \cos(\Delta m_s t) \epsilon(t) dt}{\int_0^\infty e^{-\Gamma_s t} \cosh(\frac{1}{2} \Delta \Gamma_s t) \epsilon(t) dt}. \quad (1.8)$$

Since the value of Δm_s is very large (1.2×10^{-8} MeV), B_s^0 oscillates fast and the integral yields a small value ($\sim 1\%$). Combined with the small values of a_{sl}^s and A_P ($\sim 1\%$), this is of the order $< 10^{-4}$ which is negligible compared to the uncertainties on the measurement. The expression therefore reduces to:

$$A_{\text{meas}} = \frac{N(\mu^+ D_s^-) - N(\mu^- D_s^+)}{N(\mu^+ D_s^-) + N(\mu^- D_s^+)} = \frac{a_{\text{sl}}^s}{2} + A_D. \quad (1.9)$$

Source of Uncertainty	$\sigma(A_{\text{meas}})$ [%]
$A(\mu^+\pi^-)$	0.31
$A(K^+K^-)$	< 0.02
Fitting	0.15
Background	0.10
Total	0.36

Table 1: Systematic uncertainties of 2011 a_{sl}^s analysis.

2. Latest results on a_{sl}^d and a_{sl}^s from LHCb

The LHCb detector has an excellent momentum resolution. The tracking system provides a measurement of momentum, p , of charged particles with a relative uncertainty that varies from 0.5% at low momentum to 1.0% at 200 GeV/c [8]. This allows for separation between B^0 and B_s^0 mesons. It also has a high muon identification efficiency which makes it very suitable for the a_{sl} measurements. In 2011, LHCb gathered an integrated luminosity $\mathcal{L} = 1.0 \text{ fb}^{-1}$ of data at a centre-of-mass energy of $\sqrt{s} = 7 \text{ TeV}$. In 2012, $\mathcal{L} = 2 \text{ fb}^{-1}$ was gathered with $\sqrt{s} = 8 \text{ TeV}$. More information on the LHCb detector can be found in [9].

The analysis of a_{sl}^s using data from the LHCb detector is based on data gathered in 2011. The current a_{sl}^s analysis at LHCb [10] studies the decay of $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$, where $D_s^- \rightarrow \phi (\rightarrow K^+ K^-) \pi^-$. The detection asymmetries for the final state particles hence come from the μ^+ , π^- , K^+ and K^- and can be split up as $A_D = A(K^+ K^-) + A(\mu^+ \pi^-)$. Detection asymmetries arise from the fact that the detector is not perfectly symmetric and that it can have different interaction rates for positive and negative particles. They are dependent on the kinematics of the particles and are partially cancelled by periodically reversing the dipole spectrometer magnet polarity. By restricting to the $\phi \rightarrow K^+ K^-$ resonance, the kaon pair is kinematically symmetric, and the measurement is insensitive to any momentum dependent kaon detection asymmetry. The largest systematic uncertainties of the measurement hence come from the tracking and identification asymmetries of the muons and pions which also partially cancel out due to their opposite charge, see table 1. The remaining tracking asymmetry is determined by using $D^{*+} \rightarrow D^0 (\rightarrow K^- \pi^+ \pi^+ \pi^-) \pi^-$. Figure 1 shows a mass fit to the $K^+ K^- \pi^+$ invariant mass, where the D_s^+ peak is at the right side of the plot; at the left is the D^+ peak. The final result from the $a_{\text{sl}}^s = (-0.06 \pm 0.50_{\text{stat}} \pm 0.36_{\text{syst}})\%$.

The a_{sl}^d analysis from LHCb [11] is based on the 2011 and 2012 ($\sqrt{s} = 8 \text{ TeV}$, $\mathcal{L} = 2 \text{ fb}^{-1}$) datasets. It looks at the decay of $B^0 \rightarrow D^- \mu \nu_\mu$ and $B^0 \rightarrow D^{*-} \mu \nu_\mu$, where the D^- decays to $K^+ \pi^- \pi^-$ and the D^{*-} to $\bar{D}^0 (\rightarrow K^+ \pi^-) \pi^-$. The measurement uses a time-dependent fit to disentangle A_P from a_{sl}^d . The fit for the charge asymmetry as a function of decay time for the $D^- \mu^+$ sample is shown in figure 2. Also for the a_{sl}^d measurement, the dominating systematic uncertainty comes from detection asymmetries of the final state particles, which is determined using similar methods as for the a_{sl}^s measurement. The measured value of a_{sl}^d from LHCb is $a_{\text{sl}}^d = (-0.02 \pm 0.19_{\text{stat}} \pm 0.30_{\text{syst}})\%$ and is, just as the value for a_{sl}^s , the most precise measurement to date. Figure 3 shows all current measurements of a_{sl} including the latest LHCb results.

3. Improvements for the 2012 a_{sl}^s analysis

For the upcoming analysis on the a_{sl}^s measurement for LHCb, the improvements can be divided into two categories: reducing the statistical and systematic uncertainties. The integrated luminosity will be increased by a factor three, reducing the statistical uncertainty. The increase of integrated luminosity also improves the knowledge of the detection asymmetry, which is limited by the size of the control samples. For the 2011 analysis, only the decays of $D_s^- \rightarrow \phi(\rightarrow K^+K^-)\pi^-$ were considered. For the future analysis, also $D_s^- \rightarrow K^{*0}(\rightarrow K^+\pi^-)K^-$ will be included, as well as the remaining phase space as is indicated in figure 4.

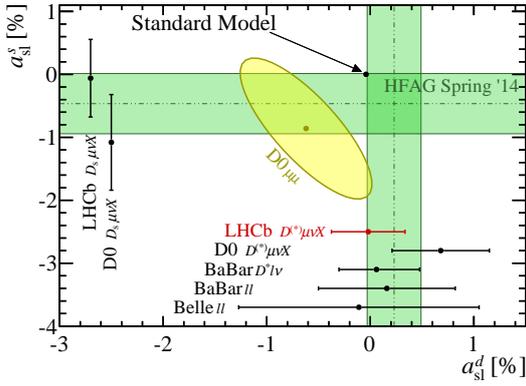


Figure 3: Overview of the measurement results of a_{sl}^s versus a_{sl}^d . The green bands are the average values of the pure a_{sl}^s and a_{sl}^d measurement, excluding the D0 dimuon measurement, which is shown as the yellow ellipse.

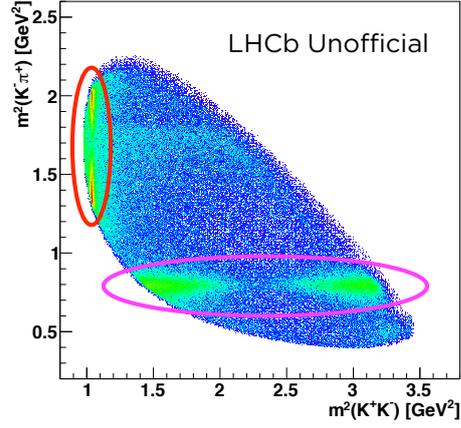


Figure 4: The Dalitz plane for $D_s^- \rightarrow K^+K^-\pi^-$, where D_s^- comes from $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$. Indicated in red is $D_s^- \rightarrow \phi(\rightarrow K^+K^-)\pi^-$, in magenta $D_s^- \rightarrow K^{*0}(\rightarrow K^+\pi^-)K^-$. The remaining phase space will also be analysed

Different studies are ongoing to improve the tracking and detection asymmetries using new methods. One of them uses prompt charm decays to determine both the muon and pion detection asymmetries. The decays that are used are $D^0 \rightarrow K^- \mu^+ \nu_\mu$ and $D^0 \rightarrow K^- \pi^+$. Both are flavour-tagged by requiring them to come from $D^{*+} \rightarrow D^0 \pi_s^+$. The measured asymmetries of these decays can be written as a sum of various production and detection asymmetries, as is done in equation 3.1. Both decays introduce production asymmetries for the D^{*-} and π_s^- , which cancel out it between the two decay modes. This is also the case for the introduced detection asymmetry of the K^+ .

$$\begin{aligned}
 A_{\text{meas}}(K^+ \mu^-) &= A_D(K^+) + A_D(\mu^-) + A_P(D^{*-}) + A_D(\pi_s^-) \\
 A_{\text{meas}}(K^+ \pi^-) &= A_D(K^+) + A_D(\pi^-) + A_P(D^{*-}) + A_D(\pi_s^-) \\
 A_{\text{meas}}(K^+ \pi^-) - A_{\text{meas}}(K^+ \mu^-) &= A_D(\pi^-) + A_D(\mu^+)
 \end{aligned} \tag{3.1}$$

Since the detection and production asymmetries are dependent on the kinematics of the measured particle, asymmetries only cancel when their kinematic distributions are equalised. This has to be done not only for the D^{*-} and K^+ particles between the two control modes, but also for the μ^- and π^+ particles between the control modes and signal mode.

In order to equalise the kinematics of all particles, three reweighting steps are defined:

1. Weight $D^{*+} \rightarrow D^0(\rightarrow K^- \boldsymbol{\pi}^+) \pi_s^+$ to $\bar{B}_s^0 \rightarrow D_s^+(\rightarrow K^+ K^- \boldsymbol{\pi}^+) \mu^- \bar{\nu}_\mu$
2. Weight $D^{*+} \rightarrow D^0(\rightarrow K^- \mu^+ \nu_\mu) \pi_s^+$ to $D^{*+} \rightarrow D^0(\rightarrow K^- \boldsymbol{\pi}^+) \pi_s^+$
3. Weight $\bar{B}_s^0 \rightarrow D_s^+(\rightarrow K^+ K^- \boldsymbol{\pi}^+) \mu^- \bar{\nu}_\mu$ to $D^{*-} \rightarrow D^0(\rightarrow K^+ \boldsymbol{\mu}^- \bar{\nu}_\mu) \pi_s^-$.

After this, mass fits are produced to extract the number of signal events for each of the samples. The reweighting step introduces a change in the effective number of events, N_{eff} , which is defined as $N_{\text{eff}} = (\sum_{i=1}^N w_i)^2 / \sum_{i=1}^N w_i^2$. In this equation, N is the number of candidates, and w_i is the weight of each candidate i . The effective number of signal events is calculated and the final asymmetry that is determined includes not only the tracking asymmetries of the pion and muon, but also the muon identification asymmetry and the interaction asymmetry of the pion with the detector: $A_{\mu\pi} = A_{\mu}^{\text{ID}} + A_{\mu}^{\text{track}} + A_{\pi}^{\text{track}} + A_{\pi}^{\text{interaction}}$.

4. Conclusion and Outlook

The semileptonic asymmetry a_{sl} provides a method to measure CP violation in mixing. The D0 experiment has found values for this asymmetry which are inconsistent with the Standard Model. The LHCb experiment measured a value for $a_{\text{sl}}^s = (-0.06 \pm 0.50_{\text{stat}} \pm 0.36_{\text{syst}})\%$, using $\mathcal{L} = 1.0 \text{ fb}^{-1}$ and a value for $a_{\text{sl}}^d = (-0.02 \pm 0.19_{\text{stat}} \pm 0.30_{\text{syst}})\%$ using $\mathcal{L} = 3 \text{ fb}^{-1}$. These values do not exclude either the Standard Model or the D0 values. Using their full 3 fb^{-1} dataset and new methods for determining charge asymmetries, LHCb will measure a more precise value for a_{sl}^s . In 2015, the LHC will start running again and with the increased energies, the dataset will be expanded faster, such that by the end of Run-II, a precision better than 10^{-3} will be reached. This will allow making a firmer statement on the D0 measurement as well as probing new physics contributions from beyond the SM.

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