

## Searching for SUSY and decaying gravitino DM at the LHC and Fermi-LAT with the $\mu\nu$ SJM

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The ‘ $\mu$  from  $\nu$ ’ supersymmetric standard model ( $\mu\nu$ SJM) solves the  $\mu$  problem of supersymmetric models and reproduces neutrino data, simply using couplings with the three families of right-handed neutrinos  $\nu$ 's. Novel signatures of supersymmetry at the LHC are expected through these new states, and couplings breaking  $R$  parity. All supersymmetric particles are potential candidates for the lightest one, which is not stable leading to prompt of displaced vertices and producing final states with multi-leptons/taus/jets/photons and missing energy. Besides, a decaying gravitino turns out to be an interesting candidate for dark matter. It can be searched through gamma-ray observations, such as those of the Fermi Large Area Telescope. The latter already impose an upper bound on the gravitino mass of the order of 5-20 GeV, depending on the region of the parameter space of the model.

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## 1. Introduction

Supersymmetry (SUSY) is still the most compelling theory for physics beyond the standard model. SUSY not only solves several important theoretical problems of the standard model, such as the gauge hierarchy problem and others, but also has spectacular experimental implications. As is well known, the spectrum of elementary particles is doubled with masses of about 1 TeV, thus even the simplest SUSY model, the minimal supersymmetric standard model (MSSM), predicts a rich phenomenology. However, the LHC started operations several years ago and, with Run 1 already finished, SUSY has not been discovered yet. Because of this, it has been raised the question of whether SUSY is still alive. The question is fair of course, but in our opinion the answer is yes, and we think that there are several arguments in favor of this answer. Here there are some of them:

- The lower bounds on SUSY particle (sparticle) masses are smaller than 1 TeV or about that number, depending on the sparticle analyzed. Thus they are still reasonable, and in that sense we can keep in mind the history of the Higgs boson.

- Because of the complicated parameter space of SUSY, experimentalists use in their analyses simplified models that do not cover the full MSSM. For example, branching-ratio variations are not considered in much detail, and other assumptions are also made.

- Run 2 is going on, and for the moment with a low luminosity of about  $20 \text{ fb}^{-1}$ . Therefore, to (be prepared) wait for the results with higher luminosity seems to be a sensible strategy, since  $100 \text{ fb}^{-1}$  are expected for the end of the Run 2.

- Most searches at the LHC assume  $R$ -parity conservation (RPC), with the lightest supersymmetric particle (LSP) stable, requiring therefore missing energy in the final state to claim for SUSY detection. But, if  $R$  parity is violated (RPV), sparticles can decay to standard model particles, and the bounds on their masses can become significantly weaker.

Nevertheless, despite all these arguments, it is also honest to recognize that SUSY has its own theoretical problems in its formulation at low energy. and, in particular, a crucial one is the so-called  $\mu$  problem [1]. In the superpotential of the MSSM

$$W = \varepsilon_{ab} \left( Y_{u_{ij}} \hat{H}_u^b \hat{Q}_i^a \hat{u}_j^c + Y_{d_{ij}} \hat{H}_d^a \hat{Q}_i^b \hat{d}_j^c + Y_{e_{ij}} \hat{H}_d^a \hat{L}_i^b \hat{e}_j^c \right) - \varepsilon_{ab} \mu \hat{H}_d^a \hat{H}_u^b, \quad (1.1)$$

the presence of the mass parameter  $\mu$  is necessary, for example to generate Higgsino masses given the current experimental lower bounds of about 100 GeV. In the presence of a high-energy theory like a GUT or string theory, with a typical scale of the order of  $10^{16}$  GeV or larger, and/or a gravitational theory at the Planck scale, one should be able to explain how to obtain a mass parameter in the superpotential of the order of the electroweak scale. The MSSM does not solve the  $\mu$  problem. One takes for granted that the  $\mu$  term is there and that is of the order of the TeV, and that's it. In this sense, the MSSM is a kind of effective theory.

From the experimental viewpoint, another problem of SUSY is to be able to reproduce neutrino data, i.e. masses and mixing angles. Let us emphasize that in the MSSM, by construction, neutrinos are massless.

The ' $\mu$  from  $\nu$ ' supersymmetric standard model ( $\mu\nu$ SJM) [2, 3, 4, 5], includes new couplings with right-handed (RH) neutrino superfields in the superpotential in order to solve the  $\mu$ -problem, while simultaneously explains the origin of neutrino masses. The  $SU(3)_c \times SU(2)_L \times U(1)_Y$  invariant couplings  $\lambda_i \hat{\nu}_i^c \hat{H}_d \hat{H}_u$  generate an effective  $\mu$  term through RH sneutrino vacuum expect-

tation values (VEVs),  $\langle \tilde{\nu}_i^c \rangle \equiv v_{\nu_i^c}$ , after the successful electroweak symmetry breaking (EWSB):  $\mu^{eff} = \lambda_i v_{\nu_i^c}$ . In addition, the other gauge invariant couplings  $\kappa_{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c$  generate effective Majorana masses for the RH neutrinos,  $M_{ij}^{eff} = 2\kappa_{ijk} v_{\nu_k^c}$ , giving rise to a generalized electroweak-scale seesaw mechanism which can reproduce the observed neutrino masses and mixing angles. We will review this solution to the  $\mu$  problem and neutrino physics in Section 2.

On the other hand, sparticles do not appear in pairs in the couplings that solve these problems, thus we say that  $R$  parity is (explicitly) broken. The latter implies that the phenomenology of the  $\mu\nu$ SJM is very different from the one of the MSSM. We will briefly review this phenomenology at the LHC in Section 3, where we will see that since the LSP is not stable because of RPV, it decays leading to prompt or displaced vertices, and producing final states with multi-leptons/taus/jets/photons and missing energy.

In RPV models, the usual sparticle candidates for the dark matter (DM) of the Universe in the case of RPC, the neutralino or the RH sneutrino, have very short lifetimes, and therefore can no longer be used. Nevertheless, the gravitino can still be a candidate for DM since its lifetime is typically very long, being suppressed both by the gravitational interaction and by the small RPV couplings. In Section 4, we will discuss the feasibility of gravitino DM in the  $\mu\nu$ SJM, whereas in Section 5 its possible detection in gamma-ray satellite experiments, such as the Fermi Large Area Telescope (LAT), will be analyzed. Our conclusions are left for Section 6

## 2. The $\mu\nu$ SJM

The superpotential of the  $\mu\nu$ SJM contains in addition to the MSSM Yukawas for quarks and charged leptons, Yukawas for neutrinos and the two couplings discussed in the introduction that generate the effective  $\mu$  term and Majorana masses [2, 3]:

$$W = \varepsilon_{ab} \left( Y_{u_{ij}} \hat{H}_u^b \hat{Q}_i^a \hat{u}_j^c + Y_{d_{ij}} \hat{H}_d^a \hat{Q}_i^b \hat{d}_j^c + Y_{e_{ij}} \hat{H}_d^a \hat{L}_i^b \hat{e}_j^c + Y_{\nu_{ij}} \hat{H}_u^b \hat{L}_i^a \hat{\nu}_j^c \right) - \varepsilon_{ab} \lambda_i \hat{\nu}_i^c \hat{H}_d^a \hat{H}_u^b + \frac{1}{3} \kappa_{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c. \quad (2.1)$$

Notice that in the limit  $Y_{\nu_{ij}} \rightarrow 0$ ,  $\hat{\nu}_i^c$  can be identified as pure singlet superfields without lepton number, similar to the case of the next-to-minimal supersymmetric standard model (NMSSM) [6], where one singlet is added to the spectrum and there is RPC. Thus RPV in the  $\mu\nu$ SJM is determined by the values of the neutrino Yukawa couplings, and as a consequence it is small.

Since only dimensionless trilinear couplings are present in (2.1), the EWSB is determined by the usual soft SUSY-breaking terms of the scalar potential. Thus all known particle physics phenomenology can be reproduced in the  $\mu\nu$ SJM with one scale, avoiding the introduction of *ad-hoc* high-energy scales. To realize this, let us remember that in addition to the soft terms the tree-level neutral scalar potential receives the  $D$  and  $F$  term contributions that can be found in Refs. [2, 3]. With the choice of CP conservation,<sup>1</sup> after the EWSB the neutral scalars develop in general the following real VEVs:

$$\langle H_d^0 \rangle = v_d, \quad \langle H_u^0 \rangle = v_u, \quad \langle \tilde{\nu}_i \rangle = v_{\nu_i}, \quad \langle \tilde{\nu}_i^c \rangle = v_{\nu_i^c}, \quad (2.2)$$

<sup>1</sup> $\mu\nu$ SJM with spontaneous CP violation was studied in Ref. [7].

where in addition to the usual VEVs of the MSSM Higgses,  $H_u^0$  and  $H_d^0$ , the new couplings generate VEVs for left-handed (LH) sneutrinos,  $\tilde{\nu}_i$ , as well as for the RH sneutrinos,  $\tilde{\nu}_i^c$ . The eight minimization conditions can be written as

$$m_{H_d}^2 = -\frac{1}{4}G^2 (v_{\nu_i}v_{\nu_i} + v_d^2 - v_u^2) - \lambda_i\lambda_j v_{\nu_i^c}v_{\nu_j^c} - \lambda_i\lambda_i v_u^2 + v_{\nu_i^c} \tan\beta \left( a_{\lambda_i} + \lambda_j \kappa_{ijk} v_{\nu_k^c} \right) + Y_{\nu_{ij}} \frac{v_{\nu_i}}{v_d} \left( \lambda_k v_{\nu_k^c} v_{\nu_j^c} + \lambda_j v_u^2 \right), \quad (2.3)$$

$$m_{H_u}^2 = \frac{1}{4}G^2 (v_{\nu_i}v_{\nu_i} + v_d^2 - v_u^2) - \lambda_i\lambda_j v_{\nu_i^c}v_{\nu_j^c} - \lambda_j\lambda_j v_d^2 + 2\lambda_j Y_{\nu_{ij}} v_{\nu_i} v_d - Y_{\nu_{ij}} Y_{\nu_{ik}} v_{\nu_k^c} v_{\nu_j^c} - Y_{\nu_{ij}} Y_{\nu_{kj}} v_{\nu_i} v_{\nu_k} + v_{\nu_i^c} \frac{1}{\tan\beta} \left( a_{\lambda_i} + \lambda_j \kappa_{ijk} v_{\nu_k^c} \right) - \frac{v_{\nu_i}}{v_u} \left( a_{\nu_{ij}} v_{\nu_j^c} + Y_{\nu_{ij}} \kappa_{ljk} v_{\nu_l^c} v_{\nu_k^c} \right), \quad (2.4)$$

$$m_{\tilde{\nu}_{ij}^c}^2 v_{\nu_j^c} = -a_{\nu_{ji}} v_{\nu_j} v_u + a_{\lambda_i} v_u v_d - a_{\kappa_{ijk}} v_{\nu_j^c} v_{\nu_k^c} - \lambda_i \lambda_j (v_u^2 + v_d^2) v_{\nu_j^c} + 2\lambda_j \kappa_{ijk} v_d v_u v_{\nu_k^c} - 2\kappa_{lim} \kappa_{ljk} v_{\nu_m^c} v_{\nu_j^c} v_{\nu_k^c} + Y_{\nu_{ji}} \lambda_k v_{\nu_j} v_{\nu_k^c} v_d + Y_{\nu_{kj}} \lambda_i v_d v_{\nu_k^c} v_{\nu_j^c} - 2Y_{\nu_{jk}} \kappa_{ikl} v_u v_{\nu_l} v_{\nu_j^c} v_{\nu_k^c} - Y_{\nu_{ji}} Y_{\nu_{lk}} v_{\nu_j} v_{\nu_l} v_{\nu_k^c} - Y_{\nu_{ki}} Y_{\nu_{kj}} v_u^2 v_{\nu_j^c}, \quad (2.5)$$

$$m_{L_{ij}}^2 v_{\nu_j} = -\frac{1}{4}G^2 (v_{\nu_j}v_{\nu_j} + v_d^2 - v_u^2) v_{\nu_i} - a_{\nu_{ij}} v_u v_{\nu_j^c} + Y_{\nu_{ij}} \lambda_k v_d v_{\nu_k^c} v_{\nu_j^c} + Y_{\nu_{ij}} \lambda_j v_u^2 v_d - Y_{\nu_{il}} \kappa_{ljk} v_u v_{\nu_j^c} v_{\nu_k^c} - Y_{\nu_{ij}} Y_{\nu_{lk}} v_{\nu_l} v_{\nu_j^c} v_{\nu_k^c} - Y_{\nu_{ik}} Y_{\nu_{jk}} v_u^2 v_{\nu_j^c}, \quad (2.6)$$

where the low-energy soft masses  $m_{H_d}^2$ ,  $m_{H_u}^2$ ,  $m_{\tilde{\nu}_{ij}^c}^2$  and  $m_{L_{ij}}^2$  are calculated as functions of the VEVs  $v_d$ ,  $v_u$ ,  $v_{\nu_j^c}$ ,  $v_{\nu_i}$ , and inspired by the structure of supergravity the soft trilinear parameters are taken directly proportional to the couplings, e.g.,  $a_{\lambda_i} = A_{\lambda_i} \lambda_i$ ,  $a_{\kappa_{ijk}} = A_{\kappa_{ijk}} \kappa_{ijk}$ ,  $a_{\nu_{ij}} = A_{\nu_{ij}} Y_{\nu_{ij}}$ , etc.

As can be easily seen from Eq. (2.5), the VEVs of the RH sneutrinos,  $v_{\nu_j^c}$ , are naturally of the order of the EWSB scale. This confirms that the 6<sup>th</sup> term in the superpotential (2.1) generates the effective Majorana masses for RH neutrinos, as discussed in the Introduction. Thus we can implement naturally an electroweak-scale seesaw in the  $\mu\nu$ SJM, asking for neutrino Yukawa couplings of the order of the electron Yukawa coupling or smaller,  $Y_{\nu_{ij}} \sim 10^{-6} - 10^{-7}$  [2, 3, 8, 9, 7, 10, 5, 11], i.e. we work with Dirac masses for neutrinos,  $m_D \sim Y_{\nu} v_u$ , of the order or smaller than about  $10^{-4}$  GeV. On the other hand, the VEVs of the LH sneutrinos,  $v_{\nu_i}$ , are much smaller than the other VEVs (2.2) in the  $\mu\nu$ SJM. Notice in this respect that in Eq. (2.6),  $v_{\nu} \rightarrow 0$  as  $Y_{\nu} \rightarrow 0$ . It is then easy to estimate the values of  $v_{\nu}$  as of the order or smaller than  $m_D$  [2].

As is well known, the couplings and Higgs VEVs present in the MSSM (determined by the superpotential (1.1)) generate the mixing of neutral gauginos and Higgsinos, where the eigenstates are the so-called neutralinos. A similar situation occurs in the  $\mu\nu$ SJM. However, in this model there are new couplings and VEVs (see Eqs. (2.1) and (2.2)), implying larger mass matrices than those of the MSSM/NMSSM. In particular, in the case of the neutralinos, they turn out to be also mixed with the LH and RH neutrinos. Besides, we saw before that Majorana masses for RH neutrinos are generated dynamically, thus they will behave as the singlino components of the neutralinos. Altogether, in a basis where  $\chi^{0T} = (\tilde{B}^0, \tilde{W}^0, \tilde{H}_d, \tilde{H}_u, \nu_{R_i}, \nu_{L_i})$ , one obtains the following  $10 \times 10$  neutral fermion (neutralino-neutrino) mass matrix [2, 3]:

$$\mathcal{M}_n = \begin{pmatrix} M & m \\ m^T & 0_{3 \times 3} \end{pmatrix}, \quad (2.7)$$

with

$$M = \begin{pmatrix} M_1 & 0 & -Av_d & Av_u & 0 & 0 & 0 \\ 0 & M_2 & Bv_d & -Bv_u & 0 & 0 & 0 \\ -Av_d & Bv_d & 0 & -\lambda_i v_{V_i^c} & -\lambda_1 v_u & -\lambda_2 v_u & -\lambda_3 v_u \\ Av_u & -Bv_u & -\lambda_i v_{V_i^c} & 0 & -\lambda_1 v_d + Y_{V_{i1}} v_{V_i} & -\lambda_2 v_d + Y_{V_{i2}} v_{V_i} & -\lambda_3 v_d + Y_{V_{i3}} v_{V_i} \\ 0 & 0 & -\lambda_1 v_u & -\lambda_1 v_d + Y_{V_{i1}} v_{V_i} & 2\kappa_{11j} v_{V_j^c} & 2\kappa_{12j} v_{V_j^c} & 2\kappa_{13j} v_{V_j^c} \\ 0 & 0 & -\lambda_2 v_u & -\lambda_2 v_d + Y_{V_{i2}} v_{V_i} & 2\kappa_{21j} v_{V_j^c} & 2\kappa_{22j} v_{V_j^c} & 2\kappa_{23j} v_{V_j^c} \\ 0 & 0 & -\lambda_3 v_u & -\lambda_3 v_d + Y_{V_{i3}} v_{V_i} & 2\kappa_{31j} v_{V_j^c} & 2\kappa_{32j} v_{V_j^c} & 2\kappa_{33j} v_{V_j^c} \end{pmatrix}, \quad (2.8)$$

where  $A \equiv \frac{G}{\sqrt{2}} \sin \theta_W$ ,  $B \equiv \frac{G}{\sqrt{2}} \cos \theta_W$ , with  $G^2 \equiv g_1^2 + g_2^2$ , and

$$m^T = \begin{pmatrix} -\frac{g_1}{\sqrt{2}} v_{V_1} & \frac{g_2}{\sqrt{2}} v_{V_1} & 0 & Y_{V_{1i}} v_{V_i^c} & Y_{V_{11}} v_u & Y_{V_{12}} v_u & Y_{V_{13}} v_u \\ -\frac{g_1}{\sqrt{2}} v_{V_2} & \frac{g_2}{\sqrt{2}} v_{V_2} & 0 & Y_{V_{2i}} v_{V_i^c} & Y_{V_{21}} v_u & Y_{V_{22}} v_u & Y_{V_{23}} v_u \\ -\frac{g_1}{\sqrt{2}} v_{V_3} & \frac{g_2}{\sqrt{2}} v_{V_3} & 0 & Y_{V_{3i}} v_{V_i^c} & Y_{V_{31}} v_u & Y_{V_{32}} v_u & Y_{V_{33}} v_u \end{pmatrix}. \quad (2.9)$$

The structure of this mass matrix is that of a generalized electroweak-scale seesaw, since it involves not only the RH neutrinos but also the neutralinos. Because of this structure, data on neutrino physics can easily be reproduced at tree level [2, 3, 8, 7, 10], even with diagonal Yukawa couplings  $Y_{V_i}$  [8, 7]. Qualitatively, we can understand this in the following way. First of all, neutrino masses are going to be very small since the entries of the matrix  $M$  are much larger than the ones of the matrix  $m$ . Notice in this sense that the entries of  $M$  are of the order of the electroweak scale, whereas the ones in  $m$  are of the order of the Dirac masses for neutrinos [2, 3]. Second, from the above matrices, one can obtain a simplified formula for the effective neutrino mixing mass matrix [7]:

$$(m_V^{eff})_{ij} \simeq \frac{Y_{V_i} Y_{V_j} v_u^2}{6\kappa v_{V_i^c}} (1 - 3\delta_{ij}) - \frac{v_{V_i} v_{V_j}}{2M}, \quad (2.10)$$

where  $M \equiv \frac{M_1 M_2}{g_1^2 M_2 + g_2^2 M_1}$ . Using this formula it is easy to understand how diagonal Yukawas,  $Y_{V_{ii}} = Y_{V_i}$  and vanishing otherwise, can give rise to off-diagonal entries in the mass matrix. One of the key points is the extra contribution given by the first term of Eq. (2.10) with respect to the ordinary seesaw where it is absent. Another extra contribution to the off-diagonal entries is the third term generated through the mixing of LH neutrinos with gauginos.

In a sense, all these arguments give an answer to the question why the mixing angles are so different in the quark and lepton sectors: because no generalized seesaw exists for the quarks.

For the rest of the mass matrices of the  $\mu\nu$ SJM, a similar situation occurs and the new couplings and sneutrino VEVs induce new mixing of states [2, 3]. Summarizing, there are the ten neutral fermions (neutralinos-neutrinos) discussed before, five charged fermions (charginos-charged leptons), seven CP-odd and eight CP-even neutral scalars (Higgses-sneutrinos), and seven charged scalars (charged Higgses-sleptons). As a consequence, the phenomenology of the  $\mu\nu$ SJM is very different from the one of the MSSM/NMSSM, and we will briefly introduce it in the next sections.

### 3. LHC phenomenology

As is well known, the phenomenology of models with RPV differs substantially from that of models with RPC. Needless to mention, the LSP is no longer stable, and therefore not all SUSY chains must yield missing energy events at colliders. In particular, in the  $\mu\nu$ SJM, depending on the value of the couplings, the LSP decays leading to prompt or displaced vertices, and producing final states with multi-leptons/taus/jets/photons and missing energy. This unusual phenomenology was explored first in Refs. [9, 12, 13, 14], discussing the decay properties of the LSP assumed to be the lightest neutralino, as well as novel Higgs decays. Further, detailed collider analyses for a Higgs-like scalar decaying into a pair of neutralinos was also discussed in Refs. [12, 14], provided that these states lie below in the mass spectrum. More recently, this issue was revisited and, under the same assumption, a Higgs-like scalar decaying to a pair of scalars/pseudoscalars was also considered [15]. The case of non-standard on-shell decays of  $W^\pm$  and Z bosons to light singlet-like scalar(s), pseudoscalar(s) and neutralinos(s) was studied in Ref. [16].

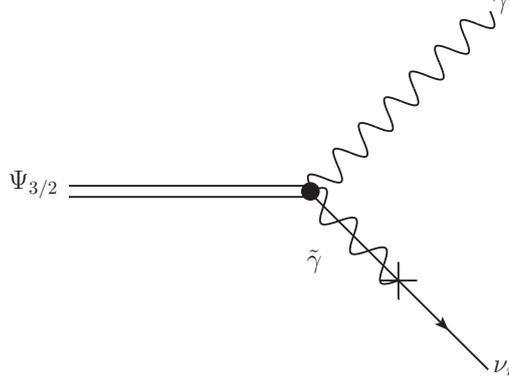
On the other hand, all sparticles are potential LSP's in RPV models, since the problem of stable charged particles as DM is not present. So to study the whole potential phenomenology of the  $\mu\nu$ SJM at the LHC, we should be prepared to analyze systematically not only the usual lightest neutralino as the LSP, but also staus, squarks, charginos, and sneutrinos as LSP's with a wide range of masses. In a first detailed analysis [17] we have concentrated in the LH sneutrino as the LSP. We have shown that for a sneutrino mass in the range about 95 – 145 GeV, a diphoton signal plus leptons, or plus missing transverse energy (from neutrinos), is observable at the LHC, even at the current Run 2 with  $100 \text{ fb}^{-1}$  of luminosity. The dominant sneutrino pair production channels are the direct production via a Z boson, or through a  $W^\pm$  decaying into a sneutrino and a LH charged slepton next-to-LSP, with the latter decaying into another sneutrino plus a very soft  $W^\pm$ . We think that these signals (where one of the sneutrinos decays in a way not very different from the Higgs) are worthy of attention by our experimental colleagues.

### 4. Gravitino dark matter

As already mentioned in the Introduction, the gravitino is an interesting candidate for DM in RPV models. This occurs when it becomes the LSP. The gravitino has an interaction term in the supergravity Lagrangian with the photon and the photino. Since the photino and the LH neutrinos are mixed in the neutral fermion mass matrix due to the RPV, as discussed in Eq. (2.7), the gravitino will be able to decay into a photon and a neutrino, as shown in Fig. 1. Nevertheless, this decay is suppressed both by the gravitational interaction and by the small R-parity violating coupling, making the gravitino lifetime much longer than the age of the Universe [18]. From the supergravity Lagrangian one obtains

$$\Gamma\left(\Psi_{3/2} \rightarrow \sum_i \gamma\nu_i\right) \simeq \frac{1}{32\pi} |U_{\tilde{\gamma}\nu}|^2 \frac{m_{3/2}^3}{M_P^2}, \quad (4.1)$$

where  $M_P = 2.4 \times 10^{18} \text{ GeV}$  is the reduced Planck mass,  $m_{3/2}$  is the gravitino mass, and  $|U_{\tilde{\gamma}\nu}|^2$



**Figure 1:** Tree-level diagram for the two-body decay of a gravitino into a photon and a neutrino, via RPV photino-neutrino mixing.

determines the neutrino content of the photino:

$$|U_{\tilde{\gamma}\nu}|^2 = \sum_{i=1}^3 |N_{i1} \cos \theta_W + N_{i2} \sin \theta_W|^2. \quad (4.2)$$

Here  $N_{i1}$  ( $N_{i2}$ ) is the Bino (Wino) component of the  $i$ -th neutrino. The lifetime of the gravitino can then be written as

$$\tau_{3/2} \simeq 3.8 \times 10^{27} \text{ s} \left( \frac{|U_{\tilde{\gamma}\nu}|^2}{10^{-16}} \right)^{-1} \left( \frac{m_{3/2}}{10 \text{ GeV}} \right)^{-3}. \quad (4.3)$$

If  $|U_{\tilde{\gamma}\nu}|^2$  is small enough, the gravitino can be very long lived compared to the current age of the Universe which is about  $4 \times 10^{17}$  s.

We can easily estimate the value of  $|U_{\tilde{\gamma}\nu}|^2$  in the  $\mu\nu$ SJM [19]. Using the mass insertion technique, from the entries in the neutral fermion mass matrix (2.7) and Fig. 1, we can deduce that the relevant coupling for the mixing between the photino and the neutrinos is given approximately by  $|U_{\tilde{\gamma}\nu}|^2 \sim \left| \frac{g_{1\nu\tilde{\nu}}}{M_1} \right|^2 \sim 10^{-6} - 10^{-8}$ , giving rise to

$$10^{-16} \lesssim |U_{\tilde{\gamma}\nu}|^2 \lesssim 10^{-12}. \quad (4.4)$$

One can confirm this estimation performing a scan of the low-energy parameter space of the  $\mu\nu$ SJM with the exact formulas above [19]. As a result of the scan, typically the mass of the neutralino is above 20 GeV, and since  $m_{3/2}$  is constrained to be smaller than that value, as we will see, the gravitino can safely be used as the LSP. Let us remark then, that under this assumption of gravitino DM, each candidate for LSP mentioned in the previous section would in fact be the next-to-LSP, since the gravitino would be the LSP. Nevertheless, the analysis of its phenomenology at the LHC would not be altered since it would also decay into ordinary particles using the same channels as if it were the LSP. Thus our analysis there can be applied exactly the same for the case of neutralino/sneutrino/stau/squark/chargedino NLSP with the gravitino as the LSP.

On the other hand, for the gravitino to be a good DM candidate we still need to check that it can be present in the right amount to explain the observed relic density  $\Omega_{DM} h^2 \simeq 0.1$ . With the

introduction of inflation, the primordial gravitinos are diluted during the exponential expansion of the Universe. Nevertheless, after inflation, in the reheating process, the gravitinos are reproduced again from the relativistic particles in the thermal bath. The yield of gravitinos from the scatterings is proportional to the reheating temperature,  $T_R$ , and estimated to be [20]

$$\Omega_{3/2} h^2 \simeq 0.27 \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \left( \frac{100 \text{ GeV}}{m_{3/2}} \right) \left( \frac{M_{\tilde{g}}}{1 \text{ TeV}} \right)^2, \quad (4.5)$$

where  $M_{\tilde{g}}$  is the gluino mass. As is well known, adjusting the reheating temperature one can reproduce the correct relic density for each possible value of the gravitino mass. For example for  $m_{3/2}$  of the order of 1 – 1000 GeV one obtains  $\Omega_{3/2} h^2 \simeq 0.1$  for  $T_R \sim 10^8 - 10^{11}$  GeV, with  $M_{\tilde{g}} \sim 1$  TeV. Even with a high value of  $T_R$  there is no gravitino problem, since the next-to-LSP decays to standard model particles much earlier than BBN epoch via RPV interactions.

Thus, the gravitino, which is a super-weakly interacting massive particle (superWIMP), represents a good DM candidate. Most importantly, as pointed out in Ref. [18] for the case of RPV, gravitino decays in the Milky Way halo would produce monochromatic gamma rays with an energy equal to half of the gravitino mass, and therefore its presence can, in principle, be inferred indirectly from gamma-ray observations. We will discuss this crucial issue in the next section.

## 5. Detection of gravitino dark matter

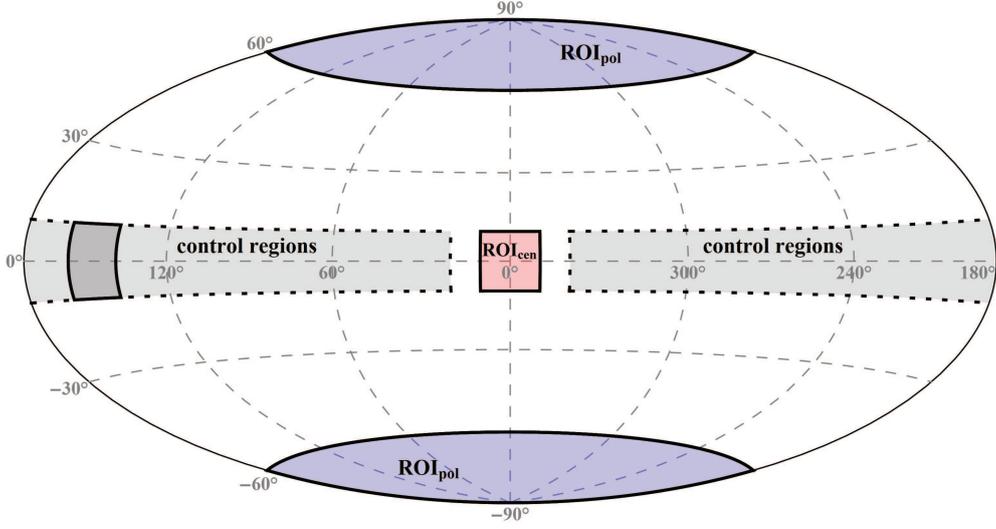
The detection of gravitino DM in several RPV scenarios has been studied in the literature considering the case of gravitinos emitting gamma rays when decaying in the smooth galactic halo and extragalactic regions at cosmological distances [18, 21, 19, 22, 23], and also in nearby extragalactic structures [24]. In the interesting case of the galactic halo, the gamma-ray signal is an anisotropic sharp line and the flux is given by

$$\frac{d\Phi}{dE}(E) = \frac{\delta(E - \frac{m_{3/2}}{2})}{4\pi\tau_{3/2}m_{3/2}} \int_{\text{los}} \rho_{\text{halo}}(\vec{l}) d\vec{l}. \quad (5.1)$$

It is worth noting that this equation has two independent factors. The first one corresponds to the particle physics properties of the DM candidate. In particular, its lifetime,  $\tau_{3/2}$ , its mass,  $m_{3/2}$ , and a delta function associated to the fact that the gravitino decays into a photon (and a neutrino), producing therefore a line with an energy equal to  $m_{3/2}/2$ . The second factor corresponds to the astrophysics and is given by the integral along the line of sight  $l$  of the halo DM density.

A first analysis in the  $\mu\nu$ SJM of the possible detection of this kind of signal in the Fermi-LAT was carried out in Ref. [19]. Taking into account the data reported by Fermi at that time, from the non-observation of lines it was possible to constrain the lifetime and the mass of the gravitino. In particular, the mass has to be around 10 GeV or smaller. In a more recent work together with Fermi-LAT members [23], a search for 100 MeV to 10 GeV gamma-ray lines was carried out using 62 months of Fermi-LAT data, and the implications for gravitino DM in the  $\mu\nu$ SJM were analyzed. In this category 2 paper of the Fermi-LAT collaboration we used an Einasto profile with a finite central density [25, 26]:

$$\rho_{\text{Ein}}(r) = \rho_{\odot} \exp \left( -\frac{2}{\alpha} \left( \left( \frac{r}{r_s} \right)^{\alpha} - \left( \frac{R_{\odot}}{r_s} \right)^{\alpha} \right) \right), \quad (5.2)$$



**Figure 2:** Skymap of the ROI used in our analysis [23]; plotted in Galactic coordinates using the Hammer Aitoff projection. The region  $\text{ROI}_{pol}$  (blue) is optimized for the signal-to-background ratio in the case of DM decay, while the region  $\text{ROI}_{cen}$  (red) is optimised for the signal-to-background ratio in the case of DM annihilation. The dashed line encloses the area for the control regions along the Galactic plane (light gray), while the gray region is an example of one of the 31 control regions used in the analysis.

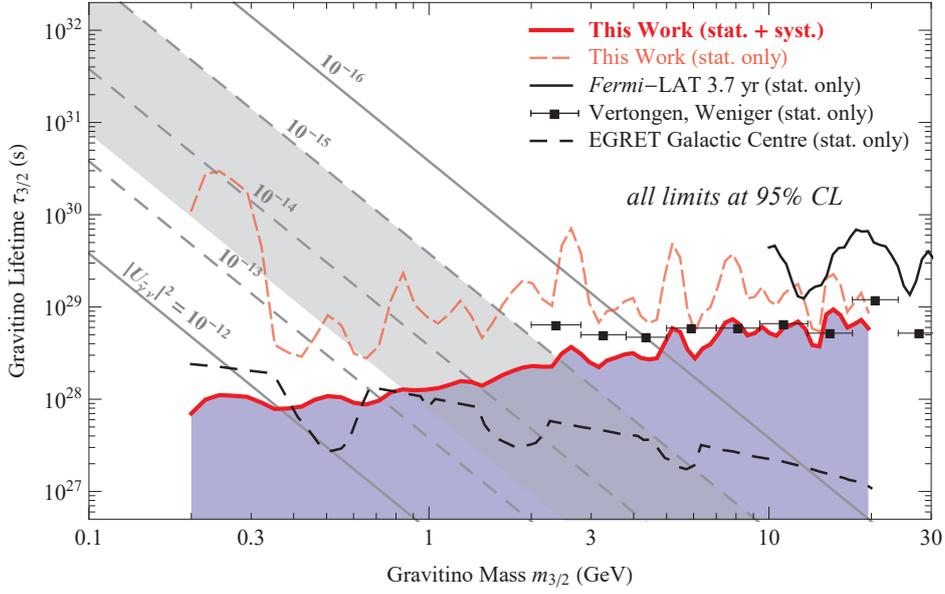
where we adopted  $\alpha = 0.17$  and  $r_s = 20 \text{ kpc}$  for the case of the Milky Way and a local DM density of  $\rho_\odot \simeq 0.4 \text{ GeV cm}^{-3}$  [27, 28, 29]. Other halo profiles as well as uncertainties on the halo parameters were also taken into account, but all these profiles behave similar in the outer part of the Milky Way, where is our region of interest (ROI), and therefore the results are similar. Concerning the ROI, we selected one that optimize the signal-to-background ratio for searches for decay, where the Galactic poles are included,  $\text{ROI}_{pol} : |b| > 60^\circ$ . This is shown in Fig. 2

The final result of the analysis is shown in Fig. 3. We did not find any statistically significant spectral lines and have set robust limits on DM interactions that would produce monochromatic gamma rays. When these limits are applied to the  $\mu\nu$ S $\overline{\text{SM}}$ , under the assumption that the gravitino is the DM, we find that the mass must be  $m_{3/2} < 4.8 \text{ GeV}$  and the lifetime  $\tau_{3/2} > 7.9 \times 10^{27} \text{ s}$  at 95% CL if we assume that all the DM in the Universe is in the form of gravitinos.

In a work in preparation [30], we are performing a deeper exploration of the  $\mu\nu$ S $\overline{\text{SM}}$ , taking also into account 3-body final states in the computation. The preliminary result shows that in some regions of the parameter space is possible to increase the upper bound on the gravitino mass to about 20 GeV.

## 6. Conclusions

The  $\mu\nu$ S $\overline{\text{SM}}$  is an interesting model that solves the  $\mu$  problem of SUSY models and reproduces neutrino data, simply using couplings with the three families of RH neutrinos. These new couplings produce RPV, generating a phenomenology very different from the one of the MSSM or the NMSSM. We have shown that novel signatures of SUSY at the LHC are expected. In particular,



**Figure 3:** Result of Ref. [23], where the parameter space of decaying gravitino DM is given in terms of the gravitino lifetime and the gravitino mass. The diagonal band shows the allowed parameter space for gravitino DM in the  $\mu\nu$ SJM. The numbers on the solid and dashed lines show the corresponding value of the photino/neutrino mixing parameter, as discussed in section 4. The theoretically most favored region is colored in gray. We also show several 95% CL lower limits on the gravitino lifetime coming from gamma-ray observations. The blue shaded region is excluded by the limits derived in the paper.

all sparticles are potential candidates for the LSP, not only the usual lightest neutralino but also the lightest stau, squark, chargino, sneutrino. The LSP is not stable leading to prompt or displaced vertices, and producing final states with multi-leptons/taus/jets/photons and missing energy. On the other hand, the gravitino turns out to be an interesting candidate for DM, since its lifetime is longer than the age of the Universe. It can be searched through gamma-ray observations such as those of the Fermi Large Area Telescope. The non-observation of spectral lines allows to set robust limits on the parameters of the model. In particular the gravitino mass must be smaller than about 5-20 GeV.

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