

## Mixing and indirect $CP$ violation in charm mesons at LHCb

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The LHCb experiment has collected the world's largest sample of charmed hadrons. This sample is used to measure  $D^0-\bar{D}^0$  mixing and to search for  $CP$  violation. New measurements of the mixing and  $CP$ -violation parameters  $x_{CP}$ ,  $y_{CP}$ ,  $\Delta x$  and  $\Delta y$  are presented.

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## 1. Introduction

Neutral meson oscillation is the transition between a neutral-flavoured meson and its antiparticle. In neutral charm mesons ( $D^0$ ), it is known as  $D^0-\bar{D}^0$  mixing. This phenomenon involves flavour changing neutral currents through down-type quarks. The study of  $D^0$  mesons is thus complementary to that of mesons containing down-type quark only,  $K^0$  and  $B_{(s)}^0$ , in searches for interactions beyond the Standard Model of particle physics (SM). Because mixing and charge-parity ( $CP$ ) violation in the charm sector are much more suppressed than in the other decays of down-type mesons, large and clean samples of  $D^0$  decays are required. Such large samples can be obtained at the LHCb experiment [1] which has collected the world's largest sample of charm hadrons during the Run 2 operation of the Large Hadron Collider between 2015 and 2018 [2]. In the following sections, two measurements of  $D^0-\bar{D}^0$  mixing and a search for  $CP$  violation performed at the LHCb experiment are presented.

## 2. Model-independent measurement of the charm mixing parameters in

### $\bar{B} \rightarrow D^0(\rightarrow K_S^0\pi^+\pi^-)\mu^-\bar{\nu}_\mu X$ decays

In the SM, the transition between a neutral flavoured meson and its antiparticle is mediated by charged weak interactions involving the exchange of two  $W$  bosons. The oscillation occurs because the mass eigenstates are not eigenstates of the weak interaction. They can be written as a linear combination of flavour eigenstates as  $|D_{1,2}\rangle \equiv p|D^0\rangle \pm q|\bar{D}^0\rangle$ , where  $p$  and  $q$  are complex parameters satisfying  $|p|^2 + |q|^2 = 1$ . The states  $|D_{1,2}\rangle$  conventionally denote as the nearly  $CP$  even ( $D_1$ ) and odd ( $D_2$ ) mass eigenstates, with eigenvalues  $\omega_{1,2} = m_{1,2} - \frac{i}{2}\Gamma_{1,2}$ , where  $m_{1(2)}$  and  $\Gamma_{1(2)}$  are the mass and decay width of the  $D_{1(2)}$  state. The oscillation can simply be described by the dimensionless mass-splitting parameter  $x = (m_1 - m_2)/\Gamma$  and decay-width splitting parameter  $y = (\Gamma_1 - \Gamma_2)/(2\Gamma)$ , where  $\Gamma$  is the average decay width [3].

A recent measurement of these mixing parameters is based on the LHCb dataset of  $D^0 \rightarrow K_S^0\pi^+\pi^-$  decays collected from 2016 to 2018 [4]. The candidates are exclusively selected with the topology of a  $b$  hadron decaying to  $D^0\mu^-\bar{\nu}_\mu X$ , where  $X$  stands for any combination of unreconstructed particles. The  $D^0$  flavour is determined from the charge of muon. The decay  $D^0 \rightarrow K_S^0\pi^+\pi^-$  has a rich resonant structure which can be used to measure the mixing and  $CP$  violation parameters  $x$ ,  $y$ ,  $|q/p|$  and  $\phi \sim \arg(q/p)$  [11]. These are expressed in terms of the  $CP$ -even mixing parameters

$$x_{CP} = \frac{1}{2} \left[ x \cos \phi \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) + y \sin \phi \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \right], \quad (1)$$

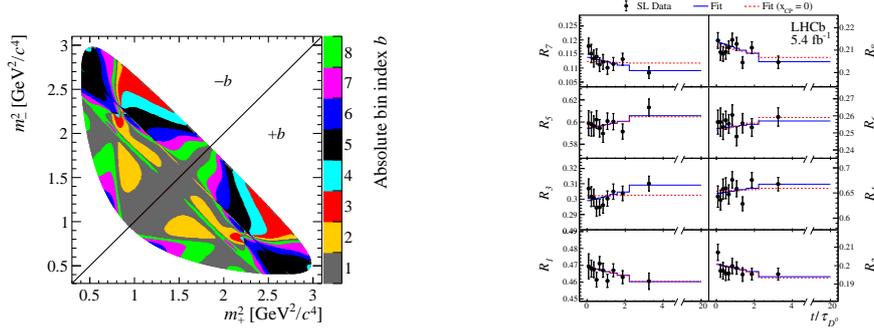
$$y_{CP} = \frac{1}{2} \left[ y \cos \phi \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) - x \sin \phi \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \right], \quad (2)$$

and the  $CP$ -violating differences

$$\Delta x = \frac{1}{2} \left[ x \cos \phi \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) + y \sin \phi \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \right], \quad (3)$$

$$\Delta y = \frac{1}{2} \left[ y \cos \phi \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) - x \sin \phi \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \right]. \quad (4)$$

Absence of  $CP$  violation ( $|q/p| = 1$ ,  $\phi = 0$ ) implies  $x_{CP} = x$ ,  $y_{CP} = y$ , and  $\Delta x = \Delta y = 0$ .



**Figure 1:** (Left) Iso- $\Delta\delta$  binning scheme of the Dalitz plot of the  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  decay;  $m_{\pm}^2$  represents  $m^2(K_S^0 \pi^{\pm})$  for  $D^0$ . (Right) Fit projection of the time-dependent  $CP$ -even yield ratios for  $D^0$  and  $\bar{D}^0$  decays in each Dalitz-plot region.

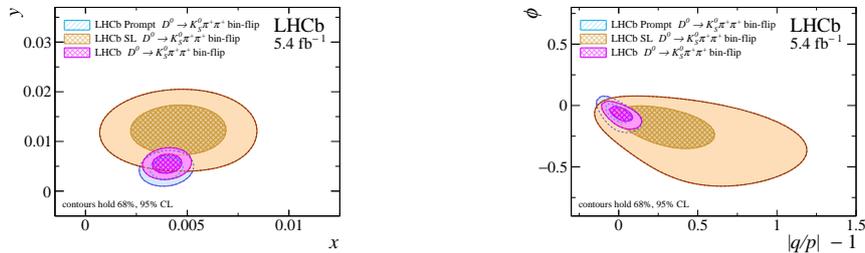
The bin-flip method [5] measures the time-dependent ratio  $R_{bj}^{\pm}$  between positive (upper-half,  $+b$ ) and negative (lower-half,  $-b$ ) Dalitz bins of constant strong phase difference partitioned according to CLEO iso- $\Delta\delta$  binning scheme [6] as shown in Figure 1 (left). The method suppresses most of the biases induced by non-uniform event reconstruction efficiencies. The fit to this time-dependent ratio is shown in Figure 1 (right), yielding

$$\begin{aligned} x_{CP} &= [ 4.29 \pm 1.48 \pm 0.26 ] \times 10^{-3}, & \Delta x &= [ -0.77 \pm 0.93 \pm 0.28 ] \times 10^{-3}, \\ y_{CP} &= [ 12.61 \pm 3.12 \pm 0.83 ] \times 10^{-3}, & \Delta y &= [ 3.01 \pm 1.92 \pm 0.26 ] \times 10^{-3}, \end{aligned}$$

where the first uncertainties are statistical and the second are systematic. The results are compatible with those measured in the analysis of  $D^{*+} \rightarrow D^0(\rightarrow K_S^0 \pi^+ \pi^-) \pi^+$  decays [7]. A combination of the two samples is performed, giving

$$x = (4.01 \pm 0.49) \times 10^{-3}, y = (5.5 \pm 1.3) \times 10^{-3}, |q/p| = 1.012_{-0.048}^{+0.050}, \phi = -0.061_{-0.044}^{+0.037} \text{ rad.}$$

Figure 2 shows the measured mixing and  $CP$ -violating parameters of the two samples and their combination. The value of  $x$  is incompatible with zero with a significance over 8 standard deviations, constituting the most precise measurement from a single experiment. The results are compatible with  $CP$  symmetry.



**Figure 2:** Two-dimensional 68% and 95% confidence-level contours for (left)  $(x, y)$  and (right)  $(|q/p| - 1, \phi)$  for the Run 2  $D^{*+} \rightarrow D^0(\rightarrow K_S^0 \pi^+ \pi^-) \pi^+$  (Prompt) [7] and  $B \rightarrow D^0(\rightarrow K_S^0 \pi^+ \pi^-) \mu^- \bar{\nu}_\mu X$  (SL) [4] measurements, and for their combination.

### 3. Measurement of the charm mixing parameter $y_{CP} - y_{CP}^{K\pi}$ using two-body $D^0$ meson decays

The parameter  $y_{CP}$ , related to decay width as defined in Equation 2, is measured by analysing the time-dependent distribution of Cabibbo-suppressed  $D^0 \rightarrow f$  decays with  $f = K^-K^+, \pi^-\pi^+$  final states. The time-dependent ratios,  $R^f(t)$ , of their yields relative to the  $D^0 \rightarrow K^-\pi^+$  final state can be approximated with an exponential distribution as

$$R^f(t) = \frac{N(D^0 \rightarrow f, t)}{N(D^0 \rightarrow K^-\pi^+, t)} \propto e^{-(y_{CP}^f - y_{CP}^{K\pi})t/\tau_{D^0}} \frac{\varepsilon(f, t)}{\varepsilon(K^-\pi^+, t)}, \quad (5)$$

where  $y_{CP}^f$  is the  $y_{CP}$  parameter measured in the final state  $f$ , and  $\varepsilon(f, t)$  is the time-dependent efficiency for the considered final state. The  $y_{CP}^{K\pi}$  and  $\varepsilon(K^-\pi^+, t)$  are  $y_{CP}$  and efficiency measured in the  $K\pi$  final state. The measurement of  $y_{CP}$  is performed using the full Run 2 dataset collected by the LHCb experiment, corresponding to an integrated luminosity of  $6 \text{ fb}^{-1}$  [8].  $D^0$  candidates are obtained from  $D^{*+} \rightarrow D^0\pi^+$  decays. The analysis measures  $y_{CP}^f$  relative to the one in  $K^-\pi^+$  final state,  $y_{CP}^f - y_{CP}^{K\pi}$ . Figure 3 presents a fit to the ratios. This yields

$$\begin{aligned} y_{CP}^{\pi\pi} - y_{CP}^{K\pi} &= (6.57 \pm 0.53 \pm 0.16) \times 10^{-3}, \\ y_{CP}^{KK} - y_{CP}^{K\pi} &= (7.08 \pm 0.30 \pm 0.14) \times 10^{-3}, \end{aligned}$$

where the first uncertainties are statistical and the second systematic. The results show good compatibility between  $K^-K^+$  and  $\pi^-\pi^+$ . A combination of the two measurements is performed, yielding

$$y_{CP} - y_{CP}^{K\pi} = (6.96 \pm 0.26 \pm 0.13) \times 10^{-3}.$$

This result is compatible with the world average before this measurement [9] and more precise by a factor of four. The world average is dominated by this measurement and provides the most precise constraint on  $y_{CP}$ .

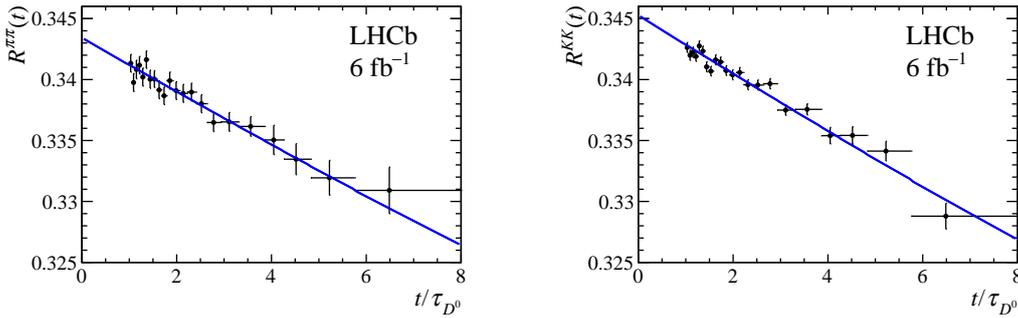


Figure 3: Fit projection of time-dependent ratios  $R^f(t)$  for (left)  $f = \pi^-\pi^+$  and (right)  $f = K^-K^+$ .

### 4. Search for time-dependent CP violation in $D^0 \rightarrow K^+K^-$ and $D^0 \rightarrow \pi^+\pi^-$ decays

A measurement of the time-dependent asymmetry between  $D^0$  and  $\bar{D}^0$  decays into a common final state  $f$ , where  $f = K^-K^+, \pi^-\pi^+$ , is presented. Since  $D^0$  mixing is very slow, the decay rate

asymmetry can be smaller than 1%. This allows their decay rate asymmetry to be approximated up to the first order in the mixing parameters as

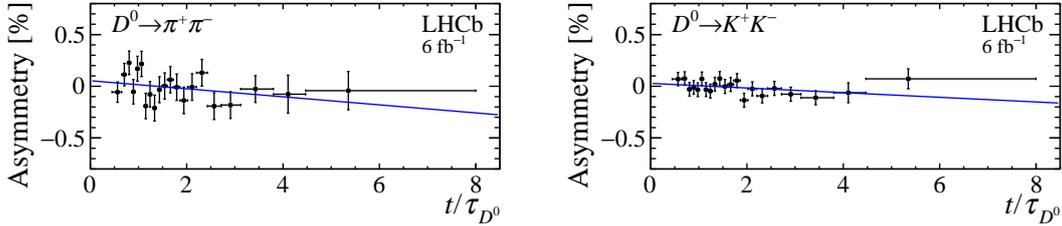
$$A_{CP}(f, t) \approx A_{CP}^{\text{decay}}(f) + \Delta Y_f \frac{t}{\tau_{D^0}}, \quad (6)$$

where  $\tau_{D^0}$  is the lifetime of the  $D^0$  meson and  $A_{CP}^{\text{decay}}(f)$  is the final state dependent  $CP$  asymmetry in the decay. A significant deviation of  $\Delta Y_f$  from zero would indicate the presence of  $CP$  violation. The SM estimation of  $\Delta Y_f$  is of the order of  $10^{-5}$ , but could be enhanced by non-perturbative strong interaction effects to  $10^{-4}$  [10, 11].

The most recent measurement from the LHCb collaboration is performed on the full LHCb Run 2 dataset, corresponding to an integrated luminosity of  $6 \text{ fb}^{-1}$  [12]. The  $D^0 \rightarrow h^+ h^-$  ( $h = K, \pi$ ) candidates are obtained from  $D^{*+} \rightarrow D^0 \pi^+$  decays. The analysis procedure is validated in the  $D^0 \rightarrow K^- \pi^+$  channel, where  $\Delta Y_{K^- \pi^+}$  is expected to be compatible with zero at the current level of sensitivity. The fits to the time-dependent asymmetries are shown in Figure 4, and yield  $\Delta Y_{K^+ K^-} = (-2.3 \pm 1.5 \pm 0.3) \times 10^{-4}$  and  $\Delta Y_{\pi^+ \pi^-} = (-4.0 \pm 2.8 \pm 0.4) \times 10^{-4}$ . These values are compatible within uncertainties. A weighted average, denoted as  $\Delta Y$ , between the results for the two final states, and including also previous LHCb measurements [13–15], yields

$$\Delta Y = (-1.0 \pm 1.1 \pm 0.3) \times 10^{-4}, \quad (7)$$

where the first uncertainty is statistical and the second systematic. This value is consistent with  $CP$  symmetry and constitutes the world most precise determination of this quantity.



**Figure 4:** Fits to the time-dependent asymmetry  $\Delta Y_{\pi^+ \pi^-}$  (left) and  $\Delta Y_{K^+ K^-}$  (right) using the full LHCb Run 2 dataset.

## 5. Conclusion and outlook

LHCb has produced the largest dataset of charm hadrons. This leads to new interesting results and often provides world-best measurements. However, the measurements are statistically limited. This is expected to be improved in Run 3, which is starting this year and will collect up to  $50 \text{ fb}^{-1}$  of integrated luminosity by 2030 with an upgraded detector software-only trigger [16, 17].

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## References

- [1] LHCb collaboration, *The LHCb detector at the LHC*, *JINST* **3** (2008) S08005.
- [2] LHCb collaboration, *Measurements of prompt charm production cross-sections in  $pp$  collisions at  $\sqrt{s} = 13$  TeV*, *JHEP* **03** (2016) 159 LHCb-PAPER-2015-041 CERN-PH-EP-2015-272, [1510.01707].
- [3] Particle Data Group, *Review of Particle Physics*, *PTEP* **2022** (2022) 083C01.
- [4] LHCb collaboration, *Model independent measurement of charm mixing parameters in  $B^- \rightarrow D^0 (\rightarrow K^{*0} \pi^+ \pi^-) \mu^- \bar{\nu}_\mu X$  decays*, 2208.06512.
- [5] A. Di Canto, J. Garra Ticó, T. Gershon, N. Jurik, M. Martinelli, T. Pilař et al., *Novel method for measuring charm-mixing parameters using multibody decays*, *Phys. Rev.* **D99** (2019) 012007.
- [6] CLEO collaboration, *Model-independent determination of the strong-phase difference between  $D^0$  and  $\bar{D}^0 \rightarrow K_{S,L}^0 h^+ h^-$  ( $h = \pi, K$ ) and its impact on the measurement of the CKM angle  $\gamma/\phi_3$* , *Phys. Rev.* **D82** (2010) 112006.
- [7] LHCb collaboration, *Observation of the mass difference between neutral charm-meson eigenstates*, *Phys. Rev. Lett.* **127** (2021) 111801.
- [8] LHCb collaboration, *Measurement of the charm mixing parameter  $y_{CP} - y_{CP}^{K\pi}$  using two-body  $D^0$  meson decays*, *Phys. Rev.* **D105** (2022) 092013.
- [9] Heavy Flavor Averaging Group, *Averages of  $b$ -hadron,  $c$ -hadron, and  $\tau$ -lepton properties as of 2018*, *Eur. Phys. J.* **C81** (2021) 226.
- [10] M. Bobrowski, A. Lenz, J. Riedl and J. Rohrwild, *How large can the SM contribution to CP violation in  $D^0-\bar{D}^0$  mixing be?*, *JHEP* **03** (2010) 009.
- [11] A.L. Kagan and L. Silvestrini, *Dispersive and absorptive CP violation in  $D^0-\bar{D}^0$  mixing*, *Phys. Rev. D* **103** (2021) 053008.
- [12] LHCb collaboration, *Search for time-dependent CP violation in  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow \pi^+ \pi^-$  decays*, *Phys. Rev.* **D104** (2021) 072010.
- [13] LHCb collaboration, *Measurement of indirect CP asymmetries in  $D^0 \rightarrow K^- K^+$  and  $D^0 \rightarrow \pi^- \pi^+$  decays using semileptonic  $B$  decays*, *JHEP* **04** (2015) 043.
- [14] LHCb collaboration, *Measurement of the CP violation parameter  $A_\Gamma$  in  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow \pi^+ \pi^-$  decays*, *Phys. Rev. Lett.* **118** (2017) 261803.
- [15] LHCb collaboration, *Updated measurement of decay-time-dependent CP asymmetries in  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow \pi^+ \pi^-$  decays*, *Phys. Rev.* **D101** (2020) 012005.
- [16] LHCb collaboration, *Framework TDR for the LHCb Upgrade: Technical Design Report*, 2012.
- [17] LHCb collaboration, *Computing Model of the Upgrade LHCb experiment*, 2018.