



X-ray bursting neutron star atmosphere models

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We present an extended set of model atmospheres and emergent spectra of X-ray bursting neutron stars in low-mass X-ray binaries. Compton scattering is taken into account. The models were computed in LTE approximation for six different chemical compositions: pure hydrogen, pure helium, and solar mix of hydrogen and helium and various heavy elements abundances: Z = 1, 0.3, 0.1, and 0.01 Z_{\odot} . For each chemical composition the models are computed for three values of gravity, $\log g = 14.0$, 14.3, and 14.6, and for 20 values of relative luminosity $l = L/L_{\rm Edd}$ in the range 0.001–0.98. The emergent spectra of all models are fitted by the diluted blackbody in the redshifted *RXTE*/PCA band 3–20 keV and the corresponding values of color correction factors f_c as function of l are presented. We also show how to use these dependencies to estimate the basic parameters of neutron stars.

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1. Method

Neutron stars (NSs) showing photospheric radius expansion X-ray bursts can be used to determine NS parameters, such as their radius R and mass M if the distance to the source is known (if, for example, a source is situated in the globular cluster, [1,2]). The relation between the observed normalization of the blackbody K as fitted to the spectra and the ratio of R to the distance during late burst phases is:

$$K^{1/2} = \frac{R_{\rm BB}(\rm km)}{D_{10}} = \frac{R(\rm km)}{f_c^2 D_{10}} (1+z), \tag{1.1}$$

where D_{10} is the distance in units 10 kpc, and $f_c = T_c/T_{eff}$ is the color correction factor. Therefore, during the cooling phases of X-ray bursts the dependence K(t) reflects the variations of the $f_c(t)$ only. We suggest to fit the observed $K^{-1/4}$ -F relation by the theoretical f_c -l relation, where F is the bolometric observed flux. From this fit we can obtain two independent values: $A = (R(\text{km}) \times (1+z)/D_{10})^{-1/2}$ and $F_{\text{Edd}} \propto L_{\text{Edd}}/((1+z)D_{10}^2)$. Combining these values we can obtain a relation between M and R, which is independent on the distance and corresponds physically to the maximum possible observed effective temperature on a NS surface (the Eddington temperature)

$$T_{\rm eff,\infty} = \left(\frac{GMc(1+z)}{\sigma R^2 k_{\rm e}}\right)^{1/4} \frac{1}{1+z} = 6.4 \times 10^9 \, F_{\rm Edd}^{1/4} \, A^{-1} \, {\rm K}. \tag{1.2}$$

Here $k_e = 0.2(1+X) \text{ cm}^2 \text{ g}^{-1}$ is the electron scattering opacity and X is the hydrogen mass fraction. In order to use this method we need an extended set of theoretical $f_c(l)$ curves. The existing models [3] do not provide enough accuracy. In this paper, we present a new set of models as well as the application of the method to one of the X-ray bursters.

2. Results of atmosphere modeling

We computed model atmospheres of X-ray bursting NSs subject to the constraints of hydrostatic and radiative equilibrium assuming planar geometry in LTE approximation with Compton scattering taken into account (see details of the code in [4,5]).

We calculated an extended set of NS model atmospheres with 6 chemical compositions (pure H, pure He, and solar H/He mixture with Z = 1, 0.3, 0.1 and $0.01 Z_{\odot}$ or [Fe/H] = 0, -0.5, -1 and -2), three surface gravities log g = 14.0, 14.3 and 14.6, and twenty luminosities L/L_{Edd} : 0.001, 0.003, 0.01, 0.03, 0.05, 0.07, 0.1, 0.15, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.75, 0.8, 0.85, 0.9, 0.95, and 0.98. Corresponding T_{eff} were calculated from L using log g and the chemical composition. The model emergent spectra were fitted by diluted blackbody spectra $F_E = wB_E(f_cT_{Edd})$ using four slightly different procedures in the redshifted *RXTE*/PCA energy band (3 - 20)(1 + z) keV. Here $w \approx f_c^{-4}$ is the dilution factor. The redshifts were calculated from log g assuming $M = 1.4M_{\odot}$. Results are presented in Figs. 1 and 2. See details in [6].



Figure 1: Left panels: Emergent (unredshifted) spectra (*top panel*) and temperature structures (*bottom panel*) of the model atmospheres with four relative luminosities (l = 0.5, 0.1, 0.01 and 0.001) and fixed surface gravity ($\log g = 14.0$) for solar hydrogen-helium mixture and various abundances of heavy elements: $Z/Z_{\odot} = 1$ (solid curves), 0.3 (dash-dotted curves), 0.1 (dotted curves), 0.01 (dashed curves). In the top panel the blackbody spectra with effective temperatures are also shown by short-dashed curves. **Right panels:** Dependence of the color correction factors on the relative luminosity for various NS atmosphere models. *Top panel:* Dependences for hydrogen and solar H/He mixture with $Z = 0.3 Z_{\odot}$ models and different surface gravities $\log g = 14.0$ (solid curves), 14.3 (dotted curves) and 14.6 (dashed curves). For clarity the dependences for hydrogen models are shifted by +0.2. *Bottom panel:* Dependences for low gravity ($\log g = 14.0$) models with various chemical compositions: pure hydrogen (upper curve), pure helium (lowest curve), and solar H/He mixture with $Z/Z_{\odot} = 1$ (dashed curve), 0.3 (dash-dotted curve), 0.1 (dotted curve), and 0.01 (solid curve).





Figure 2: Examples of NS atmosphere spectra computed for solar H/He mixture with $Z = 0.3 Z_{\odot}$ for high (*l*=0.95) and low (*l*=0.001) luminosity and low gravity (log *g* = 14.0). The computed spectra are shown by the solid curves, the fits with the blackbody with arbitrary dilution factor *w* are shown by the dashed curves, and the fits with $w = f_c^{-4}$ are shown by the dotted curves. The fits were performed in the 3–20 keV band.



Figure 3: Comparison of the X-ray burst data for 4U 1724–307 to the theoretical NS atmosphere models. The crosses represent the observed dependence of $K^{-1/4}$ vs. *F* for the long burst, while diamonds represent two short bursts. The solid curves correspond to the three best-fit theoretical models for various chemical compositions.



Figure 4: Constraints on mass and radius of the NS in 4U 1724–307 from the long burst spectra (fitted with the blackbody model and constant absorption). For a flat distribution of the distance between 5.3 and 7.7 kpc with Gaussian tails of 1σ =0.6 kpc, the constraints are shown by contours (90% confidence level). The countours are elongated along the fixed Eddington temperature $T_{\text{Edd},\infty}$, which is shown by the dashed curves. The countours plotted correspond to the three chemical compositions: green for pure hydrogen, blue for the solar ratio of H/He and subsolar metal abundance $Z = 0.3Z_{\odot}$ appropriate for Terzan 2 [8], and red for pure helium. The mass-radius relations for several equations of state of neutron and strange stars matter are shown by solid pink curves. The brown solid curves in the lower-right region correspond to the mass-shedding limit for various possible rotational frequencies.

3. Application to 4U 1724-307 and conclusion

We fitted the $K^{-1/4} - F$ relation as observed by *RXTE* [7] from the long burst of 4U 1724–307 on 1996 November 8 by the theoretical f_c –l relations (see Fig. 3). We obtained limits on *R* and *M* for various chemical compositions and the adopted distance between 5.3 and 7.7 kpc with Gaussian tails of 1 σ =0.6 kpc [8] (see Fig. 4 and [9] for more details). For H-rich compositions, the obtained *M* and *R* correspond to a stiff equation of state in the inner NS core. The atmospheres consisting of pure He are not acceptable.

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