

# Top anomalous decays in R-parity violating SUSY

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**ABSTRACT:** The flavor-changing top-quark decay  $t \rightarrow ch$ , where  $h$  is the lightest CP-even Higgs boson in the minimal supersymmetric standard model, is examined in the R-parity-violating supersymmetric model. Within the existing bounds on the relevant R-parity-violating couplings, the branching ratio for  $t \rightarrow ch$  can be as large as about  $10^{-5}$  in some part of the parameter space, reaching a level accessible at the LHC and at  $e^+e^-$  Linear Colliders with high luminosities.

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The study of heavy-particle decays via flavor-changing neutral-currents (FCNC) has been playing an important role in testing the standard model (SM) and probing new physics beyond the SM. As the heaviest elementary particle in the SM with a mass at the electroweak scale, the top quark is more likely to be sensitive to new physics. Kinematically it is accessible to many FCNC decay modes, such as  $t \rightarrow cV$  ( $V = \gamma, Z, g$ ) and  $t \rightarrow ch$ , where  $h$  is a Higgs boson. In the SM these FCNC decay modes are highly suppressed by the GIM mechanism, with typical branching ratios of  $10^{-14} - 10^{-10}$  [1, 2], which are too small to be detectable at collider experiments. On the other hand, observation of any of such FCNC top-quark decays would be robust evidence for new physics [3, 4, 5, 6].

Top quarks will be copiously produced at the next generation of colliders. At Tevatron II with an integrated luminosity of  $10 \text{ fb}^{-1}$ , there will be about  $8 \times 10^4$  top quarks produced,

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while there will be about 100 times more at the LHC with the same luminosity. At the LHC with a luminosity of  $100 \text{ fb}^{-1}$  there will be more than  $10^8$  tops per year, including both  $t\bar{t}$  and single top production, for  $m_h = 120 \text{ GeV}$  [7]. At a proposed  $e^+e^-$  Linear Collider with  $\sqrt{s} = 500 \text{ GeV}$  and luminosity of  $300 \text{ fb}^{-1}$ , such as TESLA, one expect  $1.6 \times 10^5$  tops [7, 8]. With such large data samples, good sensitivities may be reached for the rare decay channels  $t \rightarrow cV$  [3], and for studying other related processes at hadron colliders [4]. A more recent study showed that the channel  $t \rightarrow ch$  could also be detectable [5], reaching a sensitivity of  $Br(t \rightarrow ch) \sim 10^{-5}$  at the LHC and a few percent at the Tevatron. While these high detection sensitivities are still far above the SM expectation for the rare decay channels [1, 2], in many scenarios beyond the SM the branching ratios of these FCNC top-quark decays could be significantly enhanced [1, 6, 9, 10, 11, 12, 13].

In the minimal supersymmetric (SUSY) standard model (MSSM) with R-parity conservation, it was shown [10] that the possibility for observing the decay channel  $t \rightarrow ch$  could be greatly enhanced (here  $h$  is the lightest CP-even Higgs boson). Kinematically this decay mode is always allowed because of the strict theoretical upper bound on the Higgs boson mass [14], and the decay receives dominant contributions from the SUSY QCD (SQCD) loops of flavor-changing interactions [10]. If the gluino and squarks involved in the contributing SQCD loops are both light of order 100 GeV, the branching ratio could be enhanced to a level of  $10^{-5}$ . The branching ratio falls off quickly for heavier sparticles in the loops.

In this talk which is basically a short version of [15], we examine the R-parity-violating contributions to  $t \rightarrow ch$ . It is well-known that R-parity conservation in SUSY theory, which implies the separate conservation of baryon number and lepton number, is put in by hand. R-parity violation ( $\mathcal{R}$ ) can be made perfectly consistent with other fundamental principles such as gauge invariance, supersymmetry and renormalizability [16]. If  $\mathcal{R}$  is included in the MSSM,  $t \rightarrow ch$  will receive new contributions from the loops of  $\mathcal{R}$  interactions. These can be significant, since the relevant  $\mathcal{R}$  couplings inducing  $t \rightarrow ch$  involve the third-generation fermions and are subject to rather weak bounds from existing experiments. We find that the branching ratio for  $t \rightarrow ch$  from  $\mathcal{R}$  contributions can be indeed as high as about  $10^{-5}$  in some part of parameter space, reaching a level accessible at future high luminosity colliders.

Assuming that there are only trilinear couplings, one obtains the  $\mathcal{R}$  Lagrangian

$$\mathcal{L}_{\lambda''} = -\frac{1}{2}\lambda''_{ijk} \left[ \tilde{d}_R^k (\bar{u}_R^i)^c d_R^j + \tilde{d}_R^j (\bar{d}_R^k)^c u_R^i + \tilde{u}_R^i (\bar{d}_R^j)^c d_R^k \right] + h.c. \quad (1)$$

Constraints on the couplings have been obtained from various processes [17, 18, 19, 20, 21, 22, 23, 24] and their phenomenology at hadron and lepton colliders has been intensively investigated [24, 25]. For brevity, only the terms with Baryon-number violation ( $\mathcal{B}$ ) are displayed, and the similar Lepton-number violating ( $\mathcal{L}$ ) terms, *i.e.* those with  $\lambda'$ 's, are left out. Also, the limits on the  $\mathcal{L}$  couplings are stricter than for those with  $\mathcal{B}$ . With  $\mathcal{B}$  couplings, the decay  $t \rightarrow ch$  can proceed through four simple 1-loop diagrams (see Fig. 1 in [15]).

The induced effective  $tch$  vertex is given by  $V = ie \frac{\lambda''_{2jk} \lambda''_{3jk}}{16\pi^2} 2FP_L$ , where  $P_L = \frac{1}{2}(1 - \gamma_5)$ . For simplicity and space limitation, we have assumed that all fermion masses can

be neglected with respect to  $m_t$  [15]. Then, only a single diagram survives, *i.e.* the one with  $h$  emitted from  $\tilde{d}^k$  line, corresponding to the upper right one in Fig. (1) in [15], and  $F = Y m_t (C_{11} - C_{12})(-p_t, k, m_{d_j}, m_{\tilde{d}^k}, m_{\tilde{d}^k})$ , where  $k$  is the Higgs momentum. The functions  $C_{ij}$  are the conventional 3-point Feynman integrals [26], with arguments as indicated in the bracket following them. The only surviving constant for  $m_q \ll m_t$  is  $Y = -\frac{1}{3} m_Z \tan \theta_W \sin(\alpha + \beta)$ , where  $\alpha$  is the neutral Higgs boson mixing angle, and  $\tan \beta = v_2/v_1$  [27].

We now discuss the numerical results for  $Br(t \rightarrow ch)$ , as presented in Figs. 3–5 in [15]. For the SM parameters involved, we take  $m_t = 175$  GeV,  $m_Z = 91.187$  GeV,  $m_W = 80.3$  GeV,  $\alpha = 1/128$ ,  $\sin^2 \theta_W = 0.232$ . The SUSY parameters involved are the following:

- (1) For the  $\mathcal{B}$  couplings  $\lambda''_{2jk}$  and  $\lambda''_{3jk}$ , we take their upper limits [22, 28], which are of  $\mathcal{O}(1)$ . We note that the current bounds for the  $\mathcal{B}$  couplings are generally quite weak (see however [19]).
- (2) We assume a common mass for all squarks.
- (3) At tree level the Higgs sector of the MSSM is determined by two free parameters, *e.g.*,  $m_A$  and  $\tan \beta$ . When radiative corrections are included, several other parameters enter through the loops [14]. Then a single parameter  $\epsilon$  [29], determines  $\alpha$  and  $m_{h,H}$ . We constrain the parameter space of the Higgs sector as given in [30].

We presented the maximum values of the branching ratio in Fig. (5) in [15], for  $\tan \beta = 10$  as a function of  $m_A$ , for two squark masses. One sees that there is only little dependence on  $m_A$ .  $Br(t \rightarrow ch)$  can reach  $10^{-5}$  for  $m_{\tilde{q}} = 100$  GeV, dropping by more than an order of magnitude when  $m_{\tilde{q}} = 200$  GeV.

In addition, the dependence on  $\tan \beta$ , away from its excluded values, is mild [15]. We have also demonstrated the decoupling property of the MSSM, *i.e.*, for  $m_{\tilde{q}} \gtrsim 500$  GeV, the branching ratio goes down like  $1/m_{\tilde{q}}^4$ .

In summary, we found that the FCNC decay  $t \rightarrow ch$  can be significantly enhanced relative to that of the SM, in SUSY theories with R-parity violation. The branching ratio depends quadratically on the products of  $\mathcal{B}$  couplings, and scales with the heavy mass of the squarks in the loops as  $m_{\tilde{q}}^{-4}$ , and it can be at least as large as that in the MSSM. In the optimistic scenario that the involved couplings take their current upper bounds and  $m_{\tilde{q}} \approx 100$  GeV, the branching ratio can be as large as  $10^{-5}$ , which is potentially accessible at the future LHC and Linear Colliders.

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