A few topics concerning the early chemical evolution of the Milky Way are critically discussed. In particular, it is argued that: 1) Observed abundance patterns of extremely metal-poor stars (of Pop. II) do not constrain the mass range of the first generation (Pop. III) stars; the latter may well be normal massive stars (10-50 $M_\odot$) or very massive ones (140-1000 $M_\odot$) or a combination of the two classes. 2) The discrepancy between primordial Li abundance (after WMAP) and the observed “Spite plateau” cannot be due to astration by a generation of massive Pop. III stars, as recently suggested, unless such stars eject negligible amounts of metals. 3) The observed halo metallicity distribution may well be understood in the framework of hierarchical galaxy formation, as shown here with a simple semi-analytical model. 4) Formation of the Milky Way’s halo from a myriad of smaller sub-haloes may have important implications for our understanding of the abundance patterns of r-elements, the origin of which remains still unclear.

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1. Introduction

Galactic chemical evolution studies provide a useful framework for the interpretation of the everincreasing wealth of observational data concerning abundances in stars of the Milky Way. In particular, studies of abundance ratios in the oldest stars of the Milky Way (Pop. II stars, with metallicities down to $[\text{Fe/H}]=\log(\text{Fe/H})_{\odot}=-4$) allow one to put interesting constraints on the nature of the first stars that enriched the interstellar medium with metals. Ultimately, one may hope to find a distinctive imprint of the very first generation of massive stars (Pop. III), those that were born out of primordial material containing H and He only (as well as trace amounts of $^7\text{Li}$, resulting from the Big Bang). This pattern should then be visible on the surfaces of the next generation stars that were born from the enriched gas and are still around today, i.e. the oldest and most metal poor Pop. II stars.

2. Halo star composition: any signatures of massive Pop. III stars?

Star formation theory and numerical simulations suggest that the first stars were very massive (e.g. Nakamura and Umemura 2002, Glover 2004 and references therein). In view of the many important implications of those ideas (e.g. for re-ionization of the Universe) it is interesting to investigate whether the observed abundance patterns of old stars reveal any trace of a Pop III stellar generation with peculiar properties. In fact, it has been suggested that a stellar initial mass function (IMF) rich in massive stars (top-heavy IMF) can help explain (1) the abundance ratios in the Fe-peak region, and (2) the discrepancy between the expected primordial Li value (after the determination of the cosmic baryonic density by WMAP) and the one observed in the “Spite plateau”. We argue below that the answers are: (1) may be, and (2) no.

2.1 Abundance patterns in EMP stars: no clear signature of the culprits!

The recent data on Extremely Metal-Poor (EMP) stars confirm some previously found tendencies in the abundance patterns of heavy elements, and in particular:

- The constancy, down to the lowest observed metallicities, of the $\alpha$/Fe ratio (where $\alpha$ stands for alpha elements like O, Mg, Si, Ca); the high value of that ratio ($\sim3$ times solar) is attributed to SNII, while its solar value is attributed to the later contribution of Fe by SNIa.

- The decreasing trend of Mn/Fe and Cu/Fe with decreasing metallicity, in qualitative agreement with theoretical expectations (see Fig. 1).

However, more interesting are the cases where observations are at odds with theoretical expectations. These are the cases of Cr, Co and Zn, as seen in Fig. 1, where the results of a full-scale chemical evolution model of the Milky Way (originally presented in Goswami and Prantzos 2000) are displayed. The adopted stellar yields are from non-rotating Core Collapse supernovae (CCSN) in the “normal” mass range of 12 to $\sim40 M_\odot$, exploding with “canonical” energies of $E=10^{51}\text{erg}$ and with progenitor metallicities from $Z=0$ to $Z=Z_\odot$.

The reasons for those discrepancies probably lie in our poor understanding of the explosion mechanism and of the nature of the early CCSN. A large amount of work was devoted in recent years to understanding the peculiar abundance patterns among Fe-peak elements observed in EMP stars (e.g. Heger and Woosley 2002, Maeda and Nomoto 2003, Chieffi and Limongi 2004; for
Figure 1: Abundance ratios [X/Fe] as a function of metallicity [Fe/H] in stars of the Milky Way; small data points are from various sources, while the large data points at low metallicity are from the VLT survey of Cayrel et al. (2004). Results of standard chemical evolution models, performed with two sets of metallicity dependent massive star yields (Woosley and Weaver 1995, solid curves; Chieffi and Limongi 2004, dashed curves) are also displayed. Yields for SNIa are adopted from Iwamoto et al. (1999) and for intermediate mass stars from van den Hoek and Gronewegen (1997). While the behaviour of alpha elements and Mn is correctly reproduced (at least qualitatively), there are large discrepancies in the cases of Cr, Co and Zn.

reviews see Nomoto et al. 2005, Cayrel 2006 and references therein). In those works it was explored whether some specific property of the Pop. III stars (characteristic mass, rotation, explosion energy etc.) was quite different from the corresponding one of their more metal rich counterparts and produced a different nucleosynthetic pattern in the ejecta. Two main classes of solutions (not mutually exclusive) appear to arise from those works:

1) Normal massive stars (10-50 M$_\odot$), exploding as core collapse SN (CCSN) and leaving behind a neutron star or a black hole. It was shown (essentially by the Tokyo group, see Nomoto et al. 2005 for a recent review) that higher energies than the canonical one of $E = 10^{51}$ ergs combined with asphericity of the explosion can help to improve the situation concerning the Zn/Fe and Co/Fe ratios observed in EMPs. Material ejected along the rotation axis (in the form of jets) has high entropy and is found to be enriched in products of $\alpha$-rich freeze-out (Zn and Co), as well as Sc (which is generically underproduced in spherical models); this kind of models seems at present the most promising, but this is not quite unexpected (since they have at least one more
Figure 2: Nucleosynthesis yields of a 25 $M_\odot$ star, compared to observations of extremely metal-poor stars (vertical error bars, from Cayrel et al. 2004). *Left:* The star explodes with a canonical energy of $1.5 \times 10^{51}$ erg; *Right:* The star explodes as a hypernova, with an energy of $10 \times 10^{51}$ erg (both figures from Nomoto et al. 2005). Abundance ratios in the Fe-peak are much better reproduced in the second case.

degree of freedom w.r.t. spherical models). Such properties (high energies, asphericity) are indeed observed in the local Universe for *hypernovae*, a class of energetic CCSN. However, hypernovae are not so frequent today as to affect the later chemical evolution of galaxies (normal CCSN plus SNIa can easily account for e.g. the solar abundance pattern). If hypernovae indeed affected the early chemical evolution, they must have been much more abundant in Pop. III than today. No satisfactory explanation for such a large hypernova fraction in the early Universe exists up to now. It seems hard to conceive that the typical energy of the explosion was substantially higher in Pop. III stars (all other parameters, except metallicity, being kept the same). On the other hand, rotation effects may indeed be stronger in low metallicity environments, because of smaller angular momentum losses due to lower mass loss rates (e.g. Meynet et al. 2006). In any case, none of the models explored so far appears to account for the early trend of Cr/Fe, which remains a mystery at present.

2) Very massive stars (VMS), above 100 $M_\odot$. Such stars are thought to: collapse to black holes, if $M<140$ $M_\odot$; explode during oxygen burning as pair-implosion SN (PISN), if $140<M/M_\odot<300$; and again collapse without ejecting metals if $M>300$ $M_\odot$ (see Heger and Woosley 2002 and references therein). In the case of PISN, it was shown that they do not produce enough Zn to account for the observed high Zn/Fe ratio in EMP stars (Heger and Woosley 2002, Umeda and Nomoto 2005) and they were thus excluded as major contributors to the early chemical evolution of the MW. This shortcoming cast doubt as to the existence of a Pop. III generation composed exclusively of VMS. However, in a recent work Ohkubo et al. (2006) explore the conditions under which rotating stars of $M=500$ and 1000 $M_\odot$ do explode and eject metals (although a massive black hole is ultimately produced in both cases). They find explosions for a certain region of their parameter space and substantial production of Zn as a generic feature (see Fig. 3b). Even if each class of PISN or 500-1000 $M_\odot$ stars cannot reproduce the observed EMP abundance pattern alone, it is obvious that considering the full 140-1000 $M_\odot$ range (folded with an appropriate IMF) will account for such a pattern. Thus, VMS cannot be excluded at present as candidates for Pop. III stars, at least not on “chemical” grounds.
2.2 WMAP Li was (most probably) NOT astrated in massive Pop. III stars

The recent WMAP results from the 3-year data analysis of the cosmic microwave background, combined with other cosmological measurements, allow one to determine with great precision the parameters characterising our observable Universe (see Lahav and Liddle 2006). In particular, the baryonic density is \( \Omega_B = 4.5 \times 10^{-2} \). For that density, calculations of Standard Big Bang Nucleosynthesis (SBBN) predict an amount of primordial deuterium that is fully compatible with observations of its abundance in remote gas clouds (at such early times that significant astration had no time to occur); this undoubtedly constitutes a triumph for SBBN (e.g. A. Coc, this Conference). Unfortunately, the situation with Li \(^7\)Li is far less satisfactory.

Indeed, the Li abundance of the "Spite plateau" (Li/H \( \sim 1.5 \times 10^{-10} \)=const. for halo stars, down to the lowest metallicities) is a factor of 2-3 lower than the WMAP+SBBN value. Barrering systematic errors, the conclusion is that primordial Li has been depleted, either before getting into the stars where it is observed today, or during the lifetime of those stars. Two "depletion agents" have been proposed in the former case: decaying supersymmetric particles (Jedamzik 2006) and astration in a first generation of exclusively massive (mass range \( m_\ast = 10-40 \, M_\odot \)) Pop. III stars (Piau et al. 2006). The latter idea, however, suffers from a serious flaw, since in that case the metallicity of the ISM (out of which the next stellar generation would form with depleted Li) would necessarily rise to levels much higher than those observed in EMP stars. This can be seen as follows:

Assuming that the current halo stellar mass (\( M_H = 2 \times 10^9 \, M_\odot \)) was initially in the form of gas, a fraction \( f \) of which was astrated through massive stars, the resulting Li mass fraction is \( X_{Li} = (1 - f)X_{Li, P} \) where \( X_{Li, P} \) is the primordial Li abundance (assuming a return fraction \( R \sim 1 \) for the astrating and metal producing stars). Similarly, the resulting oxygen abundance would be \( X_O = m_O/M_H \), where the mass of oxygen \( m_O = N_{SN} \, Y_O \) is produced by a number of supernovae \( N_{SN} = f \, M_H / m_\ast \), each one with a typical oxygen yield of \( Y_O \) (in \( M_\odot \), to be discussed below). Putting all this together, one has:

\[
\frac{X_{Li}}{X_{Li, P}} = 1 - 0.28 \frac{(X_O/0.007)(m_\ast/40M_\odot)}{Y_O}
\]
Milky Way evolution

Nikos Prantzos

**Figure 4:** *Left:* Observations of Li in halo and disk stars of the Milky Way. The primordial Li value, obtained from the baryonic density of WMAP and calculations of SBBN, is indicated by a horizontal dashed line. The observed Li plateau at low metallicities depends sensitively on assumed stellar temperature, and differs from the WMAP value by factors 2-3. *Right:* Illustration of the problem encountered by the idea that the discrepancy is due to astration of Li by a Pop. III composed of exclusively massive stars, in the 10-100 M_☉ range (Piau et al. 2006): such stars necessarily eject metals, either through their winds (e.g. Nitrogen, in case of rotating stars) or through the final supernova explosion (e.g. Oxygen). Mixing the ejecta with various proportions of primordial material would result in Li depletion (by a factor of ~2 in case of a 50-50 mixture), but the resulting metallicity would be much higher than the one of EMP stars unless abnormally low oxygen yields were assumed (i.e. the curve in Fig. 4b parametrized with a yield \( Y_O = 0.001 \) M_☉, see text).

This relation appears in Fig. 4 (right panel) as a function of \( \log(X_O / X_O, \odot) \), with solar \( X_O, \odot = 0.007 \). The four curves correspond to different assumptions about the typical oxygen yield of a massive star of Z=0, ranging from 0.001 to 1 M_☉. Among the various calculations of massive star nucleosynthesis made so far, only one set of models in the 30-40 M_☉ range (set A of Woosley and Weaver 1995, WW95) produces extremely low oxygen (and heavy element) yields for stars of 35 and 40 M_☉. This is due to the assumption of constant kinetic energy at infinity (=1.2 \( 10^{51} \) erg) adopted for all models of set A in WW95; other assumptions (sets B and C) lead to much larger oxygen yields and to abundance ratios in rough agreement with observations in EMP stars, at least for alpha-elements (e.g. Goswami and Prantzos 2000), while set A provides a rather poor match. Other calculations at Z=0, either for spherically symmetric stars (Chieffi and Limongi 2004, assuming a fixed mass of \(^{56}\)Ni ejected) or for bipolar explosions (Maeda and Nomoto 2003) lead to \( Y_O > 1 \) M_☉ always; note that the latter models provide a better (albeit not perfect) match to observed Fe-peak element abundance ratios than “standard” (spherically symmetric) models, as discussed in Sec. 2.1.

Another way to eject astrated material by Z~0 stars is through stellar winds, which require rapidly rotating stars, since radiative pressure is inefficient at such low metallicities; but rotating massive stars produce large amounts of nitrogen (which may in fact help explaining the observed primary-like nitrogen in EMP stars, e.g. Meynet et al. 2006), thus the problem of metal overproduction is not avoided in that case either.

Astration in massive Pop. III stars cannot solve the Li discrepancy between the Spite plateau and WMAP+SBBN \(^1\): even a small Li depletion should be accompanied by excessive metal en-

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\(^1\)At least, not the 10-40 M_☉ stars suggested in Piau et al. 2006 (provided that current nucleosynthesis models for such
hancement. It appears now that depletion during the stellar evolution, within the stellar envelope, is the answer (see Korn et al. 2006 and references therein).

3. The early MW and hierarchical galaxy formation

In the previous sections, the early chemical evolution of the MW was discussed independently of the cosmological framework in which it took place. According to the currently dominant paradigm of hierarchical structure formation, the early phases of a galaxy’s evolution are the most complex ones, as they involve multiple mergers of smaller sub-units. In the case of the Milky Way, interesting "chemical signatures" of that period should still be left around us today, in the form of the metallicity distribution (MD) of long-lived stars and in dispersion in abundance ratios. We discuss those two topics in the following.

3.1 The halo metallicity distribution: outflow vs. subhalo merging

The MD of Galactic halo field stars (HMD) is rather well known in the metallicity range $-2.2 < [\text{Fe/H}] < -0.8$, while at lower metallicities its precise form has still to be established by ongoing surveys (Fig. 5a). Its overall shape is well fitted by a simple model of GCE as $dn/d\log Z \propto Z/y e^{-Z/y}$, where $y$ is the yield of a stellar generation; this function has a maximum for $Z = y$. The HMD peaks at a metallicity $[\text{Fe/H}] = -1.6$ (or $[\text{O/H}] = -1.1$, assuming $[\text{O/Fe}] = 0.5$ for halo stars), pointing to a low yield $y = 1/13$ of the corresponding value for the solar neighborhood. Such a low halo yield is "classicaly" (i.e. in the monolithic collapse scenario) interpreted as due to outflow stars are correct); 100 $M_\odot$ stars collapsing to black holes would be better candidates (provided they eject a substantial fraction of their astrated mass).
Figure 6: Left top and middle panels: Metallicity distribution (in lin and log scales, respectively) of the MW halo, assumed to be composed of a population of smaller units (sub-haloes). The individual MDs of the sub-haloes, from $10^6$ M$_\odot$ to $2 \times 10^8$ M$_\odot$, are indicated in both panels (but clearly seen only in the middle), as well as the sum over all haloes (upper curves in both panels, compared to observations). Small sub-haloes contribute the largest fraction of the lowest metallicity stars (bottom left). Properties of the sub-haloes as a function of their mass.

during halo formation (Hartwick 1976), at the large rate of 8 times the SFR (Prantzos 2003). How can it be understood in the framework of hierarchical merging?

It should be noted that the typical halo metallicity ([Fe/H]=-1.6) is substantially lower, by more than 0.5 dex, than the corresponding metallicities of nearby galaxies of similar mass ($M_{\text{Halo}}$ $\sim$ 2 $10^9$ M$_\odot$), as can be seen in Fig. 5b. That figure also displays the well known galactic relationship between stellar mass and stellar metallicity; most probably, that relationship results from mass loss, which is more important in lower mass galaxies, since the hot supernova ejecta escape more easily their swallow potential well (e.g. Dekel and Woo 2003).

Assuming that the MW halo has been assembled from sub-units similar to the low mass galaxies of Fig. 5b, one may interpret the HMD as the sum of the MD of such low mass galaxies; it is assumed that each one of those galaxies evolved with an appropriate outflow rate and corresponding effective yield $y(M) = (1 - R)/(1 + k - R)$, where $k(M)$ is the outflow rate in units of the SFR and $R$ is the return mass fraction, depending on the adopted stellar IMF (see Prantzos 2003). In that case, one has: $\text{HMD}(Z) = 1/M_{\text{Halo}} \int Z/y(M) e^{-Z/y(M)} \Phi(M) MdM$, where $\Phi(M)$ is the mass function of the sub-units and $y(M)$ is the effective yield of each sub-unit (obtained directly from Fig. 5b as $y(M) = Z(M)$, i.e. smaller galaxies suffered heavier mass loss).

The results of such a simple toy-model for the HMD appear in Fig. 6a. The HMD is extremely well reproduced, down to the lowest metallicities, assuming $\Phi(M) \propto M^{-2}$, such as those resulting
from recent high resolution numerical simulations for Milky Way sized dark haloes (Diemand et al. 2006, Salvadori et al. 2006). Low mass satellites (down to $10^6 \, M_\odot$) contribute most of the low metallicity stars of the MW halo, whereas the high metallicity stars originate in a couple of massive satellites with $M \sim 10^8 \, M_\odot$ (Fig. 6a, bottom).

Some properties of the sub-haloes as a function of their mass appear also in Fig. 6 (right panels). The outflow rate, in units of the corresponding SFR, is $k(M) = (1 - R)(y_{\text{True}}/y(M) - 1)$, where $y_{\text{True}}$ is the yield in the solar neighborhood ($y_{\text{True}} = 0.7 Z_\odot$, from the local G-dwarf MD). If the MW halo were formed in a a potential well as deep as those of comparable mass galaxies, then the large outflow rate required to justify the HMD ($k=8$) is puzzling; on the contrary, the HMD is readily understood if the MW halo is formed from a large number of smaller satellites, each one of them having suffered heavy mass loss according to the simple outflow model.

A more physical, but much less “transparent”, approach consists in deriving the full merger tree of the MW halo and (by using appropriate recipes for SFR and feedback for the sub-haloes) following the chemical evolution through merging/accretion with Monte-Carlo simulations. Recent studies (Tumlinson 2006, Salvadori et al. 2006) find good agreement with the observed HMD, but it is hard to find (in view of the many model parameters) what is (are) the key factor(s) determining the final outcome. In any case, mass loss (occurring mostly through tidal stripping than through supernova feedback, e.g. Bekki and Chiba 2001) is crucial in shaping the HMD.

### 3.2 Implications: abundance dispersion and origin of the r-elements

The early chaotic history of the MW (according to the hierarchical merging scenario) bears naturally to the issue of dispersion in the abundance ratios of EMP stars. Simple-minded arguments suggest that dispersion should increase at low metallicities, under the explicit assumption that low metallicities correspond to such early times that complete mixing of SN ejecta with the interstellar medium is impossible (Argast et al. 2002, Karlsson and Gustafsson 2001). In order to actually see such a dispersion, variations in abundance ratios among SN of different masses should be sufficiently large (say, larger than typical observational statistical uncertainties of 0.1 dex).

Several recent studies of EMP stars reveal very small scatter in the abundance ratios of all elements in the C to Fe-peak mass range (Carretta et al. 2002, Cayrel et al. 2004, Barklem et al. 2006). This could mean that i) mixing timescales are (much) shorter than typical chemical evolution timescales at metallicities down to $[\text{Fe/H}] \sim -3.5$ or ii) variations in abundance ratios of SN of different masses and energies (for the C to Fe-peak mass range) are sufficiently small, or a combination of (i) and (ii). Despite our current ignorance of the timescales of mixing and early chemical evolution, case (i), i.e. extremely efficient and rapid mixing of SN ejecta, cannot be the whole truth, since large variations in abundance ratios are observed in the case of r-elements. A solution to that may be that r-elements originate mostly in a restricted sub-class of CCSN (say 8-10 $M_\odot$), which produce a very large r/Fe ratio (e.g. Ishimaru et al. 2003, also these proceedings).

The hierarchical merging scenario may complicate even more the already unclear situation of the r-element production. At present, the production site of r-nuclei is unknown, with (some class of) CCSN favoured relative to neutron star mergers (NSM). The reasons for the “disfavor” of NSM are explored and clearly presented in Argast et al. (2004): the combination of expected low event rates, long coalescence timescales and high individual yields leads to a relatively late injection of the NSM r-nuclei in the Galaxy (around $[\text{Fe/H}] \sim -2.5$, while Eu is observed already at $[\text{Fe/H}] \sim -3$.
Figure 7: Illustration of how differently evolving sub-haloes may create a dispersion in the abundance ratio [X/Fe], provided element X is produced in two different nucleosynthesis sites, with different evolutionary timescales; this might explain observed dispersion in r/Fe. **Left:** Halo 1 evolves rapidly, so that only the first (short-lived) site of element M operates, and it reaches a high metallicity (say [Fe/H]=-1.2); halo 2 (less massive) evolves on longer timescales, allowing for the second source of element M to increase the M/Fe ratio, but it reaches a smaller metallicity (say [Fe/H]=-2.6). **Right:** When those sub-haloes merge, dispersion as a function of metallicity is naturally obtained (starting at low [Fe/H]), even if the ISM in each one of them is completely homogenized.

and the r-component of Ba at even lower metallicities), and produces a *large scatter of r/Fe ratio relatively late* (at [Fe/H]~2, when observations show that such large scatter occurs only at lower metallicities, around [Fe/H]~3, Fig. 4 in Argast et al. 2004).

The conclusions of the Argast et al. (2004) study depend strongly on the adopted assumptions about the NSM properties, as the authors recognize. They also depend on their model of the early Galaxy evolution, in which star formation proceeds stochastically in various places, but *at the same average rate everywhere*, i.e. there is in reality one single system evolving. The situation is obviously different in a (presumably more realistic) system composed of many different sub-units, each one evolving at its own rate and affected in a different way by mass loss.

An illustration of such a situation is provided in Fig. 7: Halo 1 (H1, massive) evolves rapidly (100 Myr) and reaches a high metallicity ([Fe/H]~1), while halo 2 (H2, low mass) evolves slowly (~1 Gyr) and reaches a lower final metallicity ([Fe/H]~2.6). Because of short timescales, NSM do not enrich H1 with r-elements, so its r/Fe ratio remains [r/Fe]=const=0. In H2, NSM start increasing the r/Fe ratio only after about 100 Myr (assumed as typical coalescence timescale of NSM), up to [r/Fe]~1 (before 100 Myr, CCSN produce [r/Fe]=0). Note that efficient and rapid mixing of CCSN and NSM products in the gas of both haloes is always assumed (to ensure no dispersion in abundance ratios *within each halo*). When the two haloes merge together, two distinct histories appear in the [r/Fe] vs [Fe/H] plane (Fig. 7 right). By considering a large number of intermediate mass haloes, the plane can be naturally filled at [Fe/H]>~3. A large dispersion can then be naturally recovered and NSM can be important sources of r-nuclei (along with CCSN), while at the same time dispersion for other elements (exclusively produced in CCSN) remains small, in agreement with observations.

In summary, because of the chaotic early history of the MW (formed by a myriad of smaller
sub-haloes with widely differing SF histories), it cannot be excluded at present that both CCSN and NSM have contributed to its enrichment with r-elements.

References