Faraday tomography for magnetic fields in our Galaxy and nearby Universe

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To understand the magnetic fields in the universe, we have to measure them and get to know their properties. The magnetic fields of galactic scales are crucial bridge to connect the knowledge on the stellar scale and the cosmological scale. The most effective method to reveal the large-scale extremely weak magnetic fields on galactic or a larger scale is through observing the Faraday rotation of the polarized emission of the background radio sources. Note that the Faraday rotation is integration of the magnetic field $B$ together with the thermal electron density $n_e$. In our own Milky Way Galaxy, pulsars are the best probes, because we can observe not only the rotation measure (RM), but also the pulse delay at different frequencies, i.e. the dispersion measure (DM). From these two observables, the magnetic field in the interstellar medium can be directly measured. In the Galactic disk, we obtained the large-scale magnetic field structure from pulsar RMs and DMs, and also we determined the spatial magnetic field energy spectrum which theoretic studies need. The Galacto-radial dependence of the field strength has also been derived from pulsar data. From the sky distribution of RMs of extragalactic radio sources, we identified the magnetic field structure in the Galactic halo. To explore the magnetic fields of cosmological scale, the RMs in the Galactic pole regions can be used, because the foreground RM contribution from our Galaxy is minimized and can be eliminated easily. There is evidence that the RMs become more deviate towards higher redshift, i.e. there are intergalactic magnetic fields but it is hard to disentangle it from the combination with unknown electron distribution in the intergalactic space.

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1. Introduction

Our own Galaxy, the Milky way, is so bright in sky in optical and radio bands, which we all know about it. However, the polarized radio sky [20, 22] and the Faraday’s sky or the Rotation Measure (RM) Sky are not so familiar for many astronomers except for some radio astronomers. Our Galaxy is dominant in the sky, and the RM sky has a strikingly antisymmetric distribution [9]. The foreground contribution from our Galaxy, or “pollution”, must be eliminated when we like measure any polarization or Faraday effect on the cosmological scale. However, the foreground contribution has not been measured exactly, especially the RM sky.

Faraday rotation of polarized emission from a radio source can be used to reveal the intervening magnetic fields between the source (\(\odot\)) and us (\(\oplus\)). The rotation of polarization plane caused by the magnetized medium is

\[
\psi = 810 \int \lambda^2 n_e(l) B(l) \cdot dl,
\]

(1.1)

here, \(\psi\) is total rotation angle (in rad), \(\lambda\) is wavelength (in m), \(n_e(l)\) is intervening electron density (in cm\(^{-3}\)), \(B\) is vector magnetic field (in \(\mu\)G), and \(dl\) is the unit vector of the line of sight (in kpc) pointing towards us. Note that electron density and magnetic field vary along the line of sight. To reveal the intervening magnetic fields, it is necessary to know the distribution of electron density along the line of sight.

For a cosmological radio source at a given location in the universe, e.g. at redshift \(z\), the wavelength \(\lambda(z)\) is also specifically related to observed wavelength by

\[
\lambda_{\text{obs}} = \frac{\lambda(z)}{(1 + z)}.
\]

So, the rotation measure (RM, in rad m\(^{-2}\)) of a radio source at a redshift, \(z_s\), should be defined as

\[
RM_{\text{obs}} = \frac{\psi_1 - \psi_2}{\lambda_{\text{obs}1}^2 - \lambda_{\text{obs}2}^2} = 810 \int_0^{z_s} (1 + z)^{-2} n_e(z) B(z) \cdot dl.
\]

(1.2)

In different cosmological models, the \(dl\) and \(dz\) are related by

\[
\frac{dl}{dz} = \frac{c}{H_0} (1 + z)^{-1} [\Omega_m (1 + z)^3 + (1 - \Omega_m - \Omega_\Lambda)(1 + z)^2 + \Omega_\Lambda]^{-1/2}.
\]

(1.3)

Here, \(H_0 = 100h\) km s\(^{-1}\)Mpc\(^{-1}\) is the Hubble constant, \(h\) is the dimensionless factor, \(c\) is the speed of light, \(\Omega_m\) is the dimensionless ordinary matter density, and \(\Omega_\Lambda\) is the vacuum energy density. Most recent measurements show that \(h = 0.72 \pm 0.05\), \(\Omega_m \sim 0.3\) and \(\Omega_\Lambda \sim 0.7\) [4, 23].

Observed Faraday rotation consists of three contributions,

\[
RM_{\text{obs}} = RM_{\text{in}} + RM_{\text{ig}} + RM_{\text{fg}},
\]

(1.4)

namely, the intrinsic rotation measure local to a source, \(RM_{\text{in}}\), the rotation measure from the intergalactic medium, \(RM_{\text{ig}}\), and the foreground RM from our Galaxy, \(RM_{\text{fg}}\). The foreground RM from our Galaxy are common contribution to RMs of radio sources located in a small sky region. To reveal the properties of intergalactic magnetic fields, the effect of intrinsic and foreground rotation measures should be eliminated from the observed values of \(RM_{\text{obs}}\).

Pulsars in our own Galaxy emit polarized radio emission, and their RMs can be used to measure the interstellar magnetic fields [16]. Observed Faraday rotation of pulsars does not have any intergalactic contribution or intrinsic contribution, nor do we have to consider the cosmological
effect on the wavelength. Therefore, the $RM$ (in radians m$^{-2}$) of a pulsar at distance $D$ (in kpc) can be simply given by $RM = 810 \int_0^D n_e B \cdot dl$. Positive $RMs$ correspond to the average fields directed toward us. In addition, the electron density between a pulsar and us can be measured by the pulse delay between the high and low radio frequencies (even at the two ends of a receiving radio wave band). This is the dispersion measure (DM) of a pulsar, $DM = \int_0^D n_e dl$. From the two observables, $DM$ and $RM$, we obtain a direct estimate of the field strength weighted by the local free electron density,

$$\langle B_\parallel \rangle = \frac{\int_0^D n_e B \cdot dl}{\int_0^D n_e dl} = 1.232 \frac{RM}{DM}. \quad (1.5)$$

where $RM$ and $DM$ are in their conventional units of rad m$^{-2}$ and cm$^{-3}$ pc and $B_\parallel$ is in $\mu$G.

2. RM tomography for magnetic fields in the Galactic disk

Pulsars are best probes for the Galactic magnetic fields. Magnetic fields in a large part of the Galactic disk have been delineated by Faraday rotation data of pulsars, which gives a very direct estimate of the line-of-sight component of the magnetic field through normalization by the dispersion measure (DM). They typically have substantial linear polarization, making the Faraday rotation relatively easy to measure; they are distributed in the Galaxy with approximately known distances, allowing the three-dimensional properties of the magnetic field to be investigated; and they apparently have no intrinsic rotation measure. RMs of extragalactic sources can be also used to reveal the Galactic magnetic fields. The RM average over a number of sources in a given sky region should be the common RM contribution from the Galactic disk, i.e. the integral of $n_e B$ from the boundary of the Galactic disk toward us along the line of sight. Interpretation of extragalactic RM data are then rested on the model of $n_e$ and $B$ in the interstellar space. However, these extragalactic RMs are unique probes for magnetized interstellar medium beyond the known pulsars up to the disk boundary.

2.1 Magnetic field structure in the Galactic disk

Previous analysis of pulsar RM data often used the model-fitting method, i.e., to model magnetic field structures in all paths from pulsars to us (observer) and fit them together with the electron density model to observed RM data. Significant improvement can be obtained now when RM and DM data are available for many pulsars in a given region with similar lines of sight. Measuring the gradient of RM with distance or DM is the most powerful method of determining both the direction and magnitude of the large-scale field in that particular region of the Galaxy. Field strengths in the region can be directly measured (instead of modeled) from the slope of trends in plots of RM versus DM. Based on Equation (1.5), we get

$$\langle B_\parallel \rangle_{d_1-d_0} = 1.232 \frac{\Delta RM}{\Delta DM}. \quad (2.1)$$

where $\langle B_\parallel \rangle_{d_1-d_0}$ is the mean line-of-sight field component in $\mu$G for the region between distances $d_0$ and $d_1$, $\Delta RM = RM_{d_1} - RM_{d_0}$ and $\Delta DM = DM_{d_1} - DM_{d_0}$.

Up to now, RMs of 550 pulsars have been observed. Most of the new measurements lie in the fourth and first Galactic quadrants and are relatively distant, which enable us
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Figure 1: The RM distribution of 374 pulsars with $|b| < 8^\circ$, projected onto the Galactic Plane. The linear sizes of the symbols are proportional to the square root of the RM values. The crosses represent positive RMs, and the open circles represent negative RMs. The approximate locations of four spiral arms are indicated. The large-scale structure of magnetic fields derived from pulsar RMs [11] are indicated by thick arrows.

The average RM variation along the Galactic longitude of extragalactic radio sources [3], especially these of the fourth Galactic quadrant, are very consistent with the magnetic field directions derived from the tangential regions of the arms (see Fig. 2). This implies that the dominant contribution to RMs of extragalactic radio sources behind the Galactic disk comes from the interstellar medium mainly in tangential regions.
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Figure 2: The general tendency of RM variations of extragalactic radio sources along the Galactic longitude, peaks and valleys [3], is very consistent with the large-scale structure of magnetic fields in the tangential regions derived from pulsar RMs [11].

Figure 3: Variation of the large-scale regular field strength with the Galactocentric radius derived from pulsar RM and DM data near the tangential regions [11]. Note that the “error-bars” are not caused by the uncertainty of the pulsar RM or DM data, but reflect the random magnetic fields in the regions.

2.2 Dependence of the field strength on the Galactocentric radius

Stronger regular magnetic fields in the Galactic disk towards the Galactic Center have been suggested previously [14, 24]. Measurements of the regular field strength in the Solar vicinity give values of $1.5 \pm 0.4 \mu G$ [21, 13, 15], but near the Norma arm it is $4.4 \pm 0.9 \mu G$ [10].

With significant more pulsar RM data now available, Han et al. were able to measure the regular field strength near the tangential points in the 1st and 4th Galactic quadrants [11], and then plot the dependence of regular field strength on the Galactocentric radii (see Fig. 3). Although uncertainties are large, there are clear tendencies for fields to be stronger at smaller Galactocentric radii and...
weaker in interarm regions. To parameterize the radial variation, an exponential function was used as following, which not only gives the smallest $\chi^2$ value but also avoids the singularity at $R = 0$ (for $1/R$) and unphysical values at large $R$ (for the linear gradient). That is,

$$B_{reg}(R) = B_0 \exp \left[ \frac{-(R - R_\odot)}{R_B} \right],$$

(2.2)

with the strength of the large-scale or regular field at the Sun, $B_0 = 2.1 \pm 0.3$ $\mu$G and the scale radius $R_B = 8.5 \pm 4.7$ kpc.

Figure 4: Composite magnetic-energy spectrum in our Galaxy. The large-scale spectrum was derived from pulsar RM data [7]. The thin solid and dashed/dotted lines at smaller scales are the Kolmogorov and 2D-turbulence spectra given by Minter & Spangler [18], and the upper one is from new measurements of Minter (2004, private email).

2.3 Field strength on different scales

Interstellar magnetic fields exist over a broad range of spatial scales, from the large Galactic scales to the very small dissipative scales, but with different field strength. Knowledge of the complete magnetic energy spectrum can offer a solid observational test for dynamo and other theories for the origin of Galactic magnetic fields.

Estimation of the large-scale field strength [13, 11] and a turbulent field strength at a scale of tens of pc [21, 19] is only the first step. The spatial power spectrum of electron density fluctuations from small scales up to a few pc [1] could be approximated by a single power law with a 3D spectral index $-3.7$, very close to the Kolmogorov spectrum, which gives us a hint that the magnetic energy on the small scales to a few pc should have the Kolmogorov spectrum as well. This was confirmed by Minter & Spangler who found [18] that structure functions of RM and emission measure were consistent with a 3D-turbulence Kolmogorov spectra of magnetic fields up to 4 pc, but with a 2D turbulence between 4 pc and 80 pc (see Fig. 4).
Pulsar RMs are the integration of field strength together with electron density over the path from a pulsar to us. Therefore, RM data of pulsars with different distances should reflect the fluctuations on different scales. Han et al. [7] used not only pulsars but also pulsar pairs with similar lines of sight to calculate the magnetic energy associated with each pulsar or pulsar pair. Using these pulsars and pulsar pairs, the averaged magnetic energy and the “differential” magnetic energy can be obtained at various scales, and then the spatial energy spectrum of the Galactic magnetic field in scales between $0.5 < \lambda < 15 \text{ kpc}$ can be derived [7]. The result is a 1D power-law, $E_B(k) \sim k^{-0.37\pm0.10}$, with $k = 1/\lambda$ (see Fig. 4). The rms field strength is approximately $6 \mu G$ over the relevant scales and the spectrum is much flatter than the Kolmogorov spectrum for the interstellar electron density and magnetic energy at scales less than a few pc. This study complements the derivation of the magnetic energy spectrum over the scale range $0.03 – 100 \text{ pc}$ by [18], showing that the magnetic spectrum becomes flatter at larger scales.

3. RM tomography for magnetic fields in the Galactic halo

The magnetic field structure in halos of other galaxies is difficult to observe. Our Galaxy is a unique case for detailed studies, since polarized radio sources all over the sky can be used as probes for the magnetic fields in the Galactic halo.

As we mentioned before, the foreground RM from our Galaxy are common contribution to RMs of radio sources. That is to say, an “averaging process”, which eliminates the random intrinsic RMs and discards the anonymous RMs, should be used to reveal the Galactic RM contribution. We removed any source if its RM value deviates from the average of their neighbours by 3 sigma, i.e. filtering out the outliers of RM values that is probably significantly from intrinsic RM, then from such a “cleaned” RM distribution in the sky, Han et al. identified the striking antisymmetry in the inner Galaxy respect to the Galactic coordinates [9, 12]. This RM sky can result from the azimuth magnetic fields in the Galactic halo with reversed field directions below and above the Galactic plane (see Fig. 2). Such a field can be naturally produced by an A0 mode of dynamo (see reference [27] for a review), and it is necessary to include this into any reasonable model for interstellar medium [25]. The observed filaments near the Galactic center should result from the dipole field in this scenario. The local vertical field component of $\sim 0.2 \mu G$ [13, 12] may be related to the dipole field in the solar vicinity.

I have shown [6] that the RM amplitudes of extragalactic radio sources in the mid-latitudes of the inner Galaxy are systematically larger than those of pulsars, indicating that the antisymmetric magnetic fields are not local but are extended towards the Galactic center, far beyond the pulsars. We are observing more RMs of extragalactic radio sources and modeling the RM sky with a various magnetic field structure in the Galactic halo. For example, the azimuthal halo field with reversed directions above and below the Galactic plane could simply result from a shearing of the dipole field by differentially rotating layers of the ISM.

4. RM tomography for magnetic fields in the nearby universe

To probe the magnetic fields on cosmological scales, we have to look at the variation of RMs of radio sources with the redshift of the sources after the foreground Galactic RM contribution is
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Figure 5: The antisymmetric rotation measure sky, derived from RMs of extragalactic radio sources after filtering out the outliers of anomalous RM values, should correspond to such a magnetic field structure in the Galactic halo as illustrated [9, 12].

eliminated. Three conditions have to be satisfied: 1). We have to measure the foreground RM sky to a certain level of accuracy. Looking at the RM sky in Fig.5, one can immediately see that the RMs near the two Galactic poles are on average very small. Whilst in other regions, the Galactic RMs are more difficult to assess accurately. A more extensive RM sky survey is required for this purpose. 2). To reveal the intergalactic RMs of a few rad m$^{-2}$, the measurements of each RM should be at least accurate to this level. With current techniques this is now achievable using the wide-band spectral-polarimeters available at many radio telescopes. 3). The redshift of measured objects must also be known. This is now becoming possible for large numbers of sources by virtue of new large-scale optical spectrum surveys, such as SDSS.

We have observed 110 objects with known redshift in the pole regions [8]. Together with previously published data, we found from RM data of two poles, see Fig. 6, that: 1). RM data clearly tend to have opposite signs which indicate a small but significant local vertical Galactic magnetic fields of 0.2 $\mu$G; 2) the deviations get larger at higher redshifts, which implies clearly that there is some kind of random RM contribution from intergalactic medium.

To understand the intergalactic magnetic fields, we still have three barriers to overcome. In
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Figure 6: The space distribution of radio sources in the Galactic pole regions which we have their rotation measures observed. The red points stand for the positive RMs and blue ones for the negatives. It is clear that the rotation measures tend to be more positive (red) in the south Galactic pole and negative in the north pole, indicating the local vertical Galactic magnetic fields [8].

each redshift range, we require a large number of objects with measured RMs, so that effect of their intrinsic RMs does not dominant. Second, we do not have enough information about the electron density distribution, such as whether it is clouded in the intergalactic space and how it couples with magnetic fields [28]. To delineate the intergalactic magnetic fields, there is still a long way to go.

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