We report on the current simulation studies regarding the reconstruction of Jets and Missing Transverse Energy (MET) with the CMS detector at the CERN proton-proton LHC accelerator. The performance of various jet algorithms is compared, when using calorimeter energy deposits as inputs to the algorithm. The plan for obtaining jet energy corrections is outlined and data-driven correction methods are described. Finally, the performance of MET reconstruction is summarized.
1. Jets in CMS

Almost all physics channels of interest at the LHC require good understanding of jet clustering by means of jet algorithm performances and optimization of its parameters, as well as the detector performances. In this section, several studies comparing the performance of different jet algorithms namely, Fast-\(k_T\) [1], SISCone [2], Midpoint Cone [3] and Iterative Cone [4] are presented. These jet algorithms can be applied to any given set of four-vectors, which allows one to study jets of partons, jets of particles remaining after the hadronization, and jets of energy deposited in the detector. A successful jet algorithm should provide a good correspondence between these three levels. It is desired that a jet algorithm is infrared and collinear safe that is being insensitive to addition of soft particles to the input list (soft gluon radiation) and being insensitive to having a certain energy distributed to two collinear particles instead of one, respectively. In the experiments, collinear unsafety is introduced by the finite granularity of the Calorimeter and/or any \(p_T\) threshold applied on the input objects.

The \(k_T\) algorithm merges particles by comparing the relative transverse momentum of each pair of particles in the event and is infrared and collinear safe, whereas the Cone-based algorithms cluster particles by trying to maximize the energy flow within a cone of radius \(R\). Seedless Infrared Safe Cone (SISCone) algorithm is the latest developed cone-based algorithm which is infrared safe to all orders in perturbative expansion and the algorithm itself does not apply a \(p_T\) threshold on the input particles. Another important performance parameter for jet algorithms at hadron colliders is the execution time. Figure 1 (left) shows the average CPU time per event required by each algorithm for jet reconstruction as a function of the number the of the Calorimeter Towers. Iterative Cone algorithm is employed by CMS in the High Level Trigger (HLT) for its short and predictable execution time. Note that with the fast implementation of \(k_T\) algorithm the execution time has been reduced significantly.

In order to quantify the jet reconstruction efficiency, a matching procedure between generator level (GenJets) and Calorimeter (CaloJets) jets is performed. The jet matching efficiency, shown in Fig. 1 (right), is defined as the fraction of GenJets which are matched to CaloJets with \(\Delta R < 0.5\), where \(\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}\), \(\eta\) and \(\phi\) represent the pseudorapidity and the azimuthal angle respectively. The SISCone and the \(k_T\) algorithms tend to give better efficiencies for very low \(p_T\) jets while all algorithms yield \(\sim 100\%\) efficiency for higher \(p_T\) jets.

Jet corrections are necessary for obtaining meaningful jet measurements that are consistent with the jets of partons emerging from a QCD hard collision. CMS is developing a factorized multi-level jet correction, shown schematically in Fig. 2, where each sub-correction is associated with different detector and physics effects. Most of these corrections can be obtained from collision data. Initially, however, the corrections will be derived from MC tuned on test beam data.

The offset corrections are applied to account for pile-up (PU) and the electronic noise in the detector and are expected to be relatively small, i.e. on average smaller than 0.5 GeV for a single pile-up event. The non-uniformities of the CMS Calorimeter and its non-linear response to the particles with different energies necessitate the development of corrections to the measured jet energies as functions of \(|\eta|\) (Relative \(\eta\)) and \(p_T\) (Absolute \(p_T\)) [5]. Relative-\(\eta\) corrections are applied in order to achieve a uniform the jet energy response versus \(\eta\), where the energy of a jet at a given pseudorapidity, is corrected to the most probable energy in the barrel region (\(|\eta| < 1.3\))
Jets and Missing Transverse Energy in CMS

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Figure 1: Left) Average CPU time required for jet reconstruction as a function of the number of CaloTowers above $E_T$ threshold. Right) Jet Matching Efficiency versus $p_T^{Gen}$.

Figure 2: Schematic picture of the factorized multi-level jet correction, where required corrections are shown solid boxes and analysis dependent optional ones are shown in dashed boxes.

of the Calorimeter. The results of these corrections obtained from the MC method are presented in Fig. 3 (left), where significant variations in jet energy response as a function of $\eta$ is flattened after the corrections. These corrections can be obtained using $p_T$ balance in back-to-back di-jet QCD events, where one jet being in the barrel region and any additional jets are being suppressed by a maximum $p_T$ threshold on the additional jets. The relative jet energy responses obtained using both MC and the data-driven methods are in good agreement (see Fig.3, right) verifying that such corrections can be obtained from data.

The $p_T$ balance in $\gamma/Z+$jet events, where the jet is in the control region ($|\eta| < 1.3$), are exploited for obtaining Absolute $p_T$ corrections. In the case of $\gamma$-jet balance the photon is measured in Electromagnetic Calorimeter (ECAL). The main background to this process is QCD di-jet events where one jet fakes a photon, and in order to reduce this background the isolated photons are selected. On the other hand, the $Z+$jet events, where muon decays of $Z$ are selected, provide relatively background free channel. Muons are identified using the Tracker and the Muon Chambers which give totally independent measurement from the Calorimeter where jets are measured. In both cases, the additional jets are suppressed by an upper threshold on their $p_T$. Figure 4 shows the expected $p_T(jet)/p_T(boson)$ for both $\gamma/Z+$jet for 100 $pb^{-1}$ of data. Studies show that these corrections can be obtained for jet $p_T$ up to 400(600) GeV using Z($\gamma$)+jet events. The results are found to be consistent with the ones obtained with the MC techniques within 5%, and combining the corrections from different methods by extrapolating them to higher $p_T$ region is planned.

The non-compensating feature of the CMS Calorimeter necessitate further corrections which account for the differences in response depending on the ElectroMagnetic Fraction (EMF) of the jet energy. These corrections can improve jet energy resolution up to 10%. On the other hand, the
response of the Calorimeter may differ for jets initiated by different types of partons, i.e. higher response for light quarks. These corrections can reach up to 10\% depending on the $p_T$ region. Further corrections to take into account Underlying Event (UE) and parton showering and hadronization are also investigated.

CMS develops an Asymmetry Method, a technique for measuring the jet energy resolutions from data, which relates the $p_T$ resolution to the resolution of $p_T$-imbalance between the two leading jets. By selecting events with an additional 3$^{rd}$ jet and studying the resolution as a function of the max $p_T$ requirement on the extra jet, a soft radiation correction is taken into account (see the left pane in Fig. 5). The results found to be consistent with the MC based methods verifying that jet energy resolution can be measured directly from data (see the right pane in Fig. 5 right).

2. Missing Transverse Energy in CMS

The large pseudorapidity coverage of the CMS detector allows for rather precise test of 2D-momentum conservation in the plain perpendicular to the direction of the beams. Therefore, any
measured significant imbalance in transverse momentum, Missing Transverse Energy ($E_{T}$), can be considered as the signature of weakly interacting particles which typically escape the detector without being measured. $E_{T}$ in CMS is determined from the vector sum over uncorrected transverse energy deposits in projective Calorimeter Towers [6]:

$$E_{T} = - \sum_{n} (E_{n} \sin \theta_{n} \cos \phi_{n} \hat{i} + E_{n} \sin \theta_{n} \sin \phi_{n} \hat{j}) = E_{x} \hat{i} + E_{y} \hat{j}. \quad (1)$$

$E_{T}$ is a crucial observable for measuring not only the Standard Model (SM) processes (i.e. W boson, top quark production) but also for searches for new physics beyond the SM which are associated with relatively large $E_{T}$. However, $E_{T}$ is extremely sensitive to various detector malfunctions and particles hitting poorly instrumented regions of the detector. Therefore, a great care has to be taken in order to understand the missing transverse energy distributions in detail before claiming any discovery beyond SM.

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**Figure 5:** Left: Jet energy resolution from di-jet asymmetry as a function of the max $p_{T}$ threshold on the 3rd jet in the event, extrapolated to zero. Right: Resolutions obtained from Asymmetry Method and MC truth.

**Figure 6:** Left: $E_{T}$ resolution versus $\sum E_{T}$ for QCD dijet sample. Right: The improvements on $E_{T}$ projection to Z boson direction gained after applying muon and jet calibration corrections on $E_{T}$. 
Figure 6 (left) shows the missing transverse energy resolution as a function of scalar sum of the transverse energies in the Calorimeter Towers ($E_T$) in QCD. The resolution is parametrized by 
\[ \sigma(E_T) = A \oplus B \sqrt{\sum E_T - D} \oplus C(\sum E_T - D), \]
where the $A$ ("noise") term represents effects due to electronic noise, PU and UE; the $B$ ("stochastic") term represents the statistical sampling nature of the energy deposit in each Calorimeter Towers; the $C$ ("constant") term represents residual due to non-linearities, cracks and dead material; $D$ ("offset") represents the effects of noise and PU on $\sum E_T$.

As for jets, $E_T$ needs to be corrected for various effects. The jet energy corrections are used for calibrating the measured $E_T$. The vectorial sum of absolute corrections on jet $p_T$ is subtracted from the measured raw $E_T$ given in Eq. 1 in order to obtain calibrated $E_T$. The EMF dependent corrections are also taken account. The muons, as being minimum ionizing particles, deposit very small fraction of their energy in the Calorimeter, and hence mimic $E_T$. In Fig. 6 (right), the improvements due to these corrections on the missing transverse energy projection parallel to the Z boson direction in Z+jets events, are shown. Another correction to $E_T$ become relevant when there are jets of tau lepton decays, since the response of the Calorimeter to such jets differs from those of arbitrary jets. In order to account for this effect, the measured tau energy is replaced by the energy measured by the Particle Flow (PF) algorithm which provides rather precise tau measurement. This correction improves $E_T$ resolution significantly.

3. Conclusions

Some of the highlights of jet and missing transverse energy studies in CMS are presented. The performances of the most relevant and recent jet algorithms are exercised. CMS develops a factorized jet energy correction, where the correction factors will be based on MC techniques at the start-up, as possible as data-driven when collision data is available and in long term it they will be driven from MC tuned on collision data. The $E_T$ is an important but a complicated observable that requires careful studies to understand the detector and beam effects on it. The first collision data will be crucial to understand both jet and $E_T$ objects and their calibrations.

References