

## Gluino-mediated FCNCs in the MSSM with large $\tan\beta$

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We present results of our study of  $\tan\beta$ -enhanced loop corrections in the Minimal Supersymmetric Standard Model (MSSM) with Minimal Flavour Violation (MFV). We demonstrate that these corrections induce flavour changing neutral current (FCNC) gluino couplings which have a large impact on the Wilson coefficient  $C_8$  of the chromomagnetic operator. To illustrate the phenomenological consequences of this gluino-squark contribution to  $C_8$ , we briefly discuss its effect on the mixing-induced CP asymmetry in the decay  $B_d \rightarrow \phi K_S$ .

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## 1. Introduction

The Minimal Supersymmetric Standard Model (MSSM) contains two Higgs doublets  $H_u$  and  $H_d$  coupling to up-type and down-type quark fields, respectively. The neutral components of these Higgs doublets acquire vacuum expectation values (vevs)  $v_u$  and  $v_d$  with the sum  $v_u^2 + v_d^2$  being fixed to  $v^2 \approx (174 \text{ GeV})^2$  and the ratio  $\tan\beta \equiv v_u/v_d$  remaining as a free parameter. Large values of  $\tan\beta$  ( $\sim 50$ ) are theoretically motivated by bottom-top Yukawa unification, which occurs in SO(10) GUT models with minimal Yukawa sector, and phenomenologically preferred by the anomalous magnetic moment of the muon [1]. Since a large value of  $\tan\beta$  corresponds to  $v_d \ll v_u$ , it leads to enhanced corrections in amplitudes where the tree-level contribution is suppressed by the small vev  $v_d$  but the loop-correction involves  $v_u$  instead.

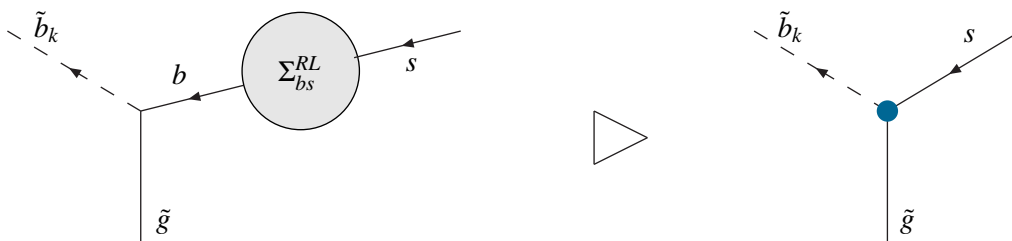
These  $\tan\beta$ -enhanced loop-corrections lead to a plethora of phenomenological consequences: They modify the relation between the down-type Yukawa couplings  $y_{d_i}$  and the quark masses  $m_{d_i}$  [2], give corrections to the elements of the CKM matrix [3] and induce FCNC couplings of the neutral Higgs bosons to down quarks [4]. Recently we found that also FCNC couplings of gluinos and neutralinos to down quarks are generated in this way [5]. In this article we explain how this FCNC gluino-couplings arise and discuss the phenomenological consequences.

## 2. Flavour-changing gluino coupling in naive MFV at large $\tan\beta$

At tree-level the bottom mass  $m_b$  is generated by coupling the  $b$ -quark to the Higgs field  $H_d$  and is thus proportional to the small vev  $v_d$ . For this reason self-energy amplitudes  $\Sigma_{bi}^{RL}$  ( $i = d, s$ ) can be  $\tan\beta$ -enhanced compared to  $m_b$  if they involve  $v_u$  instead of  $v_d$ . In this article we discuss the impact of these enhanced self-energies in the framework of naive MFV as defined in Ref. [5]. For the analysis of the analogous effects in the general MSSM we refer to Ref. [6]. For definiteness we focus on  $b \rightarrow s$  transitions and parameterise the corresponding self-energy, which is generated by chargino-squark-loops, as

$$\Sigma_{bs}^{RL} = V_{tb}^* V_{ts} m_b \epsilon_{FC} \tan\beta. \quad (2.1)$$

In naive MFV the quark-squark-gluino coupling is flavour-diagonal at tree-level. It receives flavour-changing loop-corrections among which we want to consider those induced by an insertion of the self-energy  $\Sigma_{bs}^{RL}$  in the down-quark line (see fig. 1 for the case of an external  $s$ -quark). If the  $s$ -quark is on-shell, this correction is local and can be promoted to a FCNC gluino coupling.



**Figure 1:** FCNC gluino coupling for an on-shell  $s$ -quark induced by the  $\tan\beta$ -enhanced self-energy  $\Sigma_{bs}^{RL}$

Since the  $b$ -quark propagator  $-i/m_b$  ( $m_s$  is set to zero) cancels the factor  $m_b$  in  $\Sigma_{bs}^{RL}$ , the resulting coupling is proportional to

$$\kappa_{bs} = g_s V_{tb}^* V_{ts} \varepsilon_{FC} \tan\beta. \quad (2.2)$$

If  $\tan\beta$  is large enough to compensate for the loop-factor  $\varepsilon_{FC}$ , the coupling  $\kappa_{bs}$  can be of order  $\mathcal{O}(1)$  apart from the CKM factor  $V_{tb}^* V_{ts}$ , which preserves the MFV structure.

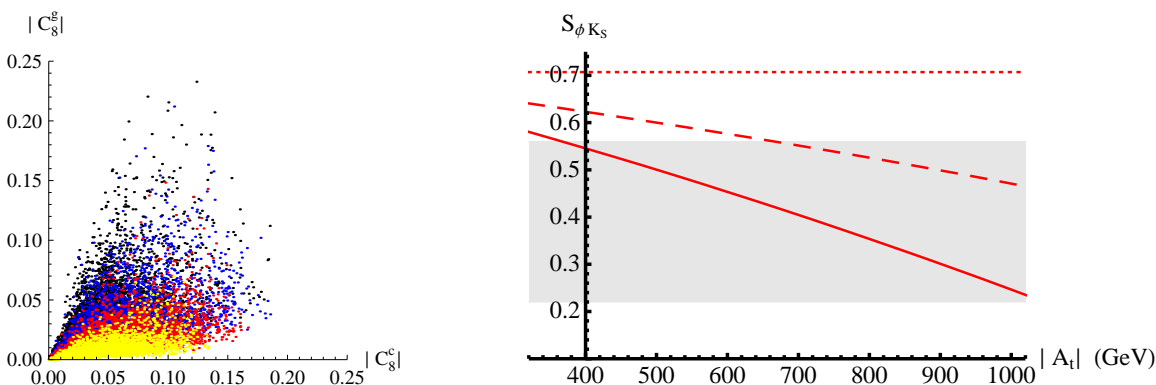
In order not to spoil the perturbative expansion a special treatment is required for these  $\tan\beta$ -enhanced corrections to resum them to all orders. This is usually done using an effective theory with the SUSY particles integrated out keeping only Higgs fields and SM fields [2–4]. However, since we want to study  $\tan\beta$ -enhanced effects in the quark-squark-gluino-coupling, we cannot integrate out the gluino and squarks and this technique is not appropriate here. In Ref. [5] instead the diagrammatic method developed in Ref. [7] is extended to the case of flavour-changing interactions. The result is that contributions of the form  $(\text{loop} \times \tan\beta)^n$  can be included to all orders  $n = 1, 2, \dots$  into the FCNC gluino coupling by replacing

$$\varepsilon_{FC} \tan\beta \longrightarrow \frac{\varepsilon_{FC} \tan\beta}{1 + (\varepsilon_b - \varepsilon_{FC}) \tan\beta} \quad (2.3)$$

in Eq. (2.2). Here  $\varepsilon_b$  denotes the counterpart of  $\varepsilon_{FC}$  in the parameterisation of the flavour-conserving self-energy  $\Sigma_b^{RL}$  analogous to Eq. (2.1). Explicit formulae for  $\varepsilon_b$  and  $\varepsilon_{FC}$  can be found in Ref. [5].

### 3. Sizable effect in $C_8$

The FCNC gluino coupling discussed in the last section gives rise to new contributions to the Wilson coefficients of the effective  $\Delta B = 1$  and  $\Delta B = 2$  Hamiltonians. Most of these contributions turn out to be numerically small for two reasons: Firstly, the FCNC gluino coupling is numerically small; for positive  $\mu$  typical values are around  $\kappa_{bs} \sim 0.1 \cdot V_{tb}^* V_{ts}$ . Secondly, unlike the higgsino-part of chargino diagrams, the gluino contributions suffer from a GIM suppression because the gluino coupling is universal for all quark flavours.



**Figure 2:** Left: Magnitudes of chargino and gluino contributions to  $C_8$  scanned over the MSSM parameter space. Right:  $S_{\phi K_S}$  as a function of  $|A_t|$ .

There is one exception: Chirally enhanced contributions to the magnetic and chromomagnetic operators  $\mathcal{O}_7$  and  $\mathcal{O}_8$  involve a left-right-flip in the squark-line which is proportional to the corresponding quark mass and thus distinguishes between different squark flavours. Whereas the corresponding contribution from gluino-squark-loops to  $C_7$  is accidentally small, the one to  $C_8$  can indeed contribute as much as the well known chargino-squark diagram. This can be seen from the left diagram in fig. 2 where the magnitudes of both contributions  $|C_8^c|$  and  $|C_8^g|$  are shown for a scan over the MSSM parameter space with positive  $\mu$ . The colour code (yellow:  $200\text{ GeV} < \mu < 400\text{ GeV}$ , red:  $400\text{ GeV} < \mu < 600\text{ GeV}$ , blue:  $600\text{ GeV} < \mu < 800\text{ GeV}$ , black:  $800\text{ GeV} < \mu < 1000\text{ GeV}$ ) reflects the fact that the importance of  $C_8^g$  grows with  $\mu$ . All points in the plot are in agreement with the constraints from  $\mathcal{B}(\bar{B} \rightarrow X_s \gamma)$  and the experimental lower bounds for the sparticle and lightest Higgs Boson masses. Note that we allow for an arbitrary phase for the parameter  $A_t$ . However, to avoid the possibility of fulfilling the  $\mathcal{B}(\bar{B} \rightarrow X_s \gamma)$  constraint by an unnatural fine-tuning of this phase, the additional condition  $|C_7^{Susy}| < |C_7^{SM}|$  is imposed.

As a consequence the  $\tan\beta$ -enhanced FCNC gluino coupling should affect those low energy observables with a strong dependence on  $C_8$ . To illustrate this fact we have plotted the mixing-induced CP asymmetry  $S_{\phi K_S}$  of the decay  $\bar{B}^0 \rightarrow \phi K_S$  as a function of  $|A_t|$  in the right diagram of fig. 2. The parameter point chosen for the plot fulfills all constraints mentioned above. The shaded area represents the experimental  $1\sigma$  range, the dotted line the SM contribution in leading-order QCD factorisation. For the results corresponding to the dashed and the solid lines we have in addition taken into account the effects of  $C_8^c$  and  $C_8^c + C_8^g$ , respectively. The plot demonstrates that for complex  $A_t$  the gluino-squark contribution can indeed have a large impact on  $S_{\phi K_S}$ , especially if  $|A_t|$  is large.

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