Selected recent quantum chromodynamics (QCD) measurements are reviewed for Fermilab Run II Tevatron proton-antiproton collisions studied by the Collider Detector at Fermilab (CDF) and DØ Collaborations at a centre-of-mass energy of $\sqrt{s} = 1.96$ TeV. Tantamount to Rutherford scattering studies at the TeV scale, inclusive jet and dijet production cross-section measurements are used to seek and constrain new particle physics phenomena, test perturbative QCD calculations, inform parton distribution function (PDF) determinations, and extract a precise value of the strong coupling constant, $\alpha_s(m_Z) = 0.1161^{\pm0.0041}_{-0.0048}$. Inclusive photon production cross-section measurements reveal an inability of next-to-leading-order (NLO) perturbative QCD (pQCD) calculations to describe low-energy photons arising directly in the hard scatter. Events with $\gamma + 3$-jet configurations are used to measure the increasingly important double parton scattering (DPS) phenomenon, with an obtained effective interaction cross section of $\sigma_{\text{eff}} = 16.4 \pm 2.3$ mb. Observations of central exclusive particle production demonstrate the viability of observing the Standard Model Higgs boson using similar techniques at the Large Hadron Collider (LHC). Three areas of inquiry into lower energy QCD, crucial to understanding high-energy collider phenomena, are discussed: the examination of intra-jet track kinematics to infer that jet formation is dominated by pQCD, and not hadronization, effects; detailed studies of the underlying event and its universality; and inclusive minimum-bias charged-particle momentum and multiplicity measurements, which are shown to challenge the Monte Carlo generators.
1. Introduction

Quantum chromodynamics (QCD), the theory of the strong interaction between quarks and gluons, is intrinsic to experimental studies of hadron collisions. This paper reviews several recent QCD results from the CDF and DØ experiments in analyses of $\sqrt{s} = 1.96$ TeV $p\bar{p}$ collisions covering up to 2.7 fb$^{-1}$ of time-integrated luminosity. The general approach has been to search for new physics phenomena, test QCD theory, enable electroweak and exotic measurements by informing Monte Carlo (MC) background models, and lay the groundwork for the LHC era of $pp$ collisions.

2. Inclusive Jet and Dijet Production

Heedful testing of perturbative QCD (pQCD) at the shortest distance scales ever studied in collider experiments is provided through measurements of differential inclusive jet and dijet cross sections. Recent CDF [1] and DØ [2] results, which agree mutually and with next-to-leading-order (NLO) pQCD calculations over eight orders of magnitude, are shown in Fig. 1. Articulation of the Tevatron measurements into several rapidity regions has revealed that the experimental precision now exceeds that of the parton distribution function (PDF) uncertainties and that softer gluons at high Feynman $x \geq 0.25$ need to be included in the PDF fits.

Also shown in Fig. 1 are recently extracted correlated values of the strong coupling constant $\alpha_s$ by DØ [3]. Inclusive cross sections for jets with transverse momentum $50 < p_T < 145$ GeV, corresponding to $x \leq 0.25$, were used to ensure negligible correlations between PDFs and extracted $\alpha_s$ values and to derive a mean of $\alpha_s(m_Z) = 0.1161^{+0.0041}_{-0.0048}$ [3]. The precise DØ measurements lie at energies intermediate to results from the HERA experiments (Fig. 1) and to those from an earlier CDF Run I result [4], which spanned $40 < p_T < 250$ GeV.

Inclusive dijet observables are favoured harbingers of new physics phenomena. Fig. 2 shows recent results from CDF [5] and DØ [6] of dijet invariant mass ($M_{jj}$) distributions, for which Standard Model (SM) extensions predict resonant enhancements. Both experiments demonstrate a mass reach out beyond 1.2 TeV/$c^2$ and test pQCD predictions, with no indications of resonances. CDF sets the tightest 95% confidence level (CL) mass exclusion limits to date on several exotic particle species that decay to two jets: excited quarks, colour-octet $\rho_T$ mesons, axigluons, flavour-universal colorons, and $W'$ and $Z'$ bosons [5]. DØ demonstrates PDF sensitivity at forward maximum rapidities in the range $2.0 < |y_{\text{max}}| < 2.4$, showing softer high-$x$ gluons to be favoured [6].

**Figure 1:** [left] CDF [1] and [centre] DØ [2] inclusive jet differential cross sections, for multiple rapidity regions, compared to NLO QCD; [right] derived $\alpha_s(p_T)$ and $\alpha_s(m_Z)$ values as a function of jet $p_T$ [3].
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**Figure 2:** [left] CDF [5] and [centre] DØ [6] dijet-mass differential cross sections compared to NLO QCD predictions; [right] DØ dijet angular distributions [7].

Fig. 2 also shows consistency between pQCD and a DØ measurement of the dijet angular distribution, an observable that is complementary to $M_{jj}$ in its capacity to reveal new phenomena [7]. Rutherford and QCD scattering are largely insensitive to $\chi_{dijet}$, which is expected to peak at low values (central rapidities) for new physics such as composite quarks, large extra spatial dimensions (LEDs), and TeV$^{-1}$ scale extra dimensions. DØ has set the most stringent 95% CL limits on the quark compositeness scale $\Lambda > 2.9$ TeV, the ADD LED (GRW) effective Planck scale $M_S > 1.6$ TeV, and the TeV$^{-1}$ ED compactification scale $M_C > 1.6$ TeV [7].

**3. Inclusive Photon Production and Double Parton Scattering**

Photons emerging directly from $p\bar{p}$ collisions are unaffected by fragmentation and hadronization, and therefore serve as potent probes of the hard parton scattering dynamics, with potential sensitivity to gluon PDFs. Fig. 3 depicts recent CDF [8] and DØ [9] inclusive photon production cross-section measurements, which agree within experimental uncertainties and show that NLO pQCD has difficulty describing the behaviour in data at low photon $p_T$. Further theoretical effort will be necessary to understand this discrepant region.
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Vector meson photoproduction

Figure 4: [left] CDF central exclusive $\mu^+\mu^-$ invariant mass distribution for $p\bar{p} \to p [\mu^+\mu^- (\gamma)] \bar{p}$ processes [13]; [right] CDF $k_T$ distribution of particles in a cone of 0.5 rad around the jet axis in a dijet invariant mass bin with $\langle Q \rangle = 19$ GeV, corresponding to dijet masses in the range $66 < M_{jj} < 95$ GeV/c$^2$ [14].

DØ has studied $\gamma + 3$-jet events to measure double parton scattering (DPS), whereby two pairs of partons undergo hard interactions in a single $p\bar{p}$ collision. DPS is not only a background to many rare processes, especially at higher luminosities, but also provides insight into the spatial distribution of partons in the colliding hadrons. The DPS cross section is expressed as $\sigma_{\gamma + 3\text{jet}}^{\text{DPS}} \equiv \sigma_{\gamma j}/\sigma_{jj}/\sigma_{\text{eff}}$, where $\sigma_{\text{eff}}$ is the effective interaction region that decreases for less uniform spatial parton distributions. DØ measures a mean of $\sigma_{\text{eff}} = 16.4 \pm 2.3$ mb [10], which is consistent with an earlier CDF result [11], and finds $\sigma_{\text{eff}}$ to be independent of jet $p_T$ in the second interaction. If more precise studies can reveal a $\sigma_{\text{eff}}$ sensitivity to jet $p_T$, this could indicate a dynamical departure from the naïve assumption that $\sigma_{\gamma + 3\text{jet}}^{\text{DPS}}$ depends on an uncorrelated product of PDFs in $\sigma_{\gamma j}$ and $\sigma_{jj}$ [12].

4. Central Exclusive Particle Production

Central exclusive processes are those where the colliding hadrons emerge intact but impart $\gamma/g$ combinations that interact at higher order to produce fully measurable states at low rapidities, with surrounding rapidity regions devoid of particles. CDF recently reported observations of $p\bar{p} \to p[\text{dijet}]\bar{p}$, in dijet events with $E_T(\text{jet}) > 10$ GeV; and $p\bar{p} \to p [\mu^+\mu^- (\gamma), J/\psi, \psi(2S), \chi^0 c] \bar{p}$, with two oppositely charged central muons and either no other particles or one additional photon detected (see Fig. 4) [13]. Consideration of the SM Higgs $H \to b\bar{b}$ signature and quantum-number analogies between the scalar $\chi^0 c$ meson and the H boson permits these measurements to demonstrate the viability of exclusive SM Higgs production through $pHp$ processes at the LHC [13].

5. Jet Fragmentation, Underlying Event, and Minimum Bias Studies

Soft QCD interactions in hadron collisions, studied through charged-particle observables, are experimentally and theoretically challenging yet crucial to understanding high $p_T$ phenomena. A CDF study of the transverse momenta ($k_T$) of intra-jet particles with respect to their jet axis has provided insight into which stage of jet formation principally determines jet characteristics [14]. Fig. 4 shows a $k_T$ distribution resembling resummed pQCD predictions, indicating support for local parton-hadron duality and a de-emphasis of non-perturbative hadronization effects in jet formation.
The underlying event (UE) consists of the beam-beam remnants minus the hard-scattering products and is becoming increasingly important to the discovery and precision potential at hadron colliders. CDF has conducted an extensive program of UE studies that exploit jet and Drell-Yan event activity topologies to maximize the sensitivity of UE observables [15]. Refs. [15] contain several distributions of UE-sensitive observables, corrected to the particle level, that suggest the UE may be universal (independent of the hard process) and inform MC tuning and development.

Other important inputs into MC tuning arise in inclusive inelastic \( p\bar{p} \) collisions, studied using a minimum-bias trigger under low luminosity conditions. CDF has measured an inclusive differential charged-particle \( p_T \) cross section over 11 orders of magnitude (see Fig. 5), finding poor agreement with \textsc{Pythia} at higher momenta [16]. Fig. 5 also shows the measured correlation between the mean \( p_T \) and multiplicity of charged particles in minimum-bias events, observables to which the MC tuning parameters favouring multiple parton interactions (MPI) are particularly sensitive. The indicated charged-particle multiplicity distribution is the most precise and extensive ever measured in the \( |\eta| \leq 1 \) pseudorapidity range; existing MC calculations describe the high-multiplicity region poorly.

6. Concluding Remarks

The Tevatron experiments now provide precision QCD physics at \( \sqrt{s} = 1.96 \) TeV, and measurements common to both CDF and DØ are mutually consistent. The Rutherford scattering approach to studying the fundamental constituents of matter has now soundly entered the TeV regime, with stringent constraints on new physics, tests of pQCD, precise measurements of \( \alpha_s \), insight into jet fragmentation processes, and information on high-\( x \) PDF gluon content. Theoretical improvements are called for in several places, in particular to describe the observed photon cross section and inclusive particle production event characteristics. These results are based on less than one third of the anticipated complete Run II sample, with more measurements expected in the coming years to illuminate the Large Hadron Collider era of QCD rediscovery and discovery, now begun!
References


[3] V. M. Abazov et al. (DØ), Determination of the strong coupling constant from the inclusive jet cross section in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV, Phys. Rev. D 80, 111107(R) (2009) [arXiv:0911.2710v3].


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