

## Charm physics at BaBar and Belle

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**Diego Milanés**<sup>\*†</sup>

*Universitat de Valencia - IFIC*

*E-mail: milanés@slac.stanford.edu*

Recent results on charm physics from Belle and BaBar are reported. These include studies of charm mixing,  $CP$  violation in the charm sector and properties of charmed meson decay. Measurements of the  $D_s$  pseudoscalar purely leptonic decay branching fractions are also reported, which allow for experimental comparisons with the lattice calculation of the  $f_{D_s}$  decay constant.

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<sup>\*</sup>Speaker.

<sup>†</sup>On behalf of the BaBar Collaboration.

During the last decade the  $B$ -factories [1], BaBar and Belle, have played a crucial role in the understanding of the heavy flavor sector in the Standard Model (SM). Both detectors use asymmetric energy  $e^+e^-$  beams at the c.m. energy of the  $\Upsilon(4S)$  resonance, where  $\sigma(e^+e^- \rightarrow c\bar{c}) \sim 1.3$  nb, achieving more than  $6 \times 10^8$  and  $9 \times 10^8$  charm events in BaBar and Belle, respectively. At  $B$ -factories,  $D^0$  analyses share some aspects:  $D^0$  mesons are produced with high-momentum in the c.m. frame, from the  $e^+e^- \rightarrow D^{*+}(D^0\pi_s^+)X^-$  decay; the flavor of the  $D^0$  is identified ("tagged") at production with the charge of the low-momentum  $\pi_s^+$ ; these events are usually characterized using the invariant mass of the exclusively reconstructed  $D^0$  meson,  $m_{D^0}$ , and the mass difference between the reconstructed  $D^{*+}$  and  $D^0$  mesons,  $\Delta m = m_{D^{*+}} - m_{D^0}$ .

## 1. Extraction of the $f_{D_s}$ decay constant

The pseudoscalar meson decay constant  $f_{D_s}$  contains information on the overlap of the wave functions of the light and heavy quarks inside the  $D_s$  meson. The determination of  $f_{D_s}$  is very important, since it is an input for the calculation of hadronic matrix elements for several key processes. The leptonic decays of the  $D_s$  meson, are CKM favored and mediated by tree level diagrams via  $W$  boson exchange, resulting in a precise and clean way to measure  $f_{D_s}$ , which is used to validate lattice QCD calculations that are also applicable to  $B$  meson decays. It may be also a source of New Physics (NP), since several models involving physics beyond the SM can induce a difference between the theoretical prediction and the measured value. The most precise SM theoretical prediction is  $f_{D_s} = (241 \pm 3)$  MeV, obtained from unquenched lattice QCD [2].

In the SM, the total decay width of the  $D_s^+$  into the leptonic final state is

$$\Gamma(D_s^+ \rightarrow l^+ \nu_l) = \frac{G_F^2}{8\pi} M_{D_s^+}^3 \left( \frac{m_l}{M_{D_s^+}} \right)^2 \left( 1 - \frac{m_l^2}{M_{D_s^+}^2} \right)^2 |V_{cs}|^2 f_{D_s}^2, \quad (1.1)$$

where  $M_{D_s^+}$  and  $m_l$  are the  $D_s^+$  and lepton masses, respectively,  $G_F$  is the Fermi constant,  $|V_{cs}|$  is the magnitude of the CKM matrix element. The factor  $(m_l/M_{D_s^+})^2$  is an helicity effect, while  $(1 - m_l^2/M_{D_s^+}^2)^2$  is a phase-space factor.

The BaBar collaboration analyzed the decay chain  $D_s^+ \rightarrow \tau^+ \nu_\tau$  with  $\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau$  [3]. Here, the signal branching fraction  $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau)$  relative to the well measured branching fraction  $\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+) = (1.49 \pm 0.09)\%$ , is determined and used to extract the decay constant  $f_{D_s}$ . In the process  $e^+e^- \rightarrow c\bar{c} \rightarrow D_s^{*+} \bar{D}_{TAG} \bar{K} X$ , the  $D_s^{*+}$  is reconstructed as a missing particle, and the subsequent decay  $D_s^{*+} \rightarrow D_s^+ \gamma$  yields an inclusive  $D_s^+$  data sample,  $\bar{D}_{TAG}$  refers to a fully reconstructed hadronic  $\bar{D}$  decay required to suppress large light-quark background,  $\bar{K}$  is a  $K^-$  or  $\bar{K}^0$  meson needed to assure overall strangeness balance, and  $X$  stands for any number of charged or neutral pions produced in the fragmentation process. The measured value is  $f_{D_s} = (233 \pm 13(\text{stat.}) \pm 10(\text{syst.}) \pm 7(\text{th.}))$  MeV, where the last uncertainty arises from theoretical inputs. The  $f_{D_s}$  world average from the Heavy Flavors Averaging Group (HFAG)[4], including this result, is  $f_{D_s} = (254.6 \pm 5.9)$  MeV, where the discrepancy with the theoretical value is  $\sim 2\sigma$ .

## 2. Charm mixing and $CP$ violation

Mixing of neutral mesons has been observed in the  $K^0$  [5],  $B_d^0$  [6] and  $B_s^0$  [7] systems, and

in the last few years strong experimental evidence in the  $D^0$  system was also claimed [8, 9, 10, 11, 12, 13]. Neutral  $D$  mesons, are created as flavor eigenstates of strong interactions but they may oscillate through weak interactions. The mixing process is described by the parameters  $x = (m_1 - m_2)/\Gamma$  and  $y = (\Gamma_1 - \Gamma_2)/2\Gamma$ , where  $m_{1,2}$  and  $\Gamma_{1,2}$  are the corresponding masses and widths of the mass eigenstates  $|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$  and  $\Gamma = (\Gamma_1 + \Gamma_2)/2$ . In the SM, mixing arises from  $|\Delta C = 2|$  transitions ( $C$  stands for the charm quantum number) from short-distance box diagrams containing only down-type quarks, highly suppressed by either GIM cancellation mechanism or small CKM couplings. Enhancement of mixing may appear introducing models beyond SM [14], or also accounting for  $|\Delta C = 1|$  long-distance SM contributions, via hadronic intermediate states accesible from both  $D^0$  and  $\bar{D}^0$ . Theoretical predictions for  $x$  and  $y$  span a large range ( $10^{-5} - 10^{-2}$ ) showing that  $D^0 - \bar{D}^0$  mixing process is very hard to calculate. However, SM predictions converge to the fact that  $|x| < |y|$  and therefore  $|x| \gg |y|$  can be addressed as a signature of NP.

Regarding  $CP$  violation ( $CPV$ ), it can appear due to three different sources:  $CPV$  in the decay if  $|\bar{A}_f/A_f| \neq 1$ ;  $CPV$  in the mixing if  $|q/p| \neq 1$ ; and  $CPV$  in the interference of the decay and mixing if  $\phi = \arg\{q/p \cdot \bar{A}_f/A_f\} \neq 0, \pi$ , where the initial state ( $t = 0$ ) amplitudes are  $A_f \equiv \langle f | \mathcal{H} | D^0 \rangle$  and  $\bar{A}_f \equiv \langle f | \mathcal{H} | \bar{D}^0 \rangle$ . In the SM it is predicted to be very small ( $< 10^{-4}$ ) and any evidence of  $CPV$  with current data samples can be addressed as a NP effect.

**Wrong-Sign hadronic decays.** The first strong evidence of mixing in the charm sector was found by the BaBar experiment [8], in the Wrong-Sign (WS)  $D^0 \rightarrow K^+ \pi^-$  decay. This final state can be achieved via a direct doubly-Cabibbo-suppressed (DCS) decay, or by mixing to a  $\bar{D}^0$  and a further Cabibbo-favored (CF) decay,  $D^0 \rightarrow \bar{D}^0 \rightarrow K^+ \pi^-$ . In the small mixing limit and assuming  $R_D \equiv A_f/\bar{A}_f \ll 1$ , the time-dependent decay width is given by

$$\Gamma_{D^0 \rightarrow f_{WS}}(t) \sim e^{-\Gamma t} \left\{ R_D + y' \sqrt{R_D} (\Gamma t) + \frac{x'^2 + y'^2}{2} (\Gamma t)^2 \right\}, \quad (2.1)$$

where,  $x' = x \cos \delta_{K\pi} + y \sin \delta_{K\pi}$  and  $y' = -x \sin \delta_{K\pi} + y \cos \delta_{K\pi}$ , with  $\delta_{K\pi}$  the relative strong phase among the DCS and CF amplitudes. Time evolution allows to disentangle the different contributions to the process, DCS decay (no time dependence), mixing ( $\sim t^2$ ) and their interference ( $\sim t$ ). Here, the unknowledge of the phase  $\delta_{K\pi}$  avoids the direct extraction of  $x$  and  $y$ . BaBar measurement has been performed on a  $384 \text{ fb}^{-1}$  data sample with  $4030 \pm 90$  WS signal events. The reconstructed proper time has been modeled with the Eq. 2.1 convolved with a resolution function determined using the Right-Sign (RS) signal events. The fit result for the rotated mixing parameters is  $x'^2 = (-0.022 \pm 0.030(\text{stat.}) \pm 0.021(\text{syst.}))\%$  and  $y' = (0.97 \pm 0.44(\text{stat.}) \pm 0.31(\text{syst.}))\%$  with a correlation of  $-0.95\%$ , excluding the no-mixing hypothesis ( $x' = y' = 0$ ) at  $3.9\sigma$ . Belle [15] and CDF [10] experiments have reported compatible results in this decay mode.

**Decay into  $CP$  eigenstates.** The presence of mixing is expected to modify the decay proper time distributions of states with different  $CP$  content. The study of these differences, between  $CP$ -even eigenstates  $D^0 \rightarrow h^+ h^-$  ( $h = \pi, K$ ), and the  $CP$ -mixed CF  $D^0 \rightarrow K^- \pi^+$  state, has led also to determination of experimental evidence of mixing in the charm sector. In fact, the first evidence of mixing in the Belle experiment [9], was observed in this kind of analysis. Here, the time-dependent amplitude of the decay into the  $CP$  eigenstate in the small mixing limit is

$\Gamma_{D^0 \rightarrow f_{CP}} \sim e^{-\Gamma(1+y_{CP})t}$ , with  $y_{CP} = \tau_{K^-\pi^+}/\tau_{h^+h^-} - 1 = y \cos \phi$ , where  $\phi$  is the *CPV* phase arising from the mixing. Belle experiment, using  $540 \text{ fb}^{-1}$  of data corresponding to  $1.22 \times 10^6$ ,  $49 \times 10^3$  and  $111 \times 10^3$  signal events for  $K^-\pi^+$ ,  $\pi^+\pi^-$ ,  $K^+K^-$  final states, respectively, has measured  $y_{CP} = (1.31 \pm 0.32(\text{stat.}) \pm 0.25(\text{syst.}))\%$ . This value excludes the no-mixing hypothesis ( $y_{CP} = 0$ ) with a significance of  $3.2\sigma$ . Compatible results using the same decay modes were found by the BaBar collaboration [11].

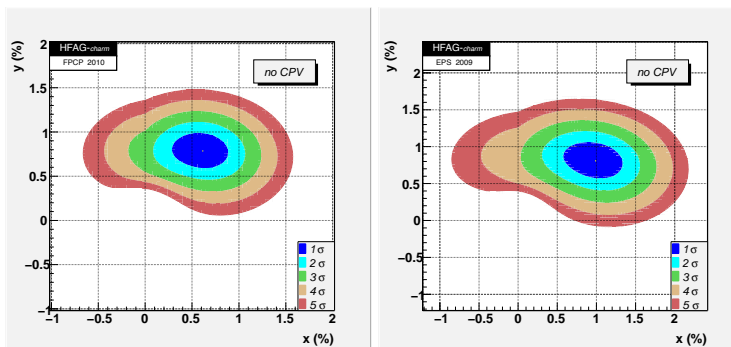
A recent BaBar analysis [13], using an "untagged" sample, has measured  $y_{CP} = (1.12 \pm 0.26(\text{stat.}) \pm 0.22(\text{syst.}))\%$ . In this analysis, since the initial flavor of the decaying  $D^0$  is not identified, no  $D^{*+}$  reconstruction is required, increasing significantly the reconstruction efficiency but increasing also the amount of background. The combination of the statistically independent samples, tagged and untagged, leads to  $y_{CP} = (1.16 \pm 0.22(\text{stat.}) \pm 0.18(\text{syst.}))\%$ , excluding the no-mixing hypothesis at  $4.1\sigma$ .

**$D^0$  3-body decays.** The methods described above provide compelling evidence of mixing in the charm sector, however, these methods are not able to give a direct measurement of  $x$  and  $y$ . The Dalitz-plot analysis of the  $D^0 \rightarrow K_S^0 h^+ h^-$  allows to extract mixing information from the rich dynamics of the 3-body decay and its evolution in time. For instance, the  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  Dalitz-plot contains CF and DCS resonances ( $K^*(892)^\pm$ ), the interference among them, and also contains *CP* eigenstates ( $\rho(770)$ ). This can be understood as the combination of the methods explained above. In this case the initial state amplitudes are function of the Dalitz-plot position,  $A_f = A_f(s_+, s_-)$ , with  $s_\pm = m^2(K_S^0 h^\pm)$  the 2-particle squared invariant mass. These amplitudes for  $D^0$  and  $\bar{D}^0$  fall into the same Dalitz-plot if we assume *CP* conserved in the decay ( $A(s_+, s_-) = \bar{A}(s_-, s_+)$ ). Here, the time-dependent decay in the small mixing limit can be written as

$$\Gamma_{D^0 \rightarrow f_{K_S^0 h^+ h^-}}(t) \sim e^{-\Gamma t} \left\{ R_D + y' \sqrt{R_D} (\Gamma t) + \frac{x'^2 + y'^2 + R_D (y'^2 - x'^2)}{4} (\Gamma t)^2 \right\}. \quad (2.2)$$

Lets recall the expresion  $y' = -x \sin \delta_f + y \cos \delta_f$ , with  $\delta_f$  been now the relative strong phase in each point of the Dalitz-plot. A model for the dependance with the Dalitz-plot will allow us to deconvolve  $y'$  and  $x'$ , and measure  $x$  and  $y$ . Nowadays, this is the only way to access direct and unambiguously to the mixing parameters. Using a  $468.5 \text{ fb}^{-1}$  data sample, BaBar collaboration performed a combined  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  and  $D^0 \rightarrow K_S^0 K^+ K^-$  time-dependent Dalitz-plot fit in the  $\{m_{D^0}, \Delta m\}$  signal box, assuming no *CPV* ( $\phi = 0$  and  $|q/p| = 1$ ), to extract the mixing parameters  $x$  and  $y$  [16]. The Dalitz-plot model uses a  $K$ -matrix approach to describe the  $S$ -wave and Breit-Wigner lineshapes for the  $P$ - and  $D$ - waves, as described in [17]. The purity of the data sample exceeds 98%, and  $541 \times 10^3$  ( $80 \times 10^3$ ) signal events were found in  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  ( $D^0 \rightarrow K_S^0 K^+ K^-$ ). The fit results are  $x = (0.16 \pm 0.23(\text{stat.}) \pm 0.12(\text{syst.}) \pm 0.08(\text{model.}))\%$ , and  $y = (0.57 \pm 0.20(\text{stat.}) \pm 0.13(\text{syst.}) \pm 0.07(\text{model.}))\%$ , with a correlation of the order of the percent. This result is the most precise single measurement of the mixing parameters and exclude the no-mixing hypothesis at  $1.9\sigma$ . This measurement favors small values for mixing, and  $|x| < |y|$  places the measure within the expected SM ranges. This measure is compatible with previous measurements using the  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  decay mode [18].

$D^0 - \bar{D}^0$  **mixing world Average.** The combination of all measurements of the mixing parameters (those described in this document and additional 3-body and semileptonic decay modes [19] with less sensitivity to mixing) by the HFAG [4], gives  $x = (0.61^{+0.19}_{-0.20})\%$  and  $y = (0.79 \pm 0.13)\%$ , shown in Fig. 1 (Left), excluding the no-mixing hypothesis at more than  $10\sigma$ . The effect of the new BaBar Dalitz-plot measurement can be observed comparing with Fig. 1 (Right), which corresponds to the previous HFAG average. It is clear how this measurement drifts the average towards SM values, specially for  $x$  where the uncertainty is largely reduced.



**Figure 1:** (Left) New HFAG [4] world average contour plot for the mixing parameters  $x$  and  $y$  including the new time-dependent Dalitz-plot analysis from BaBar [16]. (Right) Previous HFAG average.

**CP violation in the charm sector.** From the experimental point of view, the construction of  $CP$  asymmetries including all  $CPV$  sources, is the simplest way to study  $CPV$ . In the  $B$ -factories, time-integrated searches have been performed in the singly-Cabibbo-suppressed (SCS) final states  $D^0 \rightarrow h^+h^-$  [20] and  $D^0 \rightarrow \pi^0 h^+h^-$  [21], where Dalitz-plot integrated asymmetries were also studied. No evidence of  $CPV$  was found with a statistical resolution of  $\sim 0.3\%$ .

Recently, BaBar experiment performed an analysis in which a  $T$ -violating asymmetry is measured [22]. Assuming  $CPT$  a well conserved symmetry, then a test for  $T$ -violation will represent also a test for  $CPV$ . With the momentum in the  $D^0$  rest frame of the final state particles in the reaction  $D^0 \rightarrow K^+K^-\pi^+\pi^-$ , a  $T$ -odd triple product such as  $C_T \equiv \vec{p}_{K^+} \cdot (\vec{p}_{\pi^+} \times \vec{p}_{\pi^-})$  ( $\bar{C}_T$  for the  $\bar{D}^0$  decays) is built. Strong interaction dynamics in the decay may produce non-vanishing asymmetries,

$$A_T \equiv \frac{\Gamma(C_T > 0) - \Gamma(C_T < 0)}{\Gamma(C_T > 0) + \Gamma(C_T < 0)}, \quad \bar{A}_T \equiv \frac{\Gamma(-\bar{C}_T > 0) - \Gamma(-\bar{C}_T < 0)}{\Gamma(-\bar{C}_T > 0) + \Gamma(-\bar{C}_T < 0)}, \quad (2.3)$$

and from here, the true  $T$ -violating asymmetry as  $\mathcal{A}_T = (A_T - \bar{A}_T)/2$ . In the signal region a fit was performed over  $50 \times 10^3$  signal events, obtaining  $\mathcal{A}_T = (0.10 \pm 0.51(\text{stat.}) \pm 0.44(\text{syst.}))\%$ , where the systematic uncertainty is dominated by the particle identification. This measurement improves the statistical resolution in one order of magnitude with respect to the previous measurement [23], however, no sign of  $T$ -violation was found.

### 3. Conclusions

New measurements at the  $B$ -factories have provided a best understanding of the physics in the

charm sector. We have shown recent results from the BaBar experiment on the measurement of the  $f_{D_s}$  decay constant, as well as crucial results on the  $D^0 - \bar{D}^0$  mixing using a time-dependent Dalitz-plot analysis and an improvement on the search for  $T$ -violation in multibody  $D^0$  decays.

## References

- [1] B. Aubert *et al.* [BABAR Collaboration], Nucl. Instrum. Meth. A **479**, 1 (2002); [Belle Collaboration] Nucl. Instrum. Meth. A **479**, 117 (2002).
- [2] E. Follana, C. T. H. Davies, G. P. Lepage and J. Shigemitsu [HPQCD Collaboration and UKQCD Collaboration], Phys. Rev. Lett. **100**, 062002 (2008).
- [3] P. d. A. Sanchez *et al.* [The BABAR Collaboration], arXiv:1003.3063 [hep-ex].
- [4] [HFAG Collaboration], <http://www.slac.stanford.edu/xorg/hfag/charm/index.html>
- [5] K. Lande, E. T. Booth, J. Impeduglia, L. M. Lederman, and W. Chinowsky, Phys. Rev. **103**, 1901 (1956); W. F. Fry, J. Schneps, and M. S. Swami, Phys. Rev. **103**, 1904 (1956).
- [6] H. Albrecht *et al.* (ARGUS Collaboration), Phys. Lett. B **192**, 245 (1987); C. Albajar *et al.* (UA1 Collaboration), Phys. Lett. B **186**, 247 (1987).
- [7] A. Abulencia *et al.* (CDF Collaboration), Phys. Rev. Lett. **97**, 242003 (2006); V. M. Abazov *et al.* (D0 Collaboration), Phys. Rev. Lett. **97**, 021802 (2006).
- [8] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. Lett. **98**, 211802 (2007).
- [9] M. Staric *et al.* [Belle Collaboration], Phys. Rev. Lett. **98**, 211803 (2007).
- [10] T. Aaltonen *et al.* [CDF Collaboration], Phys. Rev. Lett. **100** 121802 (2008).
- [11] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. D **78**, 011105 (2008).
- [12] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. Lett. **103**, 211801 (2009).
- [13] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. D **80**, 071103 (2009).
- [14] H. N. Nelson, in *Proc. of the 19th Intl. Symp. on Photon and Lepton Interactions at High Energy LP99* ed. J.A. Jaros and M.E. Peskin.
- [15] L. M. Zhang *et al.* [BELLE Collaboration], Phys. Rev. Lett. **96**, 151801 (2006).
- [16] P. del Amo Sanchez *et al.* [The BABAR Collaboration], arXiv:1004.5053 [hep-ex].
- [17] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. D **78**, 034023 (2008).
- [18] D. M. Asner *et al.* [CLEO Collaboration], Phys. Rev. D **72**, 012001 (2005). K. Abe *et al.* [BELLE Collaboration], Phys. Rev. Lett. **99**, 131803 (2007).
- [19] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. D **76**, 014018 (2007). U. Bitenc *et al.* [BELLE Collaboration], Phys. Rev. D **77**, 112003 (2008). A. Zupanc *et al.* [Belle Collaboration], Phys. Rev. D **80**, 052006 (2009).
- [20] B. Aubert *et al.* [BaBar Collaboration], Phys. Rev. Lett. **100**, 061803 (2008). M. Staric *et al.* [Belle Collaboration], Phys. Lett. B **670**, 190 (2008).
- [21] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. D **78**, 051102 (2008). K. Arinstein [Belle Collaboration], Phys. Lett. B **662**, 102 (2008).
- [22] P. d. A. Sanchez *et al.* [The BABAR Collaboration], arXiv:1003.3397 [hep-ex].
- [23] J. M. Link *et al.* [FOCUS Collaboration], Phys. Lett. B **634**, 165 (2006).