Graviton decay to 2 photons at the LHC

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Standard Model production of $\gamma\gamma$ has been studied theoretically at hadron colliders by Balázs et al. [1] by developing the program RESBOS that computes the fully differential cross section typically in NLO QCD and at NLL resummation of initial state radiation. In collaboration with P. Nadolsky, our goal is to add to RESBOS the effect of an intermediate massive spin 2 particle $B$, coupling to the energy momentum tensor, produced via the Drell-Yan process in $pp \to B \to \gamma\gamma X$. This will help provide a model-independent spin determination of any new boson discovered at the LHC, since the $\gamma\gamma$ decay channel, though usually rare, is clean and shows pronounced angular variation. This note note presents the motivation and framework.

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\footnote{In collaboration with Pavel Nadolsky}
1. Angular Variation

The center-edge asymmetry $\sigma_{CE}$ was used by Osland et al. [2] to quantify angular variation in the cross-section $\sigma(R_{ll})$ for pp $\rightarrow$ B $\rightarrow$ ll X Drell-Yan dilepton production

$$\sigma_{CE} \equiv \left[ \int_{z_{cut}}^{z^*} \left( \int_{z_{cut}}^{z^*} + \int_{z_{cut}}^{z^*} \right) \right] \frac{d\sigma(R_{ll})}{dz} \, dz.$$  

Here, $z = \cos \theta^*$, where $\theta^*$ is the polar angle of the dileptons in the rest frame of intermediate boson B, and $z_{cut}$ is the limit of experimental acceptance. To get a rough idea, assuming no cuts or Standard Model background, and using only gluon fusion in LO QCD to produce B, we find the following comparison of angular variation for ll and $\gamma\gamma$ final states:

The (light) gray curves are for spin-2 B decaying to (ll) $\gamma\gamma$. The isotropic decay of a scalar B is shown in black for reference. We see that the angular variation is more pronounced in $\gamma\gamma$, making it easier to distinguish tensor from scalar. Moreover, a vector B does not decay to $\gamma\gamma$, but does go to ll. For most collision energies and models, $\sigma(R_{ll})$ is significantly larger than $\sigma(R_{\gamma\gamma})$, but the backgrounds are larger and identification more troublesome for the former.

1.1 Helicity decomposition

To include cuts, Standard Model backrounds, and the full PDFs, at NLO QCD and NLL resummation for $\sigma(R_{ll})$, work is in progress to modify RESBOS. Consider the transition matrix element squared for di-photon production summed over final photon polarizations $\sigma = \{-1,0,1\}$,

$$\sum_{\sigma,\sigma'} |H_{\mu\nu} \Delta^{\sigma\sigma'} P_{\sigma'\sigma} |^2.$$  

$H_{\mu\nu}$ and $P_{\sigma'\sigma}$ are hadron and photon tensors, $\Delta^{\sigma\sigma'} = i B^{\sigma\sigma'} (q^2 - M^2)^{-1}$ is the spin-2 B propagator for momentum $q$ and mass $M$. For proton momenta $p_1, p_2$, photon momenta $k_1, k_2$, with $k = k_1 - k_2$,

$$H_{\mu\nu} H_{\mu'\nu'} = \int d^4 x e^{i q \cdot x} < p_1 p_2 | T_{\mu\nu}(x) T_{\mu'\nu'}(0) | p_1 p_2 > , \quad B_{\mu\nu}^{\sigma\sigma'} = \frac{1}{2} (g_{\mu\nu} g_{\sigma\sigma'} + g_{\mu\sigma'} g_{\nu\sigma}) + ... ,$$
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\[ 4 \sum_{\sigma, \sigma'} P^{\sigma \sigma'}_{a\mu'} P^{\sigma' \sigma}_{a'\mu} = q^4 \left( g_{aa'} g_{\mu\mu'} - \frac{1}{2} \eta_{\mu\mu'} g_{a a'} \right) + 2 q^2 \left( \eta_{\mu} \eta_{\mu'} k_{\mu} k_{\mu'} - q_a q_{a'} \right) - \frac{1}{2} q^2 \left( g_{\mu\mu'} k_a k_{\mu'} + g_{a a'} k_{\mu} k_{\mu'} \right) + \frac{1}{2} \left( k_{\mu} k_{\mu'} q_a q_{a'} + k_{\mu} k_{\mu'} q_a q_{a'} \right) - 2 \left( k_{\mu} k_{\mu'} q_a q_{a'} + \frac{1}{2} (k_{\mu} k_{\mu'} q_a q_{a'} + q_a q_{a'} q_{\beta} q_{\beta'}) + S \right) \]

We neglected terms in B that do not contribute to \(|HBP|^2\) for on-shell photons. \(S\) adds the \(\alpha \leftrightarrow \beta\) and/or \(\alpha' \leftrightarrow \beta'\) expressions. The framework of RESBOS uses a helicity decomposition and factorization possible in the case of an irreducible intermediate state. We have the completeness condition \(B_{\mu\nu} a\beta = \Sigma_\epsilon \epsilon_{\mu\nu} \epsilon_{a\beta} \epsilon^* \), where \(\epsilon_{\mu\nu}\) are the traceless, transverse, orthogonal spin 2 polarization tensors, and \(s\) are the polarizations \(-2,-1,0,1,2\) of spin 2. We can then write

\[ (q^2 - M^2) \sum_{\sigma, \sigma'} |H^{\mu\nu}_{a\beta} P^{\sigma \sigma'}_{a\mu'}|^2 = \sum_{s, s'} H_{(s,s')} P_{(s,s')} \]

where

\[ H_{(s,s')} = H^0 P^{\mu\nu}_{a\beta} \epsilon_{\mu\nu} \epsilon_{a\beta} \epsilon^* , \quad P_{(s,s')} = \sum_{\sigma, \sigma'} P^{\sigma \sigma'}_{a\mu'} P^{\sigma' \sigma}_{a'\mu} \epsilon_{a\beta} \epsilon^* \epsilon_{a\beta} \epsilon^* \]

\(H_{(s,s')}\) are computed by subroutines in RESBOS at the parton level to include resummation effects, NLO QCD corrections and PDFs. They depend only upon \(q\), transverse momentum \(q_T\) and rapidity \(y\) of B. Symmetries under \(s \leftrightarrow -s\) and \(s \leftrightarrow s'\) imply that nine of the twenty-five \(P_{(s,s')}\) are independent. They may be parameterized by the following (non-unique) angular functions

\[
\begin{align*}
    P_{(2,2)} &= \frac{1}{4} q^4 \left[ \sin^4 \theta' \right] \exp i4\phi^* \\
    P_{(1,2)} &= \frac{1}{2} q^4 \left[ \sin^3 \theta' \cos \theta' \right] \exp i3\phi^* \\
    P_{(1,1)} &= q^4 \left[ \sin^4 \theta' \right] \exp i2\phi^* \\
    P_{(0,2)} &= -q^4 (\frac{1}{2\sqrt{6}} (\sin^2 \theta' + \sin^2 \theta' \cos^2 \theta') \exp i2\phi^* \\
    P_{(1,2)} &= \frac{1}{2} q^4 (4 \left[ \sin^2 \theta' \cos \theta' \right] - \left[ \sin^4 \theta' \cos \theta' \right] \exp i3\phi^* \\
    P_{(0,1)} &= (2q^4/\sqrt{6}) (3[\sin \theta' \cos \theta'] - [\sin^3 \theta' \cos \theta'] \exp i2\phi^* \\
    P_{(2,2)} &= \frac{1}{4} q^4 (8 \left[ \cos^2 \theta' \right] + [\sin^4 \theta'] ) \\
    P_{(1,1)} &= q^4 \left[ \sin^2 \theta' \right] + [\sin^2 \theta' \cos^2 \theta' ] \\
    P_{(0,0)} &= (q^4/6) (16 - 7 \left[ \sin^2 \theta' \right] - [\sin^2 \theta' \cos^2 \theta'] )
\end{align*}
\]

The imaginary parts cancel in \(|HBP|^2\) once the sum over \((s, s')\) is done.

References
