

## Renormalization of the baryon axial vector current in large- $N_c$

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The baryon axial vector current is computed at one-loop order in heavy baryon chiral perturbation theory in the large- $N_c$  limit, where  $N_c$  is the number of colors. Loop graphs with octet and decuplet intermediate states cancel to various orders in  $N_c$  as a consequence of the large- $N_c$  spin-flavor symmetry of QCD baryons. We present a preliminary study of the convergence of the chiral expansion with  $1/N_c$  corrections. The physical values  $N_f = 3$  (where  $N_f$  is the number of light quark flavors) and  $N_c = 3$  are used in the case of  $g_A$  in QCD.

*35th International Conference of High Energy Physics - ICHEP2010,  
July 22-28, 2010  
Paris France*

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<sup>†</sup>The author would like to express their gratitude to Local Organizing Committee of the 35th International Conference of High Energy Physics also acknowledge support.

## 1. Renormalization of the baryon axial vector current

The QCD operators have well-defined  $1/N_c$  expansions. For the baryon axial vector current  $A^{kc}$  its  $1/N_c$  expansion can be written as

$$A^{kc} = a_1 G^{kc} + \sum_{n=2,3}^{N_c} b_n \frac{1}{N_c^{n-1}} \mathcal{D}_n^{kc} + \sum_{3,5}^{N_c} c_n \frac{1}{N_c^{n-1}} \mathcal{O}_n^{kc}, \quad (1.1)$$

The correction containing the full dependence on the ratio  $\Delta/m_\Pi$ , where  $\Delta \equiv M_\Delta - M_N$  is the decuplet-octet mass difference and  $m_\Pi$  is the meson mass. Was derived in Ref. [1] and reads

$$\begin{aligned} \delta A^{kc} = & \frac{1}{2} [A^{ja}, [A^{jb}, A^{kc}]] \Pi_{(1)}^{ab} - \frac{1}{2} \left\{ A^{ja}, [A^{kc}, [\mathcal{M}, A^{jb}]] \right\} \Pi_{(2)}^{ab} \\ & + \frac{1}{6} \left( [A^{ja}, [[\mathcal{M}, [\mathcal{M}, A^{jb}]], A^{kc}]] - \frac{1}{2} [[\mathcal{M}, A^{ja}], [[\mathcal{M}, A^{jb}], A^{kc}]] \right) \Pi_{(3)}^{ab} + \dots \end{aligned}$$

Here  $\Pi_{(n)}^{ab}$  is a symmetric tensor which contains meson-loop integrals with the exchange of a single meson: A meson of flavor  $a$  is emitted and a meson of flavor  $b$  is reabsorbed.  $\Pi_{(n)}^{ab}$  decomposes into flavor singlet, flavor **8** and flavor **27** representations [2].

## 2. Results and Conclusions

We have computed the renormalization of the baryon axial vector current in the framework of heavy baryon chiral perturbation theory in the large- $N_c$  limit. The matrix elements of the space components of  $A^{kc}$  between  $SU(6)$  symmetric states give the actual values of the axial vector couplings. For  $N_c = 3$  and  $N_f = 3$  the couplings  $g_A$  of baryons with corrections at relative orders  $N_c$ ,  $1/N_c$ ,  $1/N_c^2$  and  $1/N_c^3$  for flavor singlet contribution are shown in Table 1.

Process	Singlet				Total
	$\mathcal{O}N_c$	$\mathcal{O}(1/N_c)$	$\mathcal{O}(1/N_c^2)$	$\mathcal{O}(1/N_c^3)$	
$n \rightarrow pe^- \bar{\nu}_e$	1.271	-0.1138	0.1402	-0.0256	1.272
$\Sigma^+ \rightarrow \Lambda e^+ \nu_e$	0.615	-0.0396	0.0663	0.0111	0.653
$\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e$	0.598	-0.0266	0.0446	0.0074	0.624
$\Lambda \rightarrow pe^- \bar{\nu}_e$	-0.941	0.0837	-0.0855	0.0389	-0.904
$\Sigma^- \rightarrow ne^- \bar{\nu}_e$	0.330	0.0014	0.0188	0.0239	0.375
$\Xi^- \rightarrow \Lambda e^- \bar{\nu}_e$	0.212	-0.0423	0.0179	-0.0483	0.139
$\Xi^- \rightarrow \Sigma^0 e^- \bar{\nu}_e$	0.868	-0.0522	0.0643	-0.0117	0.869
$\Xi^0 \rightarrow \Sigma^+ e^- \bar{\nu}_e$	1.310	-0.0998	0.1231	-0.0225	1.312

**Table 1:** Corrections at relative order for the axial vector couplings of the baryons

## References

- [1] R. Flores-Mendieta, C. P. Hofmann, E. Jenkins, and A. V. Manohar, Phys. Rev. D **62**, 034001 (2000).
- [2] R. Flores-Mendieta, C. P. Hofmann, Phys. Rev. D **74**, 094001 (2006).