Search for the decays $B^+ \to D^+ K^{(*)0}$

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We report a search for the rare decays $B^+ \to D^+ K^0$ and $B^+ \to D^+ K^{*0}$ in an event sample of approximately 465 million $\bar{B}B$ pairs collected with the BaBar detector at the PEP-II asymmetric-energy $e^+e^-$ collider at SLAC. We find no significant evidence for either mode and we set 90% probability upper limits on the branching fractions of $BF(B^+ \to D^+ K^0) < 2.9 \times 10^{-6}$ and $BF(B^+ \to D^+ K^{*0}) < 3.0 \times 10^{-6}$ [1].
1. Introduction

Charged $B$ meson decays like $B^+ \to D^+ K^{(*)0}$ are dominated by weak annihilation diagrams, for which no reliable estimates for the decay rates exist because of soft gluons exchange. In particular annihilation amplitudes cannot be evaluated with the commonly-used factorization approach [2]. Such annihilation amplitudes are suppressed by $\lambda^5$ where $\lambda$ is the sine of the Cabibbo angle [2, 3]. So far, no pure annihilation hadronic diagram has been observed, and such amplitudes are usually neglected in the measurement of $V_{ub}$. Their branching fractions could be enhanced by so-called rescattering effects (see Fig. 1), up to $\lambda^4$ [3], rendering the rate comparable to the isospin-related $B^0 \to D^0 K^{(*)0}$ decay rate of approximately $5 \times 10^{-6}$.

None of the modes studied in this note has been observed so far, and a 90% confidence level upper limit on the branching fraction $\mathcal{B}(B^+ \to D^+ K^0) < 5 \times 10^{-6}$ has been established by $BaBar$ [4]. No study of $B^+ \to D^+ K^{(*)0}$ has previously been published. The results presented here are obtained with 426 fb$^{-1}$ of data collected at the $\Upsilon(4S)$ resonance with the $BaBar$ detector at the PEP-II asymmetric $e^+e^-$ collider [6] corresponding to $465 \times 10^6 B\bar{B}$ pairs ($N_{B\bar{B}}$). An additional 44.4 fb$^{-1}$ of data (“off-resonance”) collected at a center-of-mass (CM) energy 40 MeV below the $\Upsilon(4S)$ resonance is used to study backgrounds from $e^+ e^- \to q\bar{q} (q = u, d, s, or c)$ processes, which we refer to as continuum events. The $BaBar$ detector is described in detail elsewhere [7].

2. Event Reconstruction and Selection

The $D^+$ mesons are reconstructed in the modes $D^+ \to K^- \pi^+ \pi^+ (K\pi\pi)$, $D^+ \to K_S \pi^+ (K_S\pi)$, $D^+ \to K^- \pi^+ \pi^+ \pi^0 (K\pi\pi\pi^0)$ and $D^+ \to K_S \pi^+ \pi^0 (K_S\pi\pi^0)$ for the decay channels $B^+ \to D^+ K^0$ ($DK$). Only the first two modes are used for the $B^+ \to D^+ K^{(*)0}$ decay channel ($DK^*$). The event selections are optimized by maximizing $S/\sqrt{S+B}$, where $S$ and $B$ are the expected signal and background yields, using Monte Carlo (MC) simulations and off-resonance data. The signal branching fraction is taken to be $5 \times 10^{-6}$.

The charged kaons are required to satisfy kaon identification criteria obtained from the combination of information from the Cherenkov light and the tracking detectors. Kaons and pions must satisfy $p_K > 200$ MeV/$c$ and $p_{\pi} > 150$ MeV/$c$, where $p$ is the momentum in lab frame. The invariant mass of the $D^+$ candidates is required to stand within 10 to 22 MeV/$c^2$ (depending on the channel) of the nominal mass [8]. The $K_S$ candidates are reconstructed from $\pi^+ \pi^-$ pairs with invariant mass within 5 to 7 MeV/$c^2$ of the nominal $K_S$ mass [8]. We define $\alpha_{K_S}(B^+)$ as the angle between
the momentum vector of the $K_S$ candidate and the vector connecting the $B^+$ and $K_S$ decay vertices. The prompt $K_S$ candidates from the $B^+ \rightarrow D^+ K_S$ decay must fulfill $\ln(1 - \cos \alpha_{K_S}(B^+)) < -8$ and $\ln(1 - \cos \alpha_{K_S}(D^+)) < -6$, where $\alpha_{K_S}(D^+)$ is defined in a similar way. The $\pi^0$ candidates are reconstructed from photon pairs $\gamma\gamma$ with invariant mass $m(\gamma\gamma)$ within 10 to 12 MeV/c$^2$ of the nominal $\pi^0$ mass [8]. These pairs must satisfy $E(\gamma) > 70$ MeV, $E(\gamma\gamma) > 200$ MeV, $P_{CM}(\gamma\gamma) > 400$ MeV, where $E$ and $P_{CM}$ are respectively the energy and the momentum in the CM frame. The $K^{*0}$ candidates are reconstructed in $K^{*0} \rightarrow K^+ \pi^-$ with the invariant mass lying within 40 MeV/c$^2$ of the nominal $K^{*0}$ mass [8]. We define $\theta_H$ as the angle between the direction of flight of the charged $K$ and the direction of flight of the $B$ in the $K^{*0}$ rest frame, and require $|\cos \theta_H| > 0.5$. The $B^+$ candidates are reconstructed by combining one $D^+$ and one $K_S$ or $K^{*0}$ candidate, constraining them to originate from a common vertex. We define $\theta_B$ as the $B$ polar angle with respect to the beam axis in the CM frame, and require $|\cos \theta_B|$ to be smaller than 0.76 to 0.86 depending on the channels. Using the precise knowledge of the $e^+ e^-$ beams energies and the energy conservation in the two-body decay $\Upsilon(4S) \rightarrow B\overline{B}$, we define the beam-energy substituted mass $m_{ES}$ and the energy difference $\Delta E$:

$$m_{ES} \equiv \sqrt{\left(E_{CM}^2 / c^2 \right) / 2 - p_H^2}, \quad \Delta E \equiv E_B - E_{CM} / 2,$$

where $E$ and $p$ are energy and momentum. We retain candidates with $|\Delta E|$ value smaller than 19 to 25 MeV and $m_{ES}$ in the range [5.20, 5.29] GeV/c$^2$. Multiple $B$ candidates are eliminated with selections on $D^+$ mass or $\Delta E$ distribution. The dominant background comes from continuum events, characterized by a jet-like topology, which can be described with these variables defined in the CM: the cosine of the angle between the $B$ thrust axis and the thrust axis of all the other tracks and energy deposits of the event, where the thrust axis is defined as the direction that maximizes the sum of the longitudinal momenta of all the particles, the event shape moments $L_0 = \sum_i p_i$, and $L_2 = \sum_i p_i |\cos \theta_i|^2$, where the index $i$ runs over all tracks and energy deposits in the rest of the event; $p_i$ is the momentum and $\theta_i$ is the angle to the $B$ thrust axis. We also use $|\Delta t|$, the absolute value of the time interval between the two $B$ decays [5]. These four variables are combined in a Fisher discriminant $F$ [9], whose coefficients are determined with samples of simulated signal and continuum events, and validated using off-resonance data. For the $K\pi\pi$ mode, events are classified according to their flavor-tagging category [5] (lepton, kaon or other) and fitted simultaneously. The $B\overline{B}$ background is divided into two components according to their distribution in the signal region: non-peaking and peaking. The peaking backgrounds are rejected using the $K_S$ helicity angle $\theta_{K_S}$ with $|\cos(\theta_{K_S})| > 0.8$ or 0.9 depending on the channel. Based on MC studies, almost one $B\overline{B}$ peaking background event per mode is expected in the signal region. The charmless background is evaluated from data using the $D^+$ sidebands and found to be negligible.

3. Fit Procedure

The signal and background yields are extracted with an unbinned maximum likelihood fit of $m_{ES}$ and $F$, assuming from simulation studies the correlations between $m_{ES}$ and $F$ to be negligible. For $m_{ES}$ the signal is modeled with a Gaussian function, the continuum and non-peaking $B\overline{B}$ background are described by two ARGUS functions [10]: $A(x) = x \sqrt{1 - (x / x_0)^2} \cdot \exp(c(1 - (x / x_0)^2))$, where $x_0$ is the maximum value of $x$ and $c$ accounts for the shape of the distribution and are determined from data for the continuum. All other PDF parameters are derived from the simulated
events. The peaking $B\bar{B}$ background is modeled with a Crystal Ball function [11] which is a Gaussian modified to include a power-law tail. The peaking background yield is fixed from the PDG branching fractions [8]. The signal yield determined by the fit ($N_{sig}$) is used to calculate the branching fraction (BF): $BF = N_{sig} / (N_{B}\cdot \epsilon_{sig} \cdot BF_{sec})$, where $N_{B}$ is the total number of charged $B$ mesons in the data sample, $BF_{sec}$ is the BF is of the secondary decay channels of the $D$ and $K_S$, and $\epsilon_{sig}$ is the signal reconstruction efficiency measured in MC. The fit procedure is validated using toy MC studies and no biases of the fit model were found. The fit model was tested using full MC sample with and without signal events. The results of the fit to the data are reported in Table 1 for each $D$ channel. The background yields are close to the expectations and the errors obtained on the branching fractions are in good agreement with the values found with the toy study. The leading contribution is obtained from the $K\pi\pi$ mode. The Fig. 2 gives the fit projection for $m_{ES}$, after requiring $F > 0$, to visually enhance any possible signal.

<table>
<thead>
<tr>
<th>Decay mode</th>
<th>$N_{sig}$</th>
<th>$N_{B}\pi$</th>
<th>$N_{cont}$</th>
<th>BF</th>
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</thead>
<tbody>
<tr>
<td>$B^+ \rightarrow D^+ K^0$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$K\pi\pi$</td>
<td>$-11.9^{+6.7}_{-5.6}$</td>
<td>$70 \pm 27$</td>
<td>$2690 \pm 57$</td>
<td></td>
</tr>
<tr>
<td>$K\pi\pi\pi^0$</td>
<td>$10^{+10}_{-9}$</td>
<td>$111 \pm 51$</td>
<td>$6516 \pm 94$</td>
<td></td>
</tr>
<tr>
<td>$K_S\pi$</td>
<td>$0.6^{+3.3}_{-4.6}$</td>
<td>$20 \pm 14$</td>
<td>$381 \pm 23$</td>
<td></td>
</tr>
<tr>
<td>$K_S\pi\pi^0$</td>
<td>$-6.7^{+4.5}_{-2.8}$</td>
<td>$36 \pm 22$</td>
<td>$1270 \pm 41$</td>
<td></td>
</tr>
<tr>
<td>$B^+ \rightarrow D^+ K^{*0}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$K\pi\pi$</td>
<td>$-15.6^{+8.7}_{-7.1}$</td>
<td>$463 \pm 63$</td>
<td>$6338 \pm 98$</td>
<td></td>
</tr>
<tr>
<td>$K_S\pi$</td>
<td>$-11.4^{+7.5}_{-3.4}$</td>
<td>$35 \pm 15$</td>
<td>$547 \pm 27$</td>
<td></td>
</tr>
</tbody>
</table>

4. Systematic uncertainties

The uncertainties on the PDF parameterizations is evaluated by repeating the fit varying the MC-obtained PDF parameters within their statistical errors, taking into account correlations among the parameters. Differences between the data and MC for the signal PDF shapes are investigated using data control samples $B^0 \rightarrow D^+ \pi^-$ and $B^0 \rightarrow D^+ \rho^-$. The uncertainty on the continuum background shape is estimated using off-resonance data instead of continuum MC. The uncertainty on the PDF of the non-peaking $B\bar{B}$ background is measured by leaving its parameters free in the fit and taking the difference from the nominal fits as uncertainty. We also considered the uncertainty on signal efficiency due to limited MC statistics. Uncertainties on MC-data differences in tracking efficiency, $K_S$ and $\pi^0$ reconstruction and charged-kaon identification, are estimated by comparing data and simulation performance in control samples. The uncertainty on peaking background are estimated by repeating the fit varying the event yields within their statistical errors. The uncertainties on the branching fractions of the sub-decay modes are also taken into account. The uncertainty on $N_{B\pi}$ has a negligible effect on the total error. The uncertainties are included by convolving the individual fit likelihoods with Gaussians of width equal to the systematic uncertainty. The total systematic uncertainties on the BF are given in the Table 1 for each channel.
Figure 2: From top left to bottom right: \( m_{ES} \) projection with \( F > 0 \) for \( K\pi\pi, K\pi\pi\pi^0, K\pi\pi\pi^0 \) for \( B^+ \rightarrow D^+ K \) and \( K\pi\pi\pi^0 \) and \( K\pi\pi\pi^0 \) for \( B^+ \rightarrow D^+ K^{(*)0} \). Data are black dots with error bars, the different fit components are: signal (black curve), non-peaking \( B\bar{B} \) (green), continuum (magenta) and \( B\bar{B} \) peaking background (red) and the total pdf (blue).

5. Results for Branching Fractions

The individual likelihoods for each mode are finally combined to give the average BF’s, which are compatible with zero. We then quote an upper limits at 90\% probability using a Bayesian approach with a flat prior for the BF:

\[
BF(B^+ \rightarrow D^+ K^{(*)0}) < 2.9 \times 10^{-6}, \quad BF(B^+ \rightarrow D^+ K^{(*)0}) < 3.0 \times 10^{-6}.
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References