Bottomonium states

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Recent results on studies of bottomonium states at Belle are reported. The results are obtained with a 121.4 fb−1 data sample collected with the Belle detector in the vicinity of the Υ(5S) resonance at the KEKB asymmetric-energy e+e− collider.

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1. Introduction

Bottornium is the bound system of $b\bar{b}$ quarks and is considered an excellent laboratory to study Quantum Chromodynamics (QCD) at low energies. The system is approximately non-relativistic due to the large $b$ quark mass, and therefore the quark-antiquark QCD potential can be investigated via $b\bar{b}$ spectroscopy.

The spin-singlet states $h_b(nP)$ and $\eta_b(nS)$ alone provide information concerning the spin-spin (or hyperfine) interaction in bottomonium. Measurements of the $h_b(nP)$ masses provide unique access to the $P$-wave hyperfine splitting, the difference between the spin-weighted average mass of the $P$-wave triplet states ($\chi_b(nP)$ or $n^3P_J$) and that of the corresponding $h_b(nP)$, or $n^1P_J$. These splittings are predicted to be close to zero [1], and recent measurements of the $h_c(1P)$ mass validates this expectation for charmonium.

Recently, the CLEO Collaboration observed the process $e^+e^-\rightarrow h_c(1P)\pi^+\pi^-$ at a rate comparable to that for $e^+e^-\rightarrow J/\psi\pi^+\pi^-$ in data taken above open charm threshold [2]. Such a large rate was unexpected because the production of $h_c(1P)$ requires a $c$-quark spin-flip, while production of $J/\psi$ does not. Similarly, the Belle Collaboration observed anomalously high rates for $e^+e^-\rightarrow \Upsilon(nS)\pi^+\pi^-(n=1,2,3)$ at energies near the $\Upsilon(5S)$ mass [3]. Together, these observations motivated a more detailed study of bottomonium production at the $\Upsilon(5S)$ resonance.

We use a 121.4 fb$^{-1}$ data sample collected on or near the peak of the $\Upsilon(5S)$ resonance ($\sqrt{s}\sim 10.865$ GeV) with the Belle detector [4] at the KEKB asymmetric energy $e^+e^-$ collider [5].

2. Observation of $h_b(nP)$

Our hadronic event selection requires a reconstructed primary vertex consistent with the run-averaged interaction point, at least three high-quality charged tracks. The $\pi^+\pi^-$ candidates are pairs of well reconstructed, oppositely charged tracks that are identified as pions and are not consistent with being electrons. Continuum $e^+e^-\rightarrow q\bar{q}$ ($q=u,d,s,c$) background is suppressed by requiring the ratio of the second to zeroth Fox-Wolfram moments to satisfy $R_2 < 0.3$. More details can be found in Ref. [11].

We calculate missing mass defined as $M_{\text{miss}}(\pi^+\pi^-) \equiv \sqrt{(P_{\Upsilon(5S)} - P_{\pi^+\pi^-})^2}$, where $P_{\Upsilon(5S)}$ is the 4-momentum of the $\Upsilon(5S)$ determined from the beam momenta and $P_{\pi^+\pi^-}$ is the 4-momentum of the $\pi^+\pi^-$ system. The $M_{\text{miss}}(\pi^+\pi^-)$ spectrum is divided into three adjacent regions with boundaries at $M_{\text{miss}}(\pi^+\pi^-) = 9.3, 9.8, 10.1$ and 10.45 GeV/c$^2$ and fitted separately in each region. In the third region, prior to fitting, we perform bib-by-bin subtraction of the background associated with the $K_0^0 \rightarrow \pi^+\pi^-$ production. To fit the combinatorial background we use a 6th (7th) order Chebyshev polynomial function for the first two (third) region. The signal component of the fit includes all signals observed in the $\mu^+\mu^-\pi^+\pi^-$ data as well as those arising from $\pi^+\pi^-$ transitions to $h_b(nP)$ and $\Upsilon(1D)$. The peak positions of all signals are floated, except that for $\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$, which is poorly constrained by the fit. The $M_{\text{miss}}(\pi^+\pi^-)$ spectrum, after subtraction of all the background contributions along with the signal component of the fit function overlaid is shown in Fig. 1, where clear signals of both $h_b(1P)$ and $h_b(2P)$ are visible. The signal parameters are listed in Table 1. Statistical significance of all signals except that for the $\Upsilon(1D)$ exceeds 5$\sigma$.  

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**Figure 1:** The inclusive $M_{\text{miss}}(\pi^+\pi^-)$ spectrum with the combinatorial background and $K_S^0$ contribution subtracted (points with errors) and signal component of the fit function overlaid (smooth curve). The vertical lines indicate boundaries of the fit regions.

**Table 1:** The yield and mass determined from the fits to the $M_{\text{miss}}(\pi^+\pi^-)$ distributions.

<table>
<thead>
<tr>
<th></th>
<th>Yield, $10^3$</th>
<th>Mass, MeV/$c^2$</th>
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<tbody>
<tr>
<td>$\Upsilon(1S)$</td>
<td>105.2 ± 5.8 ± 3.0</td>
<td>9459.4 ± 0.5 ± 1.0</td>
</tr>
<tr>
<td>$h_b(1P)$</td>
<td>50.4 ± 7.8$^{+4.5}_{-9.1}$</td>
<td>9898.3 ± 1.1$^{+1.0}_{-1.1}$</td>
</tr>
<tr>
<td>$3S \rightarrow 1S$</td>
<td>56 ± 19</td>
<td>9973.01</td>
</tr>
<tr>
<td>$\Upsilon(2S)$</td>
<td>143.5 ± 8.7 ± 6.8</td>
<td>10022.3 ± 0.4 ± 1.0</td>
</tr>
<tr>
<td>$\Upsilon(1D)$</td>
<td>22.0 ± 7.8</td>
<td>10166.2 ± 2.6</td>
</tr>
<tr>
<td>$h_b(2P)$</td>
<td>84.4 ± 6.8$^{+23.}_{-10.}$</td>
<td>10259.8 ± 0.6$^{+1.4}_{-1.0}$</td>
</tr>
<tr>
<td>$2S \rightarrow 1S$</td>
<td>151.7 ± 9.7$^{+19.0}_{-20.}$</td>
<td>10304.6 ± 0.6 ± 1.0</td>
</tr>
<tr>
<td>$\Upsilon(3S)$</td>
<td>45.6 ± 5.2 ± 5.1</td>
<td>10356.7 ± 0.9 ± 1.1</td>
</tr>
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The measured masses of $h_b(1P)$ and $h_b(2P)$ are $M = (9898.3 ± 1.1^{+1.0}_{-1.1})$ MeV/$c^2$ and $M = (10259.8 ± 0.6^{+1.4}_{-1.0})$ MeV/$c^2$, respectively. Using the world average masses of the $X_{bJ}(nP)$ states, we determine the hyperfine splittings to be $\Delta M_{\text{HF}} = (+1.6 ± 1.5)$ MeV/$c^2$ and $(+0.5^{+1.0}_{-1.2})$ MeV/$c^2$, respectively, where statistical and systematic uncertainties are combined in quadrature.

We also measure the ratio of cross sections $R \equiv \frac{\sigma(h_b(nP)\pi^+\pi^-)}{\sigma(\Upsilon(2S)\pi^+\pi^-)}$. To determine the reconstruction efficiency we use the results of resonant structure studies reported below. We determine the ratio of cross sections to be $R = 0.46 ± 0.08^{+0.07}_{-0.12}$ for the $h_b(1P)$ and $R = 0.77 ± 0.08^{+0.22}_{-0.17}$ for the $h_b(2P)$. Hence $\Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^-$ and $\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$ proceed at similar rates, despite the fact that the production of $h_b(nP)$ requires a spin-flip of a $b$-quark.

### 3. Observation of $Z_b(10610)$ and $Z_b(10650)$

As it was mentioned above, the processes $\Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^-$, which require a heavy-
quark spin flip, are found to have rates that are comparable to those for the heavy-quark spin conserving transitions \( \Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^- \), where \( n = 1,2,3 \). These observations differ from \textit{apriori} theoretical expectations and strongly suggest that some exotic mechanisms are contributing to \( \Upsilon(5S) \) decays.

First we perform an amplitude analysis of three-body \( \Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^- \) decays. To reconstruct \( \Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^- \), \( \Upsilon(nS) \rightarrow \mu^+\mu^- \) candidates we select events with four charged tracks with zero net charge that are consistent with coming from the interaction point. Charged pion and muon candidates are required to be positively identified. Exclusively reconstructed events are selected by the requirement \(|M_{\text{miss}}(\pi^+\pi^-) - M(\mu^+\mu^-)| < 0.2 \text{ GeV}/c^2\). Candidate \( \Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^- \) events are selected by requiring \(|M_{\text{miss}}(\pi^+\pi^-) - m_{\Upsilon(nS)}| < 0.05 \text{ GeV}/c^2\), where \( m_{\Upsilon(nS)} \) is the mass of an \( \Upsilon(nS) \) state [7]. Sideband regions are defined as 0.05 GeV/c\(^2\) < \(|M_{\text{miss}}(\pi^+\pi^-) - m_{\Upsilon(nS)}| < 0.10 \text{ GeV}/c^2\). To remove background due to photon conversions in the innermost parts of the Belle detector we require \( M^2(\pi^+\pi^-) > 0.20/0.14/0.10 \text{ GeV}/c^2 \) for a final state with an \( \Upsilon(1S), \Upsilon(2S), \Upsilon(3S) \), respectively. More details can be found in Ref. [6].

Amplitude analyses are performed by means of unbinned maximum likelihood fits to two-dimensional \( M^2[\Upsilon(nS)\pi^+] \) vs. \( M^2[\Upsilon(nS)\pi^-] \) Dalitz distributions. The fractions of signal events in the signal region are determined from fits to the \( M_{\text{miss}}(\pi^+\pi^-) \) spectrum and are found to be 0.937 ± 0.015(stat.), 0.940 ± 0.007(stat.), 0.918 ± 0.010(stat.) for final states with \( \Upsilon(1S), \Upsilon(2S), \Upsilon(3S) \), respectively. The variation of reconstruction efficiency across the Dalitz plot is determined from a GEANT-based MC simulation. The distribution of background events is determined using sideband events and found to be uniform across the Dalitz plot.

Dalitz distributions of events in the \( \Upsilon(2S) \) sidebands and signal regions are shown in Figs. 2(a) and 2(b), respectively, where \( M(\Upsilon(nS)\pi)_{\text{max}} \) is the maximum invariant mass of the two \( \Upsilon(nS)\pi \) combinations. Two horizontal bands are evident in the \( \Upsilon(2S)\pi \) system near 112.6 GeV\(^2\)/c\(^4\) and 113.3 GeV\(^2\)/c\(^4\), where the distortion from straight lines is due to interference with other intermediate states, as demonstrated below. One-dimensional invariant mass projections for events in the
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Figure 3: Comparison of fit results (open histogram) with experimental data (points with error bars) for events in the $\Upsilon(2S)$ (top) and $\Upsilon(3S)$ (bottom) signal regions. The hatched histogram shows the background component.

$\Upsilon(nS)$ signal regions are shown in Fig. 3, where two peaks are observed in the $\Upsilon(nS)\pi$ system near 10.61 GeV/c$^2$ and 10.65 GeV/c$^2$. In the following we refer to these structures as $Z_b(10610)$ and $Z_b(10650)$, respectively.

We parametrize the $\Upsilon(5S) \to \Upsilon(nS)\pi^+\pi^-$ three-body decay amplitude by:

$$M = A_{Z_1} + A_{Z_2} + A_{f_0} + A_{f_2} + A_{nr},$$

where $A_{Z_1}$ and $A_{Z_2}$ are amplitudes to account for contributions from the $Z_b(10610)$ and $Z_b(10650)$, respectively. Here we assume that the dominant contributions come from amplitudes that preserve the orientation of the spin of the heavy quarkonium state and, thus, both pions in the cascade decay $\Upsilon(5S) \to Z_b\pi \to \Upsilon(nS)\pi^+\pi^-$ are emitted in an $S$-wave with respect to the heavy quarkonium system. An angular analysis support this assumption [8]. Consequently, we parametrize the observed $Z_b(10610)$ and $Z_b(10650)$ peaks with an $S$-wave Breit-Wigner function $BW(s, M, \Gamma) = \frac{\sqrt{s}M}{s-M^2-i\Gamma}$, where we do not consider possible $s$-dependence of the resonance width. To account for the possibility of $\Upsilon(5S)$ decay to both $Z_b^0\pi^-$ and $Z_b^+\pi^+$, the amplitudes $A_{Z_1}$ and $A_{Z_2}$ are symmetrized with respect to $\pi^+$ and $\pi^-$ transposition. Using isospin symmetry, the resulting amplitude is written as

$$A_{Z_k} = a_{Z_k} e^{i\delta_{Z_k}} (BW(s_1, M_k, \Gamma_k) + BW(s_2, M_k, \Gamma_k)),$$

where $A_{Z_1}$ and $A_{Z_2}$ are amplitudes to account for contributions from the $Z_b(10610)$ and $Z_b(10650)$, respectively.
respectively. We use a Breit-Wigner function to parametrize the \( f \) values determined from the analysis of \( B \) world average values [7]; the mass and the coupling constants of the \( f \) state are fixed at values determined from the analysis of \( B^+ \rightarrow K^+ \pi^+ \pi^-; M[f_0(980)] = 950 \text{ MeV}/c^2, g_{\pi\pi} = 0.23, g_{KK} = 0.73 \) [9].

Following suggestions in Ref. [10], the non-resonant amplitude \( A_{nr} \) is parametrized as \( A_{nr} = a_1^{nr} e^{i \delta_1^{nr}} + a_2^{nr} e^{i \delta_2^{nr}} s_3 \), where \( s_3 = M^2(\pi^+ \pi^-) \) (s3 is not an independent variable and can be expressed via \( s_1 \) and \( s_2 \) but we use it here for clarity), \( a_1^{nr}, a_2^{nr}, \delta_1^{nr} \) and \( \delta_2^{nr} \) are free parameters of the fit.

The logarithmic likelihood function \( \mathcal{L} \) is then constructed as

\[
\mathcal{L} = -2 \sum \log(f_{sig} S(s_1, s_2) + (1 - f_{sig}) B(s_1, s_2)),
\]

where \( S(s_1, s_2) \) is the density of signal events \( |M(s_1, s_2)|^2 \) convolved with the detector resolution function, \( B(s_1, s_2) \) describes the combinatorial background that is considered to be constant and \( f_{sig} \) is the fraction of signal events in the data sample. Both \( S(s_1, s_2) \) and \( B(s_1, s_2) \) are efficiency corrected.

Results of the fits to \( \Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^- \) signal events are shown in Fig. 3, where one-dimensional projections of the data and fits are compared. The combined statistical significance of the two peaks exceeds 10 \( \sigma \) for all tested models and for all \( \Upsilon(nS)\pi^+\pi^- \) channels.

To study the resonant substructure of the \( \Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^- (m = 1, 2) \) three-body decays we measure their yield as a function of the \( h_b(1P)\pi^\pm \) invariant mass. The decays are reconstructed inclusively using missing mass of the \( \pi^+ \pi^- \) pair, \( M_{\text{miss}}(\pi^+\pi^-) \). We fit the \( M_{\text{miss}}(\pi^+\pi^-) \) spectra in bins of \( h_b(1P)\pi^\pm \) invariant mass, defined as the missing mass of the opposite sign pion, \( M_{\text{miss}}(\pi^\mp) \). We combine the \( M_{\text{miss}}(\pi^+\pi^-) \) spectra for the corresponding \( M_{\text{miss}}(\pi^+) \) and \( M_{\text{miss}}(\pi^-) \) bins and we use half of the available \( M_{\text{miss}}(\pi) \) range to avoid double counting.
The fit function is a sum of peaking components due to dipion transitions and combinatorial background as described Section 2. The positions of all peaking components are fixed to the values measured from the fit to the overall \(M(\pi^+ \pi^-)\) spectrum (see Table 1).

Since the \(\Upsilon(3S) \to \Upsilon(1S)\) reflection is not well constrained by the fits, we determine its normalization relative to the \(\Upsilon(5S) \to \Upsilon(2S)\) signal from the exclusive \(\mu^+ \mu^- \pi^+ \pi^-\) data for every \(M_{\text{miss}}(\pi^+ \pi^-)\) bin. In case of the \(h_b(2P)\) we use the range of \(M_{\text{miss}}(\pi^+ \pi^-) < 10.34\,\text{GeV}/c^2\), to exclude the region of the \(K^0_S \to \pi^+ \pi^-\) reflection. The peaking components include the \(\Upsilon(5S) \to h_b(2P)\) signal and a \(\Upsilon(2S) \to \Upsilon(1S)\) reflection.

The results for the yield of \(\Upsilon(5S) \to h_b(nP)\pi^+ \pi^- (m = 1, 2)\) decays as a function of the \(M_{\text{miss}}(\pi)\) are shown in Fig. 4. The distribution for the \(h_b(1P)\) exhibits a clear two-peak structure without a significant non-resonant contribution. The distribution for the \(h_b(2P)\) is consistent with the above picture, though the available phase-space is much smaller. We associate the two peaks with the production of the \(Z_b(10610)\) and \(Z_b(10650)\). To fit the \(M_{\text{miss}}(\pi)\) spectrum we use the following combination:

\[
|BW_1(s,M_1,\Gamma_1) + ae^{i\phi}BW_1(s,M_2,\Gamma_2) + be^{i\psi}|^2 \frac{qP}{\sqrt{s}}, \tag{3.4}
\]

Here \(\sqrt{s} \equiv M_{\text{miss}}(\pi)\); the variables \(M_k, \Gamma_k (k = 1, 2)\), \(a, \phi, b, \) and \(\psi\) are free parameters; \(\frac{qP}{\sqrt{s}}\) is a phase-space factor, where \(p (q)\) is the momentum of the pion originating from the \(\Upsilon(5S) (Z_b)\) decay measured in the rest frame of the corresponding mother particle. The \(P\)-wave Breit-Wigner amplitude is expressed as \(BW_1(s,M,\Gamma) = \frac{\sqrt{MTF(q/q_0)}}{M - s - iMT}\). Here \(F\) is the \(P\)-wave Blatt-Weisskopf form factor \(F = \frac{1}{\sqrt{1 + (q_0 R)^2}}, q_0\) is a daughter momentum calculated with pole mass of its mother, \(R = 1.6\,\text{GeV}^{-1}\). The function (Eq. 3.4) is convolved with the detector resolution function, integrated over the histogram bin and corrected for the reconstruction efficiency. The fit results are shown as solid histograms in Fig. 4. We find that the non-resonant contribution is consistent with zero in accord with the expectation that it is suppressed due to heavy quark spin-flip. In case of the \(h_b(2P)\) we fix the non-resonant amplitude at zero.

4. Evidence for the \(\eta_b(2S)\) and observation of \(h_b(1,2P) \to \eta_b(1S)\gamma\)

We study the processes \(e^+e^- \to \Upsilon(5S) \to h_b(nP)\pi^+ \pi^-\), \(h_b(nP) \to \eta_b(mS)\gamma\). We reconstruct only the \(\pi^+, \pi^-\) and \(\gamma\). The two-dimensional distribution \(M_{\text{miss}}^{(n)}(\pi^+ \pi^- \gamma) = M_{\text{miss}}(\pi^+ \pi^-) - M_{\text{miss}}(\pi^+ \pi^-) + m_{\eta_b(nP)}\) vs. \(M_{\text{miss}}(\pi^+ \pi^-)\) contains a signal cluster at the location of two crossing bands. A band at \(M_{\text{miss}}(\pi^+ \pi^-) = m_{\eta_b(nP)}\) is due to the \(\pi^+ \pi^-\) from the \(\Upsilon(5S) \to h_b(nP)\pi^+ \pi^-\) process and a random \(\gamma\); a band at \(M_{\text{miss}}^{(n)}(\pi^+ \pi^- \gamma) = m_{\eta_b(mS)}\) is due to the \(\gamma\). We fit the \(M_{\text{miss}}(\pi^+ \pi^-)\) spectra for different \(M_{\text{miss}}^{(n)}(\pi^+ \pi^- \gamma)\) bins to measure the \(h_b(nP)\) yield. The \(h_b(nP)\) yield peaks at \(M_{\text{miss}}^{(n)}(\pi^+ \pi^- \gamma)\) values corresponding to \(m_{\eta_b(mS)}\) due to the \(h_b(nP) \to \eta_b(mS)\gamma\) transitions.

The selection criteria is described in Ref. [11].

We fit the \(M_{\text{miss}}(\pi^+ \pi^-)\) spectrum in the \(h_b(1P)\) and \(h_b(2P)\) regions, defined as 9.8 GeV/c\(^2\) – 10.1 GeV/c\(^2\) and 10.1 GeV/c\(^2\) – 10.4 GeV/c\(^2\), respectively, with a fit function that is the sum of peaking components and a combinatorial background [11]. We find event yields for the \(\Upsilon(5S) \to h_b(nP)\) transitions of \(N_{SS-1P} = (70.3 \pm 3.3^{+1.9}_{-0.7}) \times 10^3\) and \(N_{SS-2P} = (89.5 \pm 6.1^{+0.0}_{-5.8}) \times 10^3\).
For hyperfine splittings \( \sum_{j=0}^{2} \frac{2j+1}{2} m_{\chi_{0j}(nP)} - m_{b_{0j}(nP)} \), we find \( \Delta M_{\text{HF}}(1P) = (+0.8 \pm 1.1) \text{ MeV}/c^2 \) and \( \Delta M_{\text{HF}}(2P) = (+0.5 \pm 1.2) \text{ MeV}/c^2 \), where statistical and systematic uncertainties in mass are added in quadrature.

We fit the \( M_{\text{miss}}(\pi^+\pi^-) \) spectra for each \( M_{\text{miss}}^{(i)}(\pi^+\pi^-) \) bin. From a generic MC simulation, we find that the \( K_0^0 \to \pi^+\pi^- \) contribution is independent of the \( M_{\text{miss}}^{(2)}(\pi^+\pi^-\gamma) \) value in the \( \eta_b(1S) \) region; in the \( \eta_b(2S) \) region, we restrict the \( M_{\text{miss}}(\pi^+\pi^-) \) fit range to 10.10 GeV/c\(^2\) – 10.34 GeV/c\(^2\), thereby avoiding the sharp rise in the \( K_0^0 \to \pi^+\pi^- \) contribution that occurs at 10.37 GeV/c\(^2\). The results for the \( h_b(1P) \) and \( h_b(2P) \) yields as a function of \( M_{\text{miss}}^{(i)}(\pi^+\pi^-\gamma) \) are presented in Fig. 5. Clear peaks at 9.4 GeV/c\(^2\) and 10.0 GeV/c\(^2\) are identified as signals for the \( \eta_b(1S) \) and \( \eta_b(2S) \), respectively. Generic MC simulations indicate that no peaking backgrounds are expected in these spectra.

**Figure 5:** The \( h_b(1P) \) yield vs. \( M_{\text{miss}}^{(1)}(\pi^+\pi^-\gamma) \) (a), and \( h_b(2P) \) yield vs. \( M_{\text{miss}}^{(2)}(\pi^+\pi^-\gamma) \) in the \( \eta_b(1S) \) region (b) and in the \( \eta_b(2S) \) region (c). The solid (dashed) histogram presents the fit result (background component of the fit function).

We fit the \( h_b(nP) \) yield dependence on \( M_{\text{miss}}^{(i)}(\pi^+\pi^-\gamma) \) to a sum of the \( \eta_b(nS) \) signal components described by the convolution of a non-relativistic Breit-Wigner function with the resolution function and a background parameterized by an exponentiation of a first- [second-] order polynomial in the \( \eta_b(1S) \) \( \eta_b(2S) \) region. The two \( M_{\text{miss}}^{(i)}(\pi^+\pi^-\gamma) \) spectra [from the \( h_b(1P) \) and \( h_b(2P) \)] with \( \eta_b(1S) \) signals are fitted simultaneously. We find event yields for the \( h_b(nP) \to \eta_b(mS) \) transitions of \( N_{1P-1S} = (23.5 \pm 2.0) \times 10^3 \), \( N_{2P-1S} = (10.3 \pm 1.3) \times 10^3 \) and \( N_{2P-2S} = (25.8 \pm 4.9) \times 10^3 \); the fitted masses and width are \( m_{b_{01}(1S)} = (9402.4 \pm 1.5 \pm 1.8) \text{ MeV}/c^2 \), \( \Gamma_{\eta_b(1S)} = (10.8^{+4.9}_{-3.7}^{+2.5}) \text{ MeV} \) and \( m_{b_{02}(2S)} = (9999.0 \pm 3.5^{+2.8}_{-1.9}) \text{ MeV}/c^2 \). The confidence level of the \( \eta_b(1S) \) \( \eta_b(2S) \) fit is 61% [36%]. If the \( \eta_b(2S) \) width is allowed to float in the fit, we find \( \Gamma_{\eta_b(2S)} = (4^{+12}_{-20}) \text{ MeV} \) or \( \Gamma_{\eta_b(2S)} < 24 \text{ MeV} \) at 90% C.L. using the Feldman-Cousins approach [12]. For mass and yield measurements, we fix the \( \eta_b(2S) \) width at its value from perturbative calculations [13] \( \Gamma_{\eta_b(2S)} = \Gamma_{\eta_b(1S)} \frac{\Gamma_{\eta_b(2S)}}{\Gamma_{\eta_b(1S)}} = (4.9^{+2.7}_{-1.9}) \text{ MeV} \), where the uncertainty is due to the experimental uncertainty in \( \Gamma_{\eta_b(1S)} \).

To estimate the systematic uncertainties in the \( \eta_b(nS) \) parameters, we vary the polynomial orders and fit intervals in the \( M_{\text{miss}}(\pi^+\pi^-) \) & \( M_{\text{miss}}^{(i)}(\pi^+\pi^-\gamma) \) fits, and the \( M_{\text{miss}}^{(i)}(\pi^+\pi^-\gamma) \) binning by scanning the starting point of the 10 MeV/c\(^2\) bin with 1 MeV/c\(^2\) steps. We also multiply the
non-relativistic Breit-Wigner function by an $E^3_\gamma$ term expected for an electric dipole transition and include the uncertainty in the $h_b(1P)$ and $h_b(2P)$ masses and in the estimated value of the $\eta_b(2S)$ width. We add the various contributions in quadrature to estimate the total systematic uncertainty. For the hyperfine splittings $m_{\Upsilon(nS)} - m_{\eta_b(nS)}$ we determine $\Delta M_{\text{HF}}(1S) = (57.9 \pm 2.3)\text{MeV}/c^2$ and $\Delta M_{\text{HF}}(2S) = (24.3^{+4.0}_{-4.5})\text{MeV}/c^2$, where statistical and systematic uncertainties in mass are added in quadrature.

Using Wilks’ theorem, we find $15\sigma [9\sigma]$ for the $h_b(1P) \rightarrow \eta_b(1S)\gamma [h_b(2P) \rightarrow \eta_b(1S)\gamma]$ statistical significance. For the significance of the $\eta_b(2S)$ signal, we use a method [15] that requires definition of the search window to take into account the “look elsewhere effect.” For the ratio $r = \frac{\Delta M_{\text{HF}}(2S)}{\Delta M_{\text{HF}}(1S)}$, perturbative calculations [14] predict $m_{\eta_b(1S)}^2 \Gamma_{\eta_b(1S)}^{\text{HF}} / m_{\eta_b(2S)}^2 \Gamma_{\eta_b(2S)}^{\text{HF}} = 0.513 \pm 0.011$ (where the error is due to the uncertainties in $\Gamma_{ee}$); this is consistent with the measured value of $0.420^{+0.071}_{-0.079}$. To determine boundaries of the search window, we conservatively assume $r = 0$ and $r = 1$. We find the significance of the $\eta_b(2S)$ signal to be $4.8\sigma [4.2\sigma]$ including systematics.

We measure $\mathcal{B}[h_b(1P) \rightarrow \eta_b(1S)\gamma] = (49.2 \pm 5.7^{+5.6}_{-3.3})\%$, $\mathcal{B}[h_b(2P) \rightarrow \eta_b(1S)\gamma] = (22.3 \pm 3.8^{+3.1}_{-3.3})\%$ and $\mathcal{B}[h_b(2P) \rightarrow \eta_b(2S)\gamma] = (47.5 \pm 10.5^{+6.8}_{-7.7})\%$.

5. Conclusion

In summary, we have observed the $P$-wave spin-singlet bottomonium states $h_b(1P)$ and $h_b(2P)$ in the reaction $e^+e^- \rightarrow \Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^-$. The measured hyperfine splittings are consistent with zero as expected. A detailed analysis revealed that $h_b(nP)$ states in $\Upsilon(5S)$ decays are dominantly produced via intermediate charged bottomonium-like resonances $Z_b(10610)$ and $Z_b(10650)$. Resonances $Z_b(10610)$ and $Z_b(10650)$ have also been observed in decays $\Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^-$. Weighted averages over all five channels give $M = 10607.2 \pm 2.0\text{MeV}/c^2$, $\Gamma = 18.4 \pm 2.4\text{MeV}$ for the $Z_b(10610)$ and $M = 10652.2 \pm 1.5\text{MeV}/c^2$, $\Gamma = 11.5 \pm 2.2\text{MeV}$ for the $Z_b(10650)$, where statistical and systematic errors are added in quadrature. The $Z_b(10610)$ production rate is similar to that of the $Z_b(10650)$ for each of the five decay channels. Their relative phase is consistent with zero for the final states with the $\Upsilon(nS)$ and consistent with 180 degrees for the final states with $h_b(nP)$. Analysis of charged pion angular distributions [8] favor the $J^P = 1^+$ spin-parity assignment for both the $Z_b(10610)$ and $Z_b(10650)$. Since the $\Upsilon(5S)$ has negative $G$-parity, the $Z_b$ states have positive $G$-parity due to the emission of the pion.

We report the first evidence for the $\eta_b(2S)$ using the $h_b(2P) \rightarrow \eta_b(2S)\gamma$ transition, with a significance, including systematics, of $4.2\sigma$, and the first observation of the $h_b(1P) \rightarrow \eta_b(1S)\gamma$ and $h_b(2P) \rightarrow \eta_b(1S)\gamma$ transitions. The mass and width parameters of the $\eta_b(1S)$ and $\eta_b(2S)$ are measured to be $m_{\eta_b(1S)} = (9402.4 \pm 1.5 \pm 1.8)\text{MeV}/c^2$, $m_{\eta_b(2S)} = (9999.0 \pm 3.5^{+2.8}_{-1.1})\text{MeV}/c^2$ and $\Gamma_{\eta_b(1S)} = (10.8^{+3.7}_{-3.7} \pm 4.5)\text{MeV}$. The $m_{\eta_b(2S)}$ and $\Gamma_{\eta_b(1S)}$ are first measurements; the $m_{\eta_b(1S)}$ measurement is the most precise and is about 10MeV$/c^2$ higher than the current world average [7]. The hyperfine splittings, $\Delta M_{\text{HF}}(1S) = (57.9 \pm 2.3)\text{MeV}/c^2$ and $\Delta M_{\text{HF}}(2S) = (24.3^{+4.0}_{-4.5})\text{MeV}/c^2$, are in agreement with theoretical calculations [14]. We measure branching fractions for the transitions $\mathcal{B}[h_b(1P) \rightarrow \eta_b(1S)\gamma] = (49.2 \pm 5.7^{+5.6}_{-3.3})\%$, $\mathcal{B}[h_b(2P) \rightarrow \eta_b(1S)\gamma] = (22.3 \pm 3.8^{+3.1}_{-3.3})\%$ and $\mathcal{B}[h_b(2P) \rightarrow \eta_b(2S)\gamma] = (47.5 \pm 10.5^{+6.8}_{-7.7})\%$ that are somewhat higher than theoretical expectations [1]. We update the $h_b(1P)$ and $h_b(2P)$ mass measurements $m_{h_b(1P)} = (9899.1 \pm 0.4$.
1.0) MeV/c², \( m_{b_0(2P)} = (10259.8 \pm 0.5 \pm 1.1) \) MeV/c², and 1\( P \) and 2\( P \) hyperfine splittings \( \Delta M_{HF}(1P) = (+0.8 \pm 1.1) \) MeV/c², \( \Delta M_{HF}(2P) = (+0.5 \pm 1.2) \) MeV/c².

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