PROCEEDINGS OF SCIENCE

Exclusive charmed/charmless semileptonic decays of B-mesons.

Alexei Sibidanov[*†]
School of Physics
University of Sydney
E-mail: Alexei.Sibidanov@sydney.edu.au

Recent results from the Belle and BABAR experiments on semileptonic decays of B-mesons are reviewed, including their effect on the determination of the CKM matrix elements $|V_{cb}|$ and $|V_{ub}|$.

The XIth International Conference on Heavy Quarks and Leptons
11-15 June, 2012
Prague, The Czech Republic

[*]Speaker.
[†]On behalf of the Belle collaboration

1. Introduction

In the Standard Model (SM) of elementary particle physics, flavor changing weak coupling constants are organized in the so-called CKM (Cabibbo-Kobayashi-Maskawa) matrix, which must be unitary. Particles or forces not described by the SM may violate the unitarity of the CKM matrix. To test this unitarity and to search for phenomena beyond the SM, it is important to precisely measure the values of the matrix elements. The straightforward way to obtain values of $|V_{cb}|$ and $|V_{ub}|$ is to extract them from semileptonic decays of B-mesons, in which the decay rate is directly proportional, to first order, to the corresponding CKM matrix element squared and where QCD uncertainties due to hadronic recoil are under control. In the most common Unitarity Triangle (UT) based on the CKM matrix, the well measured angle ϕ_1 (β in an alternative notation) is opposite to the side whose length is proportional to the ratio $|V_{ub}|/|V_{cb}|$ and which is now known much less precisely, as shown in Fig. 1 made by the CKMfitter group [1]. In this ratio, the main contribution to the uncertainty comes from the value of $|V_{ub}|$.

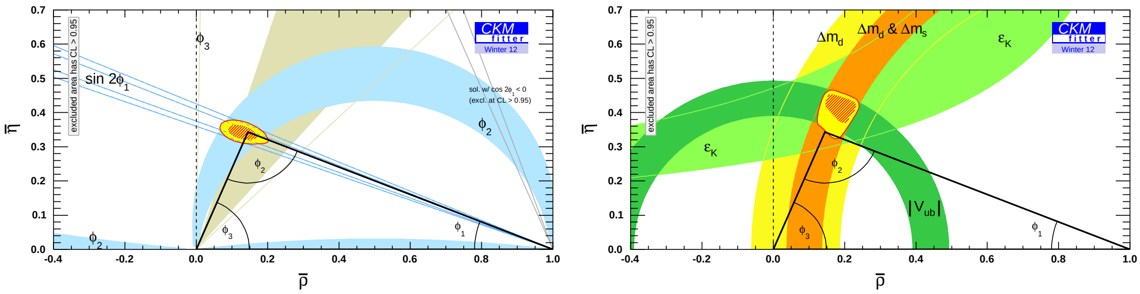

Figure 1: The Unitarity Triangle constraints: left plot – the angle measurements only, right plot – the angle measurements are excluded from the global fit [1].

The best source of B mesons to study semileptonic decays are e^+e^- collisions at the $\Upsilon(4S)$ resonance, where $B\overline{B}$ are pairs produced almost at rest in the $\Upsilon(4S)$ frame and the cross section of $B\overline{B}$ pair production is about 25% of the total hadronic cross section. In a subset of these collisions it is possible to fully reconstruct one B meson decay in a known "tagging" mode and then by using energy-momentum conservation the kinematic variables of the other B can be calculated. This is extremely useful for the exclusive semileptonic decays $B \to X\ell\overline{\nu}_\ell$ where a particular hadronic final state X is reconstructed in the detector and the kinematic properties of the missing neutrino are reconstructed using tag side information.

Two e^+e^- experiments, Belle/KEKB and BABAR/PEP-II were dedicated to the study of properties of B-meson decays at the $\Upsilon(4S)$ resonance, running until recently. They collected in total more then 1.5 ab^{-1} of integrated luminosity, and this data set is not fully analyzed to date. With this amount of data and advanced analysis techniques we can expect steady improvement in our knowledge of semileptonic B decays.

2. Charmed semileptonic decays

The matrix element for $B \to X_q\ell\overline{\nu}_\ell$ decay to first order is

$$\mathscr{M}(B \to X_q\ell\overline{\nu}_\ell) = \frac{G_F}{\sqrt{2}} V_{qb} L^\mu H_\mu,$$

where H_μ is the hadronic current which depends on the specific final state, G_F is the Fermi constant, $L^\mu = \bar{u}_\ell \gamma^\mu (1-\gamma^5) v_\nu$ is the well known leptonic current and V_{qb} is the element of CKM matrix corresponding to the $b \to q$ weak transition.

The differential decay rate for $B \to D^{(*)} \ell \bar{\nu}_\ell$ decay ($\ell = e, \mu$) can be expressed for a vector hadronic final state as

$$\frac{\mathrm{d}\Gamma(\bar{B} \to D^* \ell \bar{\nu})}{\mathrm{d}w \, \mathrm{d}\cos\theta_\ell \, \mathrm{d}\cos\theta_V \, \mathrm{d}\chi} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3} m_{D^*}^3 \sqrt{w^2-1} \, P(w) \, |\mathscr{F}(w, \cos\theta_\ell, \cos\theta_V, \chi)|^2,$$

and for a pseudo-scalar one as

$$\frac{\mathrm{d}\Gamma(\bar{B} \to D \ell \bar{\nu})}{\mathrm{d}w} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3} (m_B + m_D)^2 \, m_D^3 (w^2-1)^{3/2} |\mathscr{G}(w)|^2,$$

where $w = v_B \cdot v_D = (m_B^2 + m_D^2 - q^2)/2 m_B m_D$ is the product of the four-velocities of the final and initial hadronic states and w lies in the range $1 \le w \le w_{\rm max}$. The lower limit $w = 1$ corresponds to maximum momentum transfer squared q^2 to the hadronic recoil. In the Heavy Quark limit $\mathscr{F}(1) = 1$ and $\mathscr{G}(1) = 1$ and corrections to those values can be calculated using lattice QCD. The pseudo-scalar hadronic recoil form factor $\mathscr{G}(1)$ depends only on w and usually is expanded up to the linear term $\mathscr{G}(w) \approx \mathscr{G}(1)(1 - \rho^2(w-1))$ where ρ^2 is the form factor slope.

For the vector final state there are three additional kinematic variables (the θ_ℓ, θ_V and χ helicity angles; see Fig. 2). For massless leptons $\mathscr{F}$ can be expressed as an algebraic combination of w, $\cos\theta_\ell$, $\cos\theta_V$, $\cos\chi$ and three form factors which are dependent only on w: $A_1(w)$, $A_2(w)$ and $V(w)$. The form factor ratios $R_1(w) \propto A_2(w)/A_1(w)$ and $R_2(w) \propto V(w)/A_1(w)$ are constrained from theory. Parameters which currently can be extracted from data are $\mathscr{F}(1)|V_{cb}|$, ρ^2 (the A_1 form factor slope at $w = 1$), $R_1(1)$ and $R_2(1)$. More details about charmed semileptonic form factors can be found in [2].

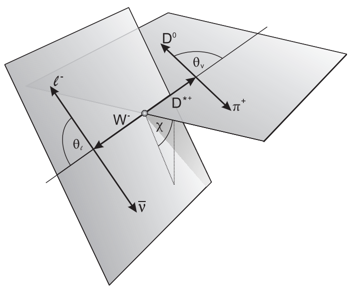

Figure 2: Definition of helicity angles in $B \to D^* \ell \bar{\nu}_\ell$ decay.

The current average by the Heavy Flavor Averaging Group (HFAG) [3] for $\mathscr{G}(1)|V_{cb}|$ is completely dominated by two BABAR analyses of exclusive $B \to D \ell \bar{\nu}_\ell$ decays as shown in Fig. 3. One has used fully reconstructed B mesons as a tag which provided a relatively clean sample of $B \to D \ell \bar{\nu}_\ell$ [4] and another has performed a global fit in $(p_\ell, p_D, \cos\theta_{BY})$ space and also extracted parameters of $B \to D^* \ell \bar{\nu}_\ell$ decay [5]. The results of these two analyses are considered to be largely uncorrelated. One can expect further improvement for this decay because the BABAR results are based on half of their full data set and the Belle result shown in Fig. 3 is based on only 10.2 of the 711 fb^{-1} of collected data. HFAG obtained the average

$$|V_{cb}| = (39.70 \pm 1.42_{\rm EXP} \pm 0.89_{\rm LQCD}) \times 10^{-3}$$

using $\mathscr{G}(1) = 1.074(18)(16)$ from unquenched Lattice QCD [7].

Recently Belle published results of an analysis of exclusive $B \to D^* \ell \bar{\nu}_\ell$ decay based on the full 711 fb^{-1} data-set collected at the $\Upsilon(4S)$ resonance [6]. Belle has used half of the reconstructed $B \to D^* \ell \bar{\nu}_\ell$ events to measure the soft pion efficiency from D^* decay and another half , which is about 123×10^3 events, to measure the branching fraction $\mathscr{B}(B^0 \to D^{*-} \ell \bar{\nu}_\ell) = (4.58 \pm 0.03 \pm 0.26)\%$ and

PoS(HQL 2012)009

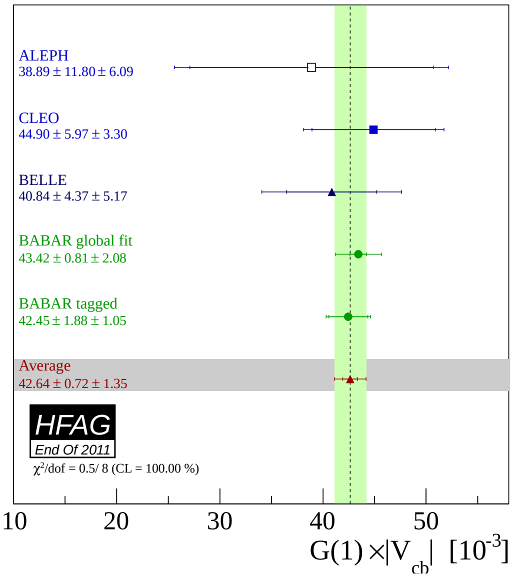

Figure 3: The HFAG average of $\mathscr{G}(1)|V_{cb}|$ [3].

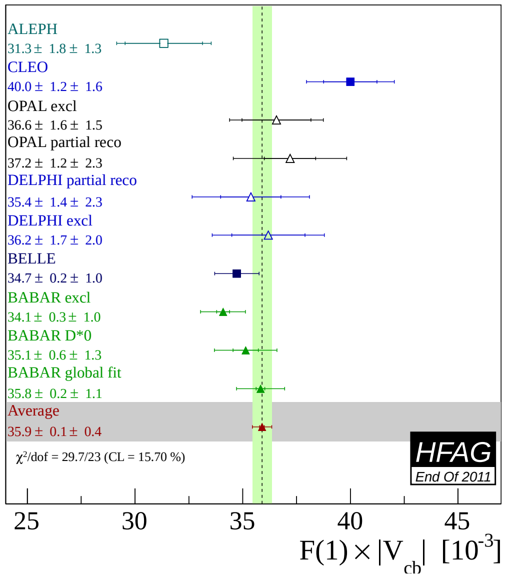

Figure 4: The HFAG average of $\mathscr{F}(1)|V_{cb}|$ [3].

perform a fit in 40 bins of w, $\cos\theta_\ell$, $\cos\theta_V$ and χ to obtain the following form factor parameters: $\mathscr{F}(1)|V_{cb}| = (34.6 \pm 0.2 \pm 1.0) \times 10^{-3}$, $\rho^2 = 1.214 \pm 0.034 \pm 0.009$, $R_1(1) = 1.401 \pm 0.034 \pm 0.018$, $R_2(1) = 0.864 \pm 0.024 \pm 0.008$. The goodness of fit is $\chi^2/\text{ndf} = 138.8/155$. The HFAG average of $\mathscr{F}(1)|V_{cb}|$ is shown in Fig. 4. They then obtained

$$|V_{cb}| = (39.54 \pm 0.50_{\text{EXP}} \pm 0.74_{\text{LQCD}}) \times 10^{-3}$$

using $\mathscr{F}(1) = 0.908 \pm 0.017$ from a recent lattice QCD calculation [8]. This value is in excellent agreement with the $B \to D\ell\bar{\nu}_\ell$ result.

The exclusive $|V_{cb}|$ value above can be compared with the inclusive $|V_{cb}| = (41.88 \pm 0.73) \times 10^{-3}$ obtained by HFAG in the kinetic scheme with a c-quark mass constraint. There is a 2σ tension between the inclusive and exclusive determination of the value of $|V_{cb}|$.

2.1 $B^+ \to D_s^{(*)-} K^+ \ell \bar{\nu}_\ell$ decay

Semileptonic decays of B-mesons to hadronic states containing a $D_s^{(*)}K$ system can provide information about the poorly explored region of hadronic masses above 2.46 GeV/c^2. Recently BABAR has analyzed the $B^+ \to D_s^{(*)-} K^+ \ell \bar{\nu}_\ell$ decay and measured the inclusive D_s and D_s^* branching fraction $\mathscr{B}(B^+ \to D_s^{(*)-} K^+ \ell \bar{\nu}_\ell) = [6.13^{+1.04}_{-1.03}(\text{stat.}) \pm 0.43(\text{syst.}) \pm 0.51(\mathscr{B}(D_s))] \times 10^{-4}$ [9].

Belle has recently performed an analysis of the decay $B^+ \to D_s^{(*)-} K^+ \ell \bar{\nu}_\ell$ using 605 fb^{-1} of data [10]. Values of the branching fractions are $\mathscr{B}(B^+ \to D_s^{(*)-} K^+ \ell \bar{\nu}_\ell) = [5.9 \pm 1.2(\text{stat.}) \pm 1.5(\text{syst.})] \times 10^{-4}$ for the combined mode and $\mathscr{B}(B^+ \to D_s K^+ \ell \bar{\nu}_\ell) = [3.0 \pm 0.9(\text{stat.})^{+1.1}_{-0.8}(\text{syst.})] \times 10^{-4}$ and $\mathscr{B}(B^+ \to D_s^{*-} K^+ \ell \bar{\nu}_\ell) = [2.9 \pm 1.6(\text{stat.})^{+1.1}_{-1.0}(\text{syst.})] \times 10^{-4}$ for the individual modes. For the first time, Belle has also presented the D_sK invariant mass spectrum (Fig. 5) with a prominent peak around 2.6 GeV/c^2, which may be explained by D excited states. The results from both experiments are in excellent agreement.

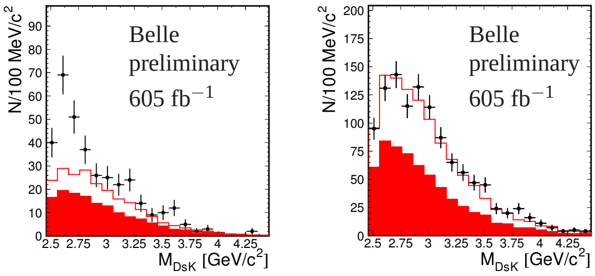

Figure 5: The Belle invariant mass spectrum of D_sK in the signal enriched sample (left) and sideband (right). The filled (empty) histograms show expected backgrounds from fake (true) D_s.

3. Charmless semileptonic decays

The differential decay rate for $B \to X_u \ell \overline{\nu}_\ell$ decay ($\ell = e, \mu$) can be expressed in a similar way to that given in Section 2, except in this case it is more convenient to use the hadron recoil q^2 for form factor parametrization because non-perturbative calculations using Light Cone Sum Rules (LCSR) can predict the form factor behavior at $q^2 = 0$. Thus, analogously to the case for $B \to D\ell\overline{\nu}_\ell$ decay, the differential decay rate for $B \to \pi\ell\overline{\nu}_\ell$ decay assuming massless leptons is

$$\frac{\mathrm{d}\Gamma(B \to \pi\ell\overline{\nu}_\ell)}{\mathrm{d}q^2} = \frac{G_F^2 |V_{ub}|^2}{192\pi^3 m_B^3} \lambda(q^2)^{3/2} |f_+^\pi(q^2)|^2,$$

where $\lambda(q^2) = (q^2 + m_B^2 - m_\pi^2)^2 - 4m_B^2 m_\pi^2$ is a phase space factor, $q^2 = (p_\ell + p_\nu)^2 = (p_B - p_\pi)^2$ is the hadronic recoil four momentum squared, and $f_+^\pi(q^2)$ is a vector form factor. For the case of vector particle hadronic recoil the differential decay rate can be expressed in a similar way to that for $B \to D^*\ell\overline{\nu}_\ell$ decay.

3.1 Untagged analysis

There has been much progress in the untagged analysis of $B \to \pi\ell\overline{\nu}_\ell$ decays in recent times by the Belle [13] and BABAR [11, 12] experiments, on which the current HFAG averages are mainly based. In all cases the signal has been extracted in a similar way, by fitting distributions in the variables $\Delta E = E_{\text{beam}} - (E_\pi + E_\ell + E_\nu)$ and $M_{bc} = \sqrt{E_{\text{beam}}^2 - |\vec{p}_\pi + \vec{p}_\ell + \vec{p}_\nu|^2}$, where E_{beam} is the energy of the incoming electron or positron in the $\Upsilon(4S)$ rest frame. As an example, projections of the M_{bc} and ΔE distributions obtained by Belle are shown in Fig. 6.

In all analyses the differential decay rate $\mathrm{d}\Gamma/\mathrm{d}q^2$ has been measured, which either allows extraction of the $|V_{ub}|$ value in a limited range of q^2 or a model independent fit to be performed using form factors calculated by lattice QCD methods. In Table 1 values for $|V_{ub}|$ based on form factor predictions by various models and branching fractions in the corresponding phase space regions performed by HFAG are listed. Model independent fit results in the full phase space region of the BABAR [11, 12] and Belle [13] measurements, along with FNAL/MILC lattice QCD calculations [18] are shown in Fig. 7. The result of the fit is $|V_{ub}| = [3.23 \pm 0.30] \times 10^{-3}$ but the consistency of the fit is not good, $\chi^2/\text{dof} = 58.9/31$, and this may suggest that some of the inputs have underestimated errors.

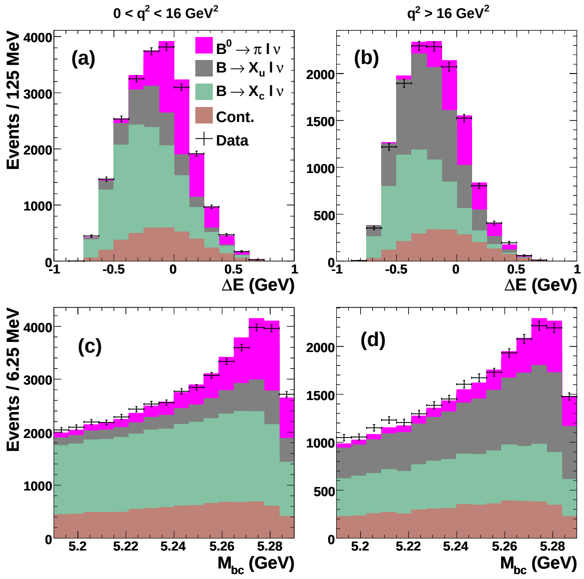

Figure 6: Fit projections in ΔE with $M_{bc} > 5.27$ GeV/c^2 (top row) and in M_{bc} with $|\Delta E| < 0.125$ GeV (bottom row) from Belle [13]. Left and right columns show the regions $q^2 < 16$ GeV$^2/c^2$ and $q^2 > 16$ GeV$^2/c^2$ respectively.

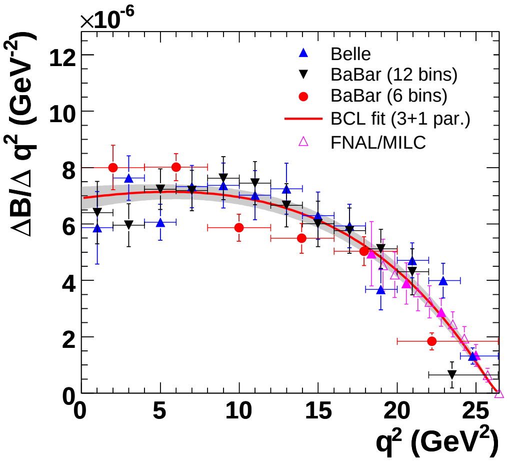

Figure 7: Simultaneous fit of BABAR [11, 12] and Belle [13] $B \to \pi \ell \bar{\nu}_\ell$ measurements and FNAL/MILC lattice QCD calculations [18].

Table 1: HFAG determination of $|V_{ub}|$ based on decay width and theoretical prediction of form factor within limited q^2 range.

Theory	q^2, GeV$^2/c^2$	$\lvert V_{ub}\rvert \times 10^3$
LCSR1 [15]	< 12	$3.40 \pm 0.07^{+0.37}_{-0.32}$
LCSR2 [16]	< 16	$3.57 \pm 0.06^{+0.59}_{-0.39}$
HPQCD [17]	> 16	$3.45 \pm 0.09^{+0.60}_{-0.39}$
FNAL/MILC [18]	> 16	$3.30 \pm 0.09^{+0.37}_{-0.30}$

BABAR also recently studied the decay $B^+ \to \omega \ell \bar{\nu}_\ell$ and measured the total branching fraction, differential decay rate in 5 bins of q^2 [19], and extracted the $|V_{ub}|$ value in different q^2 regions. This analysis supersedes the previous BABAR result [20]. The branching fraction value is $\mathscr{B}(B^+ \to \omega \ell \bar{\nu}_\ell) = [1.15 \pm 0.15(\text{stat.}) \pm 0.12(\text{syst.})] \times 10^{-4}$. Compared to the previous result the median value and statistical error are almost the same but the systematic error has increased by 50%. The obtained $|V_{ub}|$ value in the range $q^2 < 12$ GeV$^2/c^2$ using the LCSR form factor prediction [21] is $|V_{ub}| = [3.41 \pm 0.28 \pm 0.38] \times 10^{-3}$, which is in excellent agreement with the value from $B \to \pi \ell \bar{\nu}_\ell$ decay.

3.2 Charmless semileptonic decays with a fully reconstructed tag at Belle

Recently a new reconstruction procedure for B hadronic decays based on the NeuroBayes package has been introduced in Belle [14]. The new procedure tries to reconstruct B-mesons in more than 1100 exclusive hadronic decay channels. Compared to the previous cut-based algorithm it offers roughly a factor of two efficiency gain and about 2.1×10^6 (1.4×10^6) fully reconstructed

$B^{\pm}$ (B^0) decays with 710 fb^{-1} collected at the $\Upsilon(4S)$ resonance. The fully reconstructed hadronic tag method is especially useful for decays with neutrinos in the final state, providing a clean signal sample with very little background. The hadronic tagging has been calibrated using well measured high statistics charmed semileptonic decays with a precision of 4.2 % for B^+ and 4.5 % for B^0 decays.

Using the new tagging method Belle has studied the exclusive charmless semileptonic decays $B \to \pi \ell \bar{\nu}_\ell$, $B \to \rho \ell \bar{\nu}_\ell$, $B^+ \to \omega \ell \bar{\nu}_\ell$, $B^+ \to \eta \ell \bar{\nu}_\ell$ and $B^+ \to \eta' \ell \bar{\nu}_\ell$. The study is based on the full data set of 710 fb^{-1}. All Belle results using hadronic tagging discussed here are preliminary.

Signal yields have been extracted by performing a binned maximum likelihood fit to the missing mass squared distribution for each process without assuming isospin symmetry. The fit results are shown in Fig. 8. As can be seen, with hadronic tagging Belle has an excellent signal-to-background ratio compared to that for untagged analyses. This allows these Belle results to be competitive with the best untagged measurements for $B \to \pi \ell \bar{\nu}_\ell$ decays and even outperform them for $B \to \rho \ell \bar{\nu}_\ell$ and $B^+ \to \omega \ell \bar{\nu}_\ell$ decays.

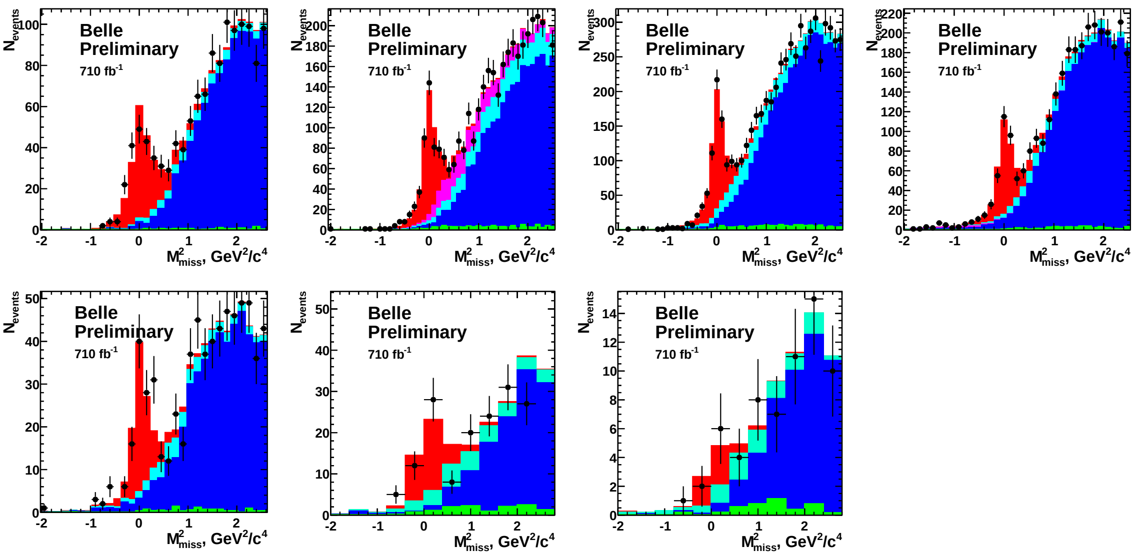

Figure 8: The missing mass squared spectra for $B \to X_u \ell \bar{\nu}_\ell$ decays using fully reconstructed hadronic tagging and Belle data. From left to right – top row: $B^+ \to \pi^0 \ell \bar{\nu}_\ell$, $B^0 \to \pi^+ \ell \bar{\nu}_\ell$, $B^+ \to \rho^0 \ell \bar{\nu}_\ell$, $B^0 \to \rho^+ \ell \bar{\nu}_\ell$; bottom row: $B^+ \to \omega \ell \bar{\nu}_\ell$, $B^+ \to \eta \ell \bar{\nu}_\ell$, $B^+ \to \eta' \ell \bar{\nu}_\ell$. Black points – data, red histogram – corresponding signal, magenta – $\rho^+ \ell \bar{\nu}_\ell$ cross feed, light blue – $X_u \ell \bar{\nu}_\ell$ cross feed, blue – $B\bar{B}$ background, green – continuum background.

The total yields and branching fractions are given in Table 2. The main contribution to the systematic errors comes from the tag calibration uncertainty and this can be further improved by better determination of the charmed semileptonic decays. The measured branching fractions for $B^+ \to \rho^0 \ell \bar{\nu}_\ell$ and $B^+ \to \omega \ell \bar{\nu}_\ell$ decays have better precision than the current HFAG averages. The branching fractions for $B^+ \to \eta \ell \bar{\nu}_\ell$ and $B^+ \to \eta' \ell \bar{\nu}_\ell$ decay confirm the previous *BABAR* measurements and are in good agreement with the corresponding HFAG averages for these modes.

Knowledge of the initial B momentum allows for a precise determination of the momentum transfer squared q^2 compared to the case for an untagged analysis and this is important for mea-

Table 2: Total yields and branching fractions for charmless semileptonic decays with hadronic tagging at Belle.

Process	Yield	$\mathscr{B} \times 10^4$
$B^0 \to \pi^+ \ell \overline{\nu}_\ell$	461±28	$1.49 \pm 0.09 \pm 0.07$
$B^+ \to \pi^0 \ell \overline{\nu}_\ell$	230±22	$0.80 \pm 0.08 \pm 0.04$
$B^0 \to \rho^+ \ell \overline{\nu}_\ell$	338±28	$3.17 \pm 0.27 \pm 0.18$
$B^+ \to \rho^0 \ell \overline{\nu}_\ell$	632±35	$1.86 \pm 0.10 \pm 0.09$
$B^+ \to \omega \ell \overline{\nu}_\ell$	99±15	$1.09 \pm 0.16 \pm 0.08$
$B^+ \to \eta \ell \overline{\nu}_\ell$	39±11	$0.42 \pm 0.12 \pm 0.05$
$B^+ \to \eta' \ell \overline{\nu}_\ell$	6.1±4.7	< 0.57 @ 90% CL

surement of the $\mathrm{d}\Gamma/\mathrm{d}q^2$ differential decay rate. To obtain the differential decay rate, fits to the missing mass squared distributions were performed in bins of q^2. The results are shown in Fig. 9 for the decays where statistics allowed it.

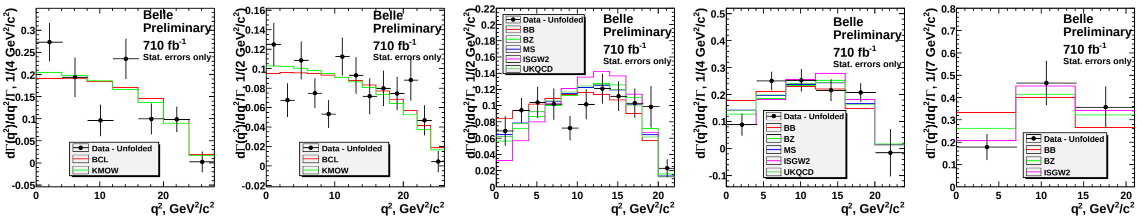

Figure 9: The normalized differential decay rate $\mathrm{d}\Gamma/\mathrm{d}q^2$ determined from Belle data using a hadronic tag method. From left to right: $B^+ \to \pi^0 \ell \overline{\nu}_\ell$, $B^0 \to \pi^+ \ell \overline{\nu}_\ell$, $B^+ \to \rho^0 \ell \overline{\nu}_\ell$, $B^0 \to \rho^+ \ell \overline{\nu}_\ell$ and $B^+ \to \omega \ell \overline{\nu}_\ell$. Theoretical models – BCL [25], KMOW [15], BB [26], BZ [21], MS [23], ISGW2 [24] and UKQCD [22].

Form factors predicted by LCSR models are valid within a limited q^2 range close to $q^2 = 0$, whereas lattice QCD calculations can only be done when the recoil hadron system is produced at rest, which corresponds to maximum momentum transfer $q^2 = \max$. For exclusive charmless semileptonic decays the most recent theoretical studies are available only for $B \to \pi \ell \overline{\nu}_\ell$ decay. There has not been much progress on the theory side for other light hadron states. In Table 3, using various form factor predictions in various phase space regions, extracted values of $|V_{ub}|$ are given. For $B \to \pi \ell \overline{\nu}_\ell$ decay, Belle extracted $|V_{ub}|$ in both isospin states without assuming isospin symmetry, whereas current HFAG averages are mainly based on the $B^0 \to \pi^+ \ell \overline{\nu}_\ell$ decay mode with a small admixture of $B^+ \to \pi^0 \ell \overline{\nu}_\ell$ fixed by isospin relations. There is good agreement between the Belle results and current HFAG averages, as can be seen from Table 1. The uncertainty of $|V_{ub}|$ obtained from exclusive $B \to \rho \ell \overline{\nu}_\ell$ decay is almost the same as from the HFAG average of $B \to \pi \ell \overline{\nu}_\ell$ decays. Reliable inputs from theory are needed for this decay, taking into account the finite width of ρ, ρ-ω mixing and possible excited states of the ρ.

4. Conclusions

The Belle and *BABAR* experiments stopped operating several years ago but analysis of data collected by the experiments is not finished and is still producing outstanding scientific results.

Table 3: The Belle preliminary determination of $|V_{ub}|$ based on the decay rate of exclusive $B \to X_u \ell \overline{\nu}_\ell$ and theoretical predictions of form factors within various q^2 ranges. The theoretical uncertainty for the ISGW2 model is not available.

X_u	Theory	q^2, GeV/c^2	$\lvert V_{ub}\rvert \times 10^3$
π^0	LCSR1 [15]	< 12	$3.30 \pm 0.22 \pm 0.09^{+0.35}_{-0.30}$
	LCSR2 [16]	< 16	$3.62 \pm 0.20 \pm 0.10^{+0.60}_{-0.40}$
	HPQCD [17]	> 16	$3.45 \pm 0.31 \pm 0.09^{+0.58}_{-0.38}$
	FNAL/MILC [18]	> 16	$3.30 \pm 0.30 \pm 0.09^{+0.36}_{-0.30}$
π^+	LCSR1 [15]	< 12	$3.38 \pm 0.14 \pm 0.09^{+0.36}_{-0.32}$
	LCSR2 [16]	< 16	$3.57 \pm 0.13 \pm 0.09^{+0.59}_{-0.39}$
	HPQCD [17]	> 16	$3.86 \pm 0.23 \pm 0.10^{+0.66}_{-0.44}$
	FNAL/MILC [18]	> 16	$3.69 \pm 0.22 \pm 0.09^{+0.41}_{-0.34}$
ρ^0	LCSR [21]	< 16	$3.60 \pm 0.11 \pm 0.09^{+0.54}_{-0.37}$
	Beyer/Melikhov [23]	full range	$3.80 \pm 0.11 \pm 0.10^{+0.31}_{-0.25}$
	UKQCD [22]	full range	$3.72 \pm 0.10 \pm 0.09^{+0.29}_{-0.34}$
	ISWG2 [24]	full range	$4.02 \pm 0.11 \pm 0.10^{+?.??}_{-?.??}$
ρ^+	LCSR [21]	< 16	$3.48 \pm 0.17 \pm 0.10^{+0.52}_{-0.36}$
	Beyer/Melikhov [23]	full range	$3.64 \pm 0.15 \pm 0.10^{+0.30}_{-0.24}$
	UKQCD [22]	full range	$3.56 \pm 0.15 \pm 0.10^{+0.28}_{-0.33}$
	ISWG2 [24]	full range	$3.84 \pm 0.16 \pm 0.11^{+?.??}_{-?.??}$
ω	LCSR [21]	< 12	$3.02 \pm 0.29 \pm 0.11^{+0.43}_{-0.30}$
	ISWG2 [24]	full range	$3.06 \pm 0.23 \pm 0.11^{+?.??}_{-?.??}$

The clean environment of e^+e^- colliders is especially useful for studying semileptonic decays of B-mesons in order to derive fundamental parameters of the SM such as the elements $|V_{cb}|$ and $|V_{ub}|$ of the CKM matrix.

The $|V_{cb}|$ values extracted from exclusive $B \to D^* \ell \overline{\nu}_\ell$ and $B \to D \ell \overline{\nu}_\ell$ with new lattice results agree with a high precision. Studies of $B \to D^{(*)} \ell \overline{\nu}_\ell$ decay now enter the poorly explored region in hadronic invariant mass above 2.46 GeV$/c^2$. The first $M_{D_s K}$ spectrum measurement by Belle can help theory to describe this region.

There is much progress in the determination of $|V_{ub}|$ from $B \to \pi \ell \overline{\nu}_\ell$ decay, where recent high statistic measurements allow the form factor shape to be extracted. Together with lattice QCD calculations this allows $|V_{ub}|$ to be determined in a model independent way.

Belle has recently introduced a new procedure for B-meson full reconstruction in hadronic modes and offers a factor of two efficiency gain compared to the previously employed cut based algorithm. With this new method Belle has studied a number of charmless semileptonic modes: $B \to \pi \ell \overline{\nu}_\ell$, $B \to \rho \ell \overline{\nu}_\ell$, $B^+ \to \omega \ell \overline{\nu}_\ell$, $B^+ \to \eta \ell \overline{\nu}_\ell$ and $B^+ \to \eta' \ell \overline{\nu}_\ell$.

Despite all of this progress, there is still a continued tension at the 2σ level between exclusive and inclusive measurements of $|V_{cb}|$ and $|V_{ub}|$. This might yet be solved by improved theoretical calculations of hadronic form factors and more sophisticated analysis of the existing data.

References

[1] J. Charles *et al.* Phys. Rev. D **84** (2011) 033005 [arXiv:1106.4041 [hep-ph]].

[2] I. Caprini, L. Lellouch and M. Neubert, Nucl. Phys. B **530**, 153 (1998) [hep-ph/9712417].

[3] Y. Amhis *et al.* [Heavy Flavor Averaging Group Collaboration], arXiv:1207.1158 [hep-ex].

[4] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. Lett. **104**, 011802 (2010) [arXiv:0904.4063].

[5] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. D **79**, 012002 (2009) [arXiv:0809.0828].

[6] W. Dungel *et al.* [Belle Collaboration], Phys. Rev. D **82** (2010) 112007 [arXiv:1010.5620 [hep-ex]].

[7] M. Okamoto, C. Aubin, C. Bernard, C. E. DeTar, M. Di Pierro, A. X. El-Khadra, S. Gottlieb and E. B. Gregory *et al.*, Nucl. Phys. Proc. Suppl. **140** (2005) 461 [hep-lat/0409116].

[8] J. A. Bailey *et al.* [Fermilab Lattice and MILC Collaboration], PoS LATTICE **2010** (2010) 311 [arXiv:1011.2166 [hep-lat]].

[9] P. del Amo Sanchez *et al.* [BABAR Collaboration], Phys. Rev. Lett. **107** (2011) 041804 [arXiv:1012.4158 [hep-ex]].

[10] J. Stypula *et al.* [Belle Collaboration], arXiv:1207.6244 [hep-ex].

[11] P. del Amo Sanchez *et al.* [BABAR Collaboration], Phys. Rev. D **83** (2011) 032007 [arXiv:1005.3288].

[12] P. del Amo Sanchez *et al.* [BABAR Collaboration], Phys. Rev. D **83** (2011) 052011 [arXiv:1010.0987].

[13] H. Ha *et al.* [BELLE Collaboration], Phys. Rev. D **83** (2011) 071101 [arXiv:1012.0090 [hep-ex]].

[14] M. Feindt, F. Keller, M. Kreps, T. Kuhr, S. Neubauer, D. Zander and A. Zupanc, Nucl. Instrum. Meth. A **654** (2011) 432 [arXiv:1102.3876 [hep-ex]].

[15] A. Khodjamirian, Th. Mannel, N. Offen, Y.-M. Wang, Phys. Rev. **D83** (2011) 094031 [arXiv:1103.2655 [hep-ph]].

[16] P. Ball and R. Zwicky, Phys. Rev. D **71** (2005) 014015 [hep-ph/0406232].

[17] E. Dalgic, A. Gray, M. Wingate, C. T. H. Davies, G. P. Lepage and J. Shigemitsu, Phys. Rev. D **73** (2006) 074502 [Erratum-ibid. D **75** (2007) 119906] [arXiv:hep-lat/0601021].

[18] J. A. Bailey, C. Bernard, C. E. DeTar, M. Di Pierro, A. X. El-Khadra, R. T. Evans, E. D. Freeland and E. Gamiz *et al.*, Phys. Rev. D **79** (2009) 054507 [arXiv:0811.3640 [hep-lat]].

[19] J. P. Lees *et al.* [BABAR Collaboration], arXiv:1205.6245 [hep-ex].

[20] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. **D79** (2009) 052011. [arXiv:0808.3524 [hep-ex]].

[21] P. Ball, R. Zwicky, Phys. Rev. **D71** (2005) 014029. [hep-ph/0412079].

[22] L. Del Debbio *et al.* [UKQCD Collaboration], Phys. Lett. **B416** (1998) 392-401. [arXiv:hep-lat/9708008 [hep-lat]].

[23] M. Beyer and D. Melikhov, Phys. Lett. B **436** (1998) 344 [hep-ph/9807223].

[24] D. Scora, N. Isgur, Phys. Rev. **D52** (1995) 2783-2812. [hep-ph/9503486]. N. Isgur, D. Scora, B. Grinstein, M. B. Wise, Phys. Rev. **D39** (1989) 799-818.

[25] C. Bourrely, I. Caprini, L. Lellouch, Phys. Rev. **D79** (2009) 013008. [arXiv:0807.2722 [hep-ph]].

[26] P. Ball and V. M. Braun, Phys. Rev. D **58**, 094016 (1998) [hep-ph/9805422].

PoS(HQL 2012)009