

B_S^0 decays at Belle

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We report the measurement of the absolute branching fraction for $B_S^0 \rightarrow J/\psi \phi$, for $B_S^0 \rightarrow J/\psi K^+ K^-$ and $B_S^0 \rightarrow J/\psi f_2'(1525)$ as well as a first observation of $B_S^0 \rightarrow J/\psi \eta$ and $B_S^0 \rightarrow J/\psi \eta'$. In addition the results for the absolute branching ratios of the decay channels $B_S^0 \rightarrow D_S^{(*)+} D_S^{(*)-}$ and a determination of the ratio $\frac{\Delta\Gamma_S}{\Gamma_S}$ are presented.

All results are based on a 121 fb^{-1} data sample collected with the Belle detector at the KEK-B asymmetric e^+e^- collider at the $\Upsilon(5S)$ resonance.

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1 **1. Introduction**

2 During its operation, the Belle detector collected over 700 fb^{-1} of data at the $\Upsilon(4S)$ resonance and
 3 121 fb^{-1} at the $\Upsilon(5S)$ resonance. This second data sample is unique at B factories and provides the
 4 opportunity to study decays of B_s^0 mesons.

5 To extract the B_s^0 signal, two nearly independent kinematic variables, ΔE and M_{bc} , are used:

$$\Delta E = E_B^* - E_{\text{beam}}^* \quad \text{and} \quad M_{bc} = \sqrt{(E_{\text{beam}}^*)^2 - (p_B^*)^2} \quad (1.1)$$

6 where E_{beam}^* is the beam energy in the center of mass frame and E_B^* and p_B^* denote the energy and
 7 the momentum of the reconstructed B_s^0 meson, respectively, given in the center of mass system.

8 In the analyses presented below, the B_s^0 meson is fully reconstructed. However, the photon from
 9 the decay $B_s^* \rightarrow B_s^0 \gamma$ is not included. As the energy information from this photon is lost, the sig-
 10 nal region plotted in the M_{bc} - ΔE plane splits up into three areas, depending on the number of B_s^*
 11 mesons in the initial state. As these areas are not overlapping in M_{bc} , they can easily be separated
 12 during the analysis by choosing a certain range in M_{bc} (fig. 1(b)).

13
 14 The Belle detector, located at the asymmetric e^+e^- collider KEK-B [1] in Tsukuba Japan, is a
 15 large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer
 16 central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-
 17 like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter
 18 comprised of CsI(Tl) crystals (ECL) located inside a super-conducting solenoid coil that provides
 19 a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect K_L^0
 20 mesons and to identify muons (KLM). The detector is described in detail elsewhere [2].

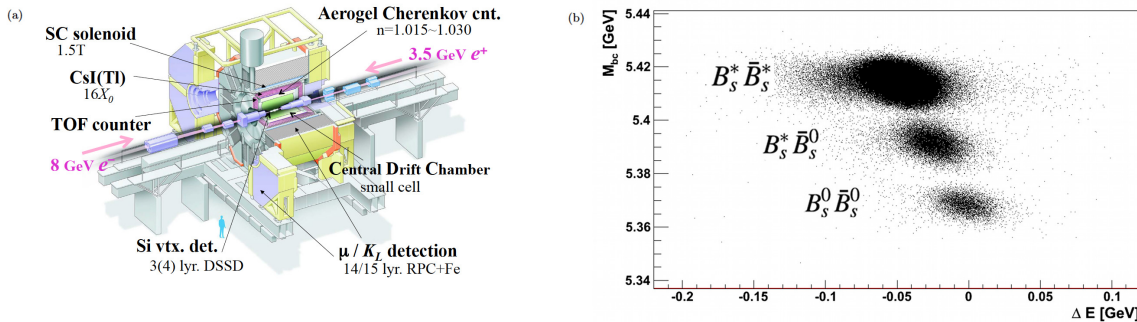


Figure 1: (a) Schematic view of the Belle detector. (b) Signal regions (from MC data) shown as a scatter plot in the $M_{bc} - \Delta E$ plane.

21 **2. Precise measurement of $\mathcal{B}(B_s^0 \rightarrow J/\psi \phi)$ and $\mathcal{B}(B_s^0 \rightarrow J/\psi K^+ K^-)$**

22 The decay $B_s^0 \rightarrow J/\psi \phi$ is an important mode for measuring the CP violating phase ϕ_s in $B_s \bar{B}_s$
 23 mixing, which is of particular interest as it is expected to be sensitive to physics beyond the Stan-
 24 dard Model [3]. While hadron collider experiments recently improved the measurement of this

25 parameter [4], they have to calculate the corresponding branching ratios relative to another decay
 26 channel. However, the Belle experiment can directly determine the absolute branching fractions as
 27 the final state $e^+e^- \rightarrow \Upsilon(5S) \rightarrow B_S^0 \bar{B}_S^0$ is well defined at lepton collider experiments. Until now,
 28 the value of the branching fraction for $B_S^0 \rightarrow J/\psi \phi$ is based on a relative measurement from the
 29 CDF experiment [5, 6, 7]. Therefore, a precise measurement of the absolute branching ratio is an
 30 important extension of the current study of the $B_S^0 \rightarrow J/\psi \phi$ decay.

31 Furthermore, in this analysis the absolute branching fractions of the decays $B_S^0 \rightarrow J/\psi K^+K^-$ and
 32 $B_S^0 \rightarrow J/\psi f_2'(1525)$ – both have not been measured so far – are determined together with the
 33 branching ratio of $B_S^0 \rightarrow J/\psi \phi$. The decay $B_S^0 \rightarrow J/\psi f_2'(1525)$ was recently found by the LHCb
 34 [8] and D0 [9] experiments.

35
 36 Candidate events are selected as follows: First, the decay $J/\psi \rightarrow \ell^+\ell^-$ is reconstructed by identi-
 37 fying two oppositely charged leptons (electrons or muons) with invariant mass close to the nominal
 38 J/ψ mass. A correction for energy loss through bremsstrahlung emission is applied. The J/ψ
 39 candidate is combined with two oppositely charged identified kaons. In case of the invariant kaon
 40 mass, only a lower cut of $m(K^+K^-) \geq 0.95$ GeV is applied, which corresponds to the lower end of
 41 the $m(K^+K^-)$ phase space, so that the full $m(K^+K^-)$ distribution can be investigated.

42 Finally, to extract the B_S^0 meson signal only events with $M_{bc} > 5.4$ GeV are selected, which means
 43 only the dominant $B_S^* \bar{B}_S^*$ signal region is investigated as this provides the best signal to background
 44 ratio.

45
 46 To determine the branching ratios a two dimensional unbinned likelihood fit in ΔE and $m(K^+K^-)$
 47 is performed.

48 The probability density functions (pdfs) for the $m(K^+K^-)$ distribution are determined by investi-
 49 gating generic Monte Carlo (MC) data. The simulation of this data basically includes all known
 50 contributions that can be found in the PDG and additionally the decay $B_S^0 \rightarrow J/\psi f_2'(1525)$. In case
 51 of the ΔE distribution, the pdf parameters are adjusted by using the real data control sample from
 52 the decay $B^0 \rightarrow J/\psi K^*(892)$, as its final state is very similar to the final state of the investigated
 53 decays, except that one kaon is replaced by a pion.

54 Investigating the $m(K^+K^-)$ distribution, the peak of the ϕ meson can be clearly identified at the
 55 low energy part of the spectrum, while the peak of the $f_2'(1525)$ is located at 1.52 GeV. The nonres-
 56 onant decay $B_S^0 \rightarrow J/\psi K^+K^-$ has a flat distribution up to the kinematic endpoint of the $m(K^+K^-)$
 57 spectrum which can be modeled by an Argus function. As a consequence, the three decay modes
 58 are distinguishable via the distribution of the invariant kaon mass, rather than by performing an
 59 angular analysis.

60
 61 The fit results obtained from the full 121 fb^{-1} Belle data sample are presented in tab. 1 and the
 62 applied pdf model is found to be in good agreement with the data (fig. 2 and fig. 3).

63 With a signal yield of 158 ± 13 (168 ± 14) events for $B_S^0 \rightarrow J/\psi \phi$ in the muon (electron) channel,
 64 the corresponding branching fraction can be calculated to be

$$\mathcal{B}(B_S^0 \rightarrow J/\psi \phi) = (1.25 \pm 0.07_{\text{stat}} \pm 0.20_{\text{sys}}) 10^{-3} \quad (2.1)$$

65 This result does not include contributions from the decay channels $B_S^0 \rightarrow J/\psi K^+K^-$ or $B_S^0 \rightarrow$

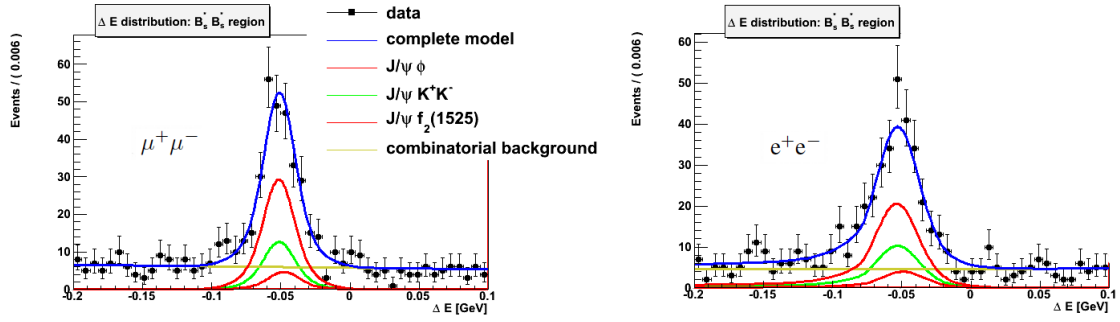


Figure 2: Fitted ΔE distribution for the $\mu^+\mu^-$ and the e^+e^- channel on 121 fb^{-1} .

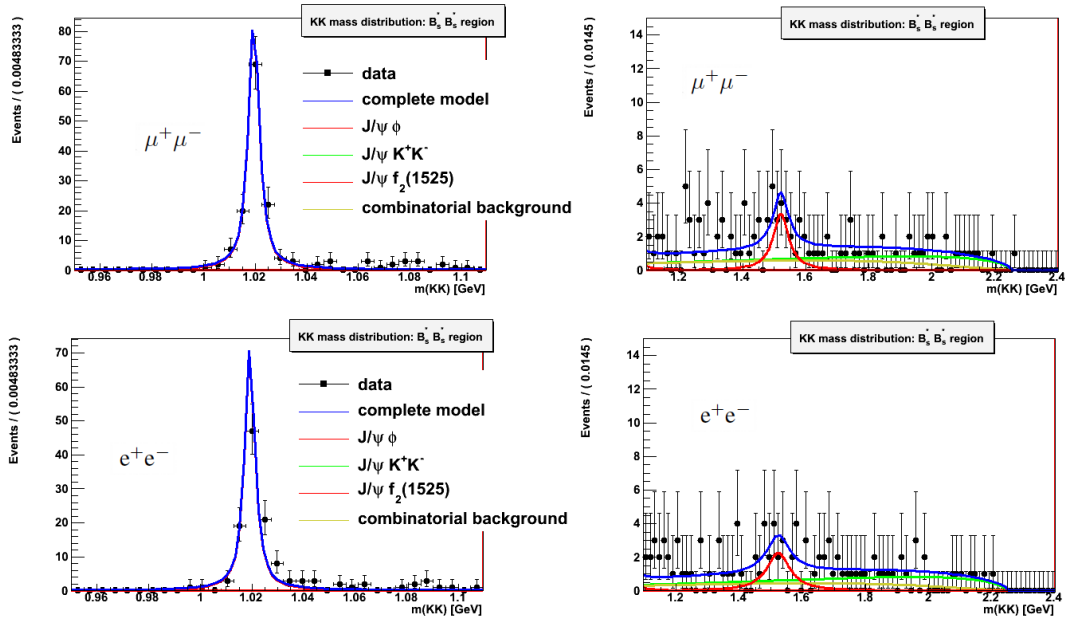


Figure 3: Fitted $m(K^+K^-)$ distribution for the $\mu^+\mu^-$ and the e^+e^- channel on 121 fb^{-1} . The selection $-0.07 \text{ GeV} \leq \Delta E \leq -0.03 \text{ GeV}$ is applied.

66 $J/\psi f_2'(1525)$ and is in agreement with the current PDG value as well as with the old and the cur-
 67 rent results from the CDF experiment [5, 6, 7].

68 Summarizing all contributions to the systematic error that are presented in tab. 2, the total system-
 69 atic error concerning $\mathcal{B}(B_S^0 \rightarrow J/\psi \phi)$ is determined to be 16%. The dominant contribution to
 70 the systematic error is the uncertainty in f_S , the ratio of $B_S^* \bar{B}_S^*$ events within all produced $b\bar{b}$ pairs,
 71 which is therefore limiting the accuracy of the analysis at the present time.

72 The fit result for the nonresonant component $B_S^0 \rightarrow J/\psi K^+K^-$ is 89 ± 13 (110 ± 16) events in the
 73 muon (electron) channel, which leads to

$$\mathcal{B}(B_S^0 \rightarrow J/\psi K^+K^-) = (0.36 \pm 0.04_{\text{stat}} \pm 0.08_{\text{sys}}) 10^{-3} \quad (2.2)$$

channel	$J/\psi \phi$	$J/\psi K^+K^-$	$J/\psi f_2'(1525)$	combinatorial background
$\mu^+\mu^-$	158 ± 13	89 ± 13	25.3 ± 8.5	304 ± 20
e^+e^-	168 ± 14	110 ± 16	32.6 ± 10.5	239 ± 20

Table 1: Signal yields for the $\mu^+\mu^-$ and the e^+e^- channel on 121 fb^{-1} .

Parameter	Error	%
Luminosity	0.847 fb^{-1}	0.7
$\sigma_{\text{bb}}^{\text{r}(s\text{S})}$ [10]	0.014 nb	4.6
f_s [11]	0.029	15.0
$\mathcal{B}(J/\psi \rightarrow \mu^+\mu^-)$ [5]	0.0006	1.0
$\mathcal{B}(J/\psi \rightarrow e^+e^-)$ [5]	0.0006	1.0
$\mathcal{B}(\phi \rightarrow K^+K^-)$ [5]	0.005	1.0
$\mathcal{B}(f_2(1525) \rightarrow K^+K^-)$ [5]	0.011	2.5
$\epsilon_{\text{MC statistic}}(\mu^+\mu^-)$	0.001	0.2
$\epsilon_{\text{MC statistic}}(e^+e^-)$	0.001	0.3
$\epsilon_{\text{Polarisation}}(\mu^+\mu^-)$	0.005	1.5
$\epsilon_{\text{Polarisation}}(e^+e^-)$	0.004	1.3
tracking		1.4
lepton and kaon ID		2.0
PDF shape $B_S^0 \rightarrow J/\psi_{\mu^+\mu^-} \phi$	3.7 events	2.3
PDF shape $B_S^0 \rightarrow J/\psi_{e^+e^-} \phi$	4.6 events	2.7
PDF shape $B_S^0 \rightarrow J/\psi_{\mu^+\mu^-} K^+K^-$	10.5 events	11.8
PDF shape $B_S^0 \rightarrow J/\psi_{e^+e^-} K^+K^-$	22.6 events	20.5
PDF shape $B_S^0 \rightarrow J/\psi_{\mu^+\mu^-} f_2'(1525)$	1.9 events	7.7
PDF shape $B_S^0 \rightarrow J/\psi_{e^+e^-} f_2'(1525)$	3.3 events	10.2

Table 2: Contributions to the systematic error in the absolute branching fractions.

74 The estimated significance of this measurement is 5.3σ , including the systematic uncertainty. This
 75 value does not contain events from $B_S^0 \rightarrow J/\psi \phi$. However, the contribution from the decay $B_S^0 \rightarrow$
 76 $J/\psi f_2'(1525)$ is not separated from this result. The dominant sources of the systematic error are
 77 the uncertainty in f_s and the pdf shape.

78 The fit results for the decay $B_S^0 \rightarrow J/\psi f_2'(1525)$ are 25.3 ± 8.5 (32.6 ± 10.5) events in the muon
 79 (electron) channel. The corresponding branching fractions can be calculated to be

$$\mathcal{B}(B_S^0 \rightarrow J/\psi f_2'(1525)) = (0.24 \pm 0.06_{\text{stat}} \pm 0.04_{\text{sys}}) 10^{-3} \quad (2.3)$$

80 which has a statistical significance of 4.0σ , taking into account the systematic uncertainties.

81 The branching ratio for $B_S^0 \rightarrow J/\psi f_2'(1525)$, relative to the branching fraction for $B_S^0 \rightarrow J/\psi \phi$,
 82 is determined to

$$\frac{\mathcal{B}(B_S^0 \rightarrow J/\psi f_2'(1525))}{\mathcal{B}(B_S^0 \rightarrow J/\psi \phi)} = 19.3 \pm 4.6_{\text{stat}} \pm 3.1_{\text{sys}} \% \quad (2.4)$$

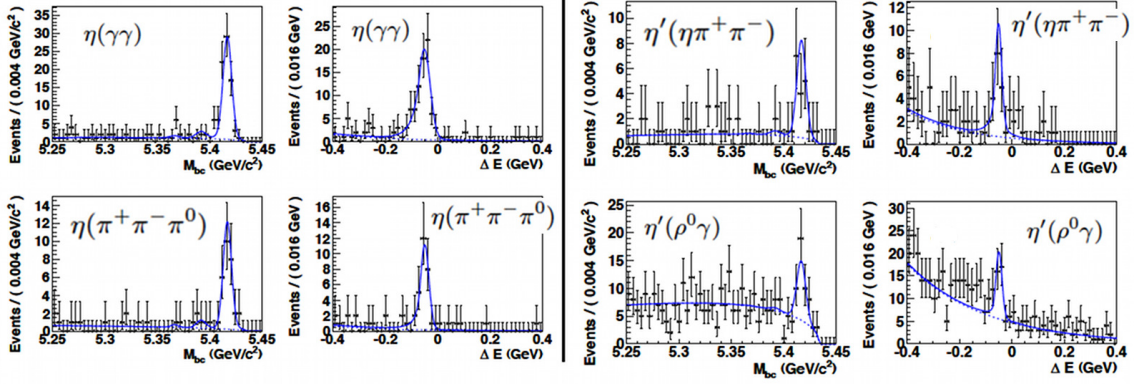


Figure 4: Fitted M_{bc} and ΔE distributions for $B_S^0 \rightarrow J/\psi \eta$ (left) and $B_S^0 \rightarrow J/\psi \eta'$ (right). The solid lines present the projection of the fit results, while the dotted curves illustrate the background component.

83 which is in very good agreement with the reported results from LHCb with $26.4 \pm 2.7 \pm 2.4\%$ [8]
 84 and from D0 with $22 \pm 5 \pm 4\%$ [9].

85 **3. First observation of $B_S^0 \rightarrow J/\psi \eta$ and $B_S^0 \rightarrow J/\psi \eta'$**

86 The measurement of the decays $B_S^0 \rightarrow J/\psi \eta$ and $B_S^0 \rightarrow J/\psi \eta'$ provides the possibility to investi-
 87 gate new CP-even eigenstates. Furthermore, the SU(3) flavor symmetry predicts the ratio of these
 88 two branching fractions to be close to one and therefore, a measurement of these decay channels
 89 would allow to test the SU(3) symmetry as well as the $\eta - \eta'$ mixing (for more detail, see *e.g.*
 90 [12, 13, 14, 15]).

91 However, these decays have not been observed so far. The L3 experiment published an upper limit
 92 of $\mathcal{B}(B_S^0 \rightarrow J/\psi \eta) < 3.8 \cdot 10^{-3}$ at a 90% confidence level [16].

94 To determine the branching fractions of $B_S^0 \rightarrow J/\psi \eta$ and $B_S^0 \rightarrow J/\psi \eta'$ the B_S^0 meson is fully recon-
 95 structed in five different final states. While the J/ψ meson is identified via two oppositely charged
 96 leptons, the η meson is reconstructed from a $\gamma\gamma$ or $\pi^+\pi^-\pi^0$ state and the η' meson is expected to
 97 decay into a $\rho^0\gamma$ or a $\eta\pi^+\pi^-$ final state. For more detailed information on the reconstruction and
 98 the fitting method in this analysis see [17].

99 The fit is performed as a two dimensional unbinned, extended maximum likelihood fit in ΔE and
 100 M_{bc} , simultaneously for all five final states. The fit results are presented in fig. 4 where the applied
 101 pdf model shows a good agreement with the data in all subchannels. With 141 ± 14 (86 ± 14) events
 102 found for $B_S^0 \rightarrow J/\psi \eta$ ($B_S^0 \rightarrow J/\psi \eta'$), the corresponding branching fractions are calculated to

$$\mathcal{B}(B_S \rightarrow J/\psi \eta) = \left(5.10 \pm 0.50_{\text{stat}} \pm 0.25_{\text{sys}} \begin{matrix} +1.14 \\ -0.79 \end{matrix} (N_{B_S^*} \bar{B}_S^{(*)}) \right) \cdot 10^{-4} \quad (3.1)$$

$$\mathcal{B}(B_S \rightarrow J/\psi \eta') = \left(3.71 \pm 0.61_{\text{stat}} \pm 0.18_{\text{sys}} \begin{matrix} +0.83 \\ -0.57 \end{matrix} (N_{B_S^*} \bar{B}_S^{(*)}) \right) \cdot 10^{-4} \quad (3.2)$$

104 The dominant systematic error is the uncertainty in f_S , which is quoted separately as third error in
 105 equations 3.1 and 3.2.

channel	signal yield	\mathcal{B} [%]	significance
$D_S^+ D_S^-$	$33.1^{+6.0}_{-5.4}$ events	$0.58^{+0.11}_{-0.09} \text{stat} \pm 0.13 \text{sys}$	11.5σ
$D_S^{*\pm} D_S^{\mp}$	$44.5^{+5.8}_{-5.5}$ events	$1.8 \pm 0.2 \text{stat} \pm 0.4 \text{sys}$	10.1σ
$D_S^{*+} D_S^{*-}$	$24.4^{+4.1}_{-3.8}$ events	$2.0 \pm 0.3 \text{stat} \pm 0.5 \text{sys}$	7.8σ

Table 3: Results for $B_S^0 \rightarrow D_S^{(*)+} D_S^{(*)-}$ on 121 fb^{-1} .

106 The ratio of these two branching fractions is determined to be

$$\frac{\mathcal{B}(B_S \rightarrow J/\psi \eta')}{\mathcal{B}(B_S \rightarrow J/\psi \eta)} = 0.73 \pm 0.14 \text{stat} \pm 0.02 \text{sys} \quad (3.3)$$

107 While the result for $B_S^0 \rightarrow J/\psi \eta$ is in agreement with the upper limit obtained from the L3 experi-
108 ment, the determined ratio shows a deviation at a 2.1σ level with respect to the prediction.

109 4. Observation of $B_S^0 \rightarrow D_S^{(*)+} D_S^{(*)-}$ and determination of $\Delta\Gamma_S$

110 While previous measurements of the decay width difference $\Delta\Gamma_S$ are based on the decay mode
111 $B_S^0 \rightarrow J/\psi \phi$ [18, 19, 20], the decay channels $B_S^0 \rightarrow D_S^{(*)+} D_S^{(*)-}$ can provide another possibility to
112 investigate CP violation in the $B_S^0 \bar{B}_S^0$ system. Assuming that these decays have CP-even final states
113 and saturate the decay width difference $\Delta\Gamma_S^{\text{CP}}$ [21], the ratio $\Delta\Gamma_S/\Gamma_S$ is simply depending on the
114 branching fraction including all CP-even decay modes and the CP violating phase ϕ_S [22]

$$\frac{\Delta\Gamma_S}{\Gamma_S} = \frac{1/\cos\phi_S - \sqrt{(1/\cos\phi_S)^2 - 4\mathcal{B}(1-\mathcal{B})}}{1-\mathcal{B}} \quad (4.1)$$

115 In this analysis the B_S^0 meson is reconstructed in the three final states $B_S^0 \rightarrow D_S^+ D_S^-$, $B_S^0 \rightarrow D_S^{*\pm} D_S^{\mp}$
116 and $B_S^0 \rightarrow D_S^{*+} D_S^{*-}$ with $D_S^{\pm} \rightarrow \phi \pi^{\pm}$, $K_S^0 K^{\pm}$, $\bar{K}^{*0} K^{\pm}$, $\phi \rho^{\pm}$, $K_S^0 K^{*\pm}$, $\bar{K}^{*0} K^{*\pm}$. Afterwards a two
117 dimensional unbinned, extended maximum-likelihood fit is performed in ΔE and M_{bc} . The results
118 are presented in fig. 5 and tab. 3. For more detailed information on the reconstruction and fit
119 method see [23].

120 The total signal yield is determined to be $102.0^{+9.3}_{-8.6}$ events which corresponds to an absolute
121 branching fraction of

$$\mathcal{B} = \left(4.3 \pm 0.4 \text{stat} \pm 0.5 \text{sys} \pm 0.9 [\mathcal{B}]_{\text{sys}} \right) \% \quad (4.2)$$

122 where the last systematic error is due to uncertainties in external parameters as f_S and the D_S^{\pm}
123 branching fractions, which form the most important contributions to the total systematic error.

124 Assuming that the CP violation is negligible ($\phi_S = 0$) the ration $\Delta\Gamma_S/\Gamma_S$ is calculated with the
125 above branching fraction to be

$$\frac{\Delta\Gamma_S}{\Gamma_S} = 0.090 \pm 0.009 \pm 0.022 \quad (4.3)$$

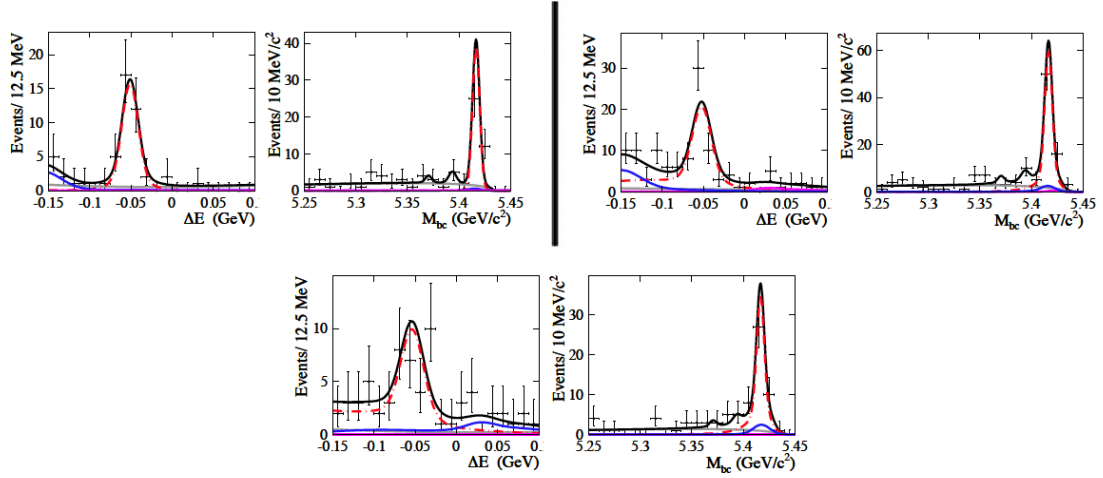


Figure 5: Fitted ΔE and M_{bc} distributions for $B_S^0 \rightarrow D_S^+ D_S^-$ (upper left plot), $B_S^0 \rightarrow D_S^{*+} D_S^-$ (upper right plot) and $B_S^0 \rightarrow D_S^{*+} D_S^{*-}$ (lower plot). The solid black line presents the complete pdf model, the red line shows the signal from correct reconstructed wrong combined events, the purple line indicates the cross-feed and the grey line illustrates the background.

126 which is consistent with theory predictions and comparable with results from hadron collider ex-
 127 periments.

128 5. Summary

129 We performed a precise measurement of the absolute branching fraction for $B_S^0 \rightarrow J/\psi \phi$, for
 130 $B_S^0 \rightarrow J/\psi f_2'(1525)$ and the inclusive branching ratio for $B_S^0 \rightarrow J/\psi K^+ K^-$. The results concern-
 131 ing the branching fractions of $B_S^0 \rightarrow J/\psi \phi$ and $B_S^0 \rightarrow J/\psi f_2'(1525)$ are in good agreement with
 132 previous measurements from other experiments.

133 Furthermore, we presented the first observation of $B_S^0 \rightarrow J/\psi \eta$ and $B_S^0 \rightarrow J/\psi \eta'$. While the
 134 result for the branching fraction of $B_S^0 \rightarrow J/\psi \eta$ is in agreement with the upper limit of a former
 135 measurement, the ratio of the two branching fractions shows a deviation of 2.1σ level with regard
 136 to the prediction.

137 In addition we presented a precise measurement of the absolute branching ratios for $B_S^0 \rightarrow D_S^{(*)+} D_S^{(*)-}$
 138 and a determination of $\frac{\Delta\Gamma_S}{\Gamma_S}$ which is comparable with results from hadron collider experiments and
 139 consistent with theory predictions.

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