

## Heavy quark impact factor for the LHC phenomenology

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We comment on the calculation of the finite part of the heavy quark impact factor at next-to-leading logarithmic (N $L_x$ ) accuracy. The result is presented in a form suitable for phenomenological studies such as the calculation of the cross-section for single heavy quark production at the LHC within the  $k_T$ -factorization scheme.

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## 1. Introduction

Significant developments in the last two decades in small- $x$  physics made possible the phenomenological analysis of deep inelastic scattering (DIS) and other high energy scattering processes within the  $k_T$ -factorization scheme. They were mainly driven by the Balitsky-Fadin-Kuraev-Lipatov (BFKL) framework for the resummation of high center-of-mass energy logarithms at leading (Lx) [1] and next-to-leading (NLx) [2] logarithmic accuracy.

A key ingredient for studying high energy scattering processes within the  $k_T$ -factorisation scheme is the impact factor, a process dependent object. The impact factors for gluons and massless quarks have been calculated in Ref. [3], at NLx accuracy. This allows for the calculation of various processes with massless quarks and gluons in the initial state. The generalization to hadron-hadron collisions has also been established [4–6].

The NLx impact factor for a massive quark in the initial state has been calculated in Ref. [7]. However, the result was given in the form of a sum of an infinite number of terms. To make the result of Ref. [7] available for phenomenological studies we recalculate the NLx heavy quark impact factor in a compact and resummed form which is more suitable for numerical applications.

## 2. High energy factorisation

In the high energy limit:  $\Lambda_{QCD} \ll |t| \ll s$ , the partonic cross-section of  $2 \rightarrow 2$  processes factorises into the impact factors  $h_a(\mathbf{k}_1)$  and  $h_b(\mathbf{k}_2)$  of the two colliding partons a and b, and the gluon Green's function  $\mathcal{G}_\omega(\mathbf{k}_1, \mathbf{k}_2)$  (here in Mellin space) so that the differential cross-section can be written as

$$\frac{d\sigma_{ab}}{d[\mathbf{k}_1]d[\mathbf{k}_2]} = \int \frac{d\omega}{2\pi i \omega} h_a(\mathbf{k}_1) \mathcal{G}_\omega(\mathbf{k}_1, \mathbf{k}_2) h_b(\mathbf{k}_2) \left( \frac{s}{s_0(\mathbf{k}_1, \mathbf{k}_2)} \right)^\omega,$$

where  $\omega$  is the dual variable to the rapidity  $Y$ , and  $d[\mathbf{k}] = d^{2+2\varepsilon}\mathbf{k}/\pi^{1+\varepsilon}$  is the transverse space measure. The Lx quark impact factor can be expressed by a very simple formula:

$$h^{(0)}(\mathbf{k}) = \sqrt{\frac{\pi}{N_c^2 - 1}} \frac{2C_F \alpha_s N_\varepsilon}{\mathbf{k}^2 \mu^{2\varepsilon}}, \quad N_\varepsilon = \frac{(4\pi)^{\varepsilon/2}}{\Gamma(1 - \varepsilon)},$$

and it is the same (up to a color factor) for quarks and gluons. Variables  $\mu$  and  $\varepsilon$  are the renormalization scale and the dimensional regularization parameter respectively.

## 3. The analytic impact factor

Collecting all the contributions, the impact factor of a heavy quark at NLx accuracy reads  $h_q(\mathbf{k}) = h^{(0)}(\mathbf{k}) + h_q^{(1)}(\mathbf{k})$ , and can be expressed in terms of a singular and a finite contribution

$$h_q(\mathbf{k}) = h_q^{(1)}(\mathbf{k})|_{\text{sing}} + h_q(\mathbf{k})|_{\text{finite}}.$$

The singular term  $h_q^{(1)}(\mathbf{k})|_{\text{sing}}$  is given in [7].

The finite contribution, which is our main result, finally reads

$$h_q(\mathbf{k})|_{\text{finite}} = h^{(0)}(\mathbf{k}, \alpha_s(\mathbf{k})) \left\{ 1 + \frac{\alpha_s N_c}{2\pi} \left[ \mathcal{K} - \frac{\pi^2}{6} + 1 - R \log(4R) - \log(Z) (1 + 2R) \sqrt{\frac{1+R}{R}} \right. \right. \\ \left. \left. - 2\log(Z)^2 - 3\sqrt{R} \left( \text{Li}_2(Z) - \text{Li}_2(-Z) + \log(Z) \log\left(\frac{1-Z}{1+Z}\right) \right) \right. \right. \\ \left. \left. + \text{Li}_2(4R) \Theta_{mk} + \left( \frac{1}{2} \log(4R) + \frac{1}{2} \log^2(4R) + \text{Li}_2\left(\frac{1}{4R}\right) \right) \Theta_{km} \right] \right\},$$

with  $R = \mathbf{k}^2/(4m^2)$  and  $Z = (\sqrt{1+R} + \sqrt{R})^{-1}$ . As in Ref. [7], we have absorbed the singularities proportional to the beta function into the running of the strong coupling  $\alpha_s(\mathbf{k})$  [8], for details we refer the reader to Ref. [9]. The heavy quark impact factor, as described here, will be applied to high-energy phenomenology study of the cross section for single heavy quark forward production at the LHC [10].

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## References

- [1] L. N. Lipatov, Sov. J. Nucl. Phys. **23** (1976) 338; E. A. Kuraev, L. N. Lipatov, V. S. Fadin, Phys. Lett. B **60** (1975) 50, Sov. Phys. JETP **44** (1976) 443, Sov. Phys. JETP **45** (1977) 199; Ia. Ia. Balitsky, L. N. Lipatov, Sov. J. Nucl. Phys. **28** (1978) 822.
- [2] V. S. Fadin, L. N. Lipatov, Phys. Lett. B **429** (1998) 127 [hep-ph/9802290]; M. Ciafaloni, G. Camici, Phys. Lett. B **430** (1998) 349 [hep-ph/9803389].
- [3] M. Ciafaloni and D. Colferai, Nucl. Phys. B **538**, 187 (1999) [hep-ph/9806350].
- [4] A. H. Mueller and H. Navelet, Nucl. Phys. B **282** (1987) 727.
- [5] A. Sabio Vera and F. Schwennsen, Nucl. Phys. B **776** (2007) 170 [hep-ph/0702158 [HEP-PH]].
- [6] J. Kwiecinski, A. D. Martin, L. Motyka and J. Outhwaite, Phys. Lett. B **514** (2001) 355 [hep-ph/0105039].
- [7] M. Ciafaloni and G. Rodrigo, JHEP **0005** (2000) 042 [hep-ph/0004033].
- [8] G. Rodrigo and A. Santamaria, Phys. Lett. B **313** (1993) 441 [hep-ph/9305305]; G. Rodrigo, A. Pich and A. Santamaria, Phys. Lett. B **424** (1998) 367 [hep-ph/9707474].
- [9] G. Chachamis, M. Deak and G. Rodrigo, arXiv:1310.6611 [hep-ph]; G. Chachamis, M. Deak and G. Rodrigo, arXiv:1307.2780 [hep-ph].
- [10] G. Chachamis, M. Deak, M. Hentschinski, G. Rodrigo, C. Salas and A. S. Vera, work in progress.