

# Jet quenching in a strongly interacting plasma – A lattice approach

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The phenomenon of jet quenching, related to the momentum broadening of a high-energy parton, provides important experimental evidence for the production of a strongly coupled, deconfined medium in heavy-ion collisions. Its theoretical description has been addressed in a number of works, both perturbatively and non-perturbatively (using the gauge-gravity duality). In this contribution, following a proposal by Caron-Huot, we discuss a novel approach to this problem, enabling one to extract non-perturbative information on this real-time phenomenon from simulations on a Euclidean lattice.

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## 1. Introduction

More than thirty years ago, Bjorken suggested a possible way to detect the creation of deconfined QCD matter in collisions of ultrarelativistic nuclei: due to interactions with the medium constituents, a hard parton propagating through the quark-gluon plasma (QGP) at a given temperature  $T$  would experience energy loss and momentum broadening, and this would result in the suppression of final-state hadrons with large transverse momentum and of back-to-back correlations [1]. This prediction was eventually confirmed by experiments [2].

Providing a firm theoretical description for this beautiful physical idea is, however, challenging, as it involves an interplay of both perturbative and non-perturbative physics effects [3]. Even if one focuses only on the short-distance interactions between the hard parton and QGP constituents [4], the problem is still complicated by the fact that, for temperatures within the reach of present experiments, the QCD coupling  $g$  is not very small, so perturbative computations may not be reliable. On the other hand, strong-coupling approaches based on the gauge/string duality, like the ones carried out for a massless hard parton [5] or for the drag force experienced by a heavy quark [6], are not based on the QCD Lagrangian. Finally, non-perturbative lattice QCD computations are not straightforward for this real-time problem.

In this contribution, however, we would like to discuss some recent progress in the latter direction [7], based on an idea proposed in ref. [8]. Related studies include refs. [9–11], whereas a different way to study the jet quenching phenomenon on the lattice was proposed in ref. [12].

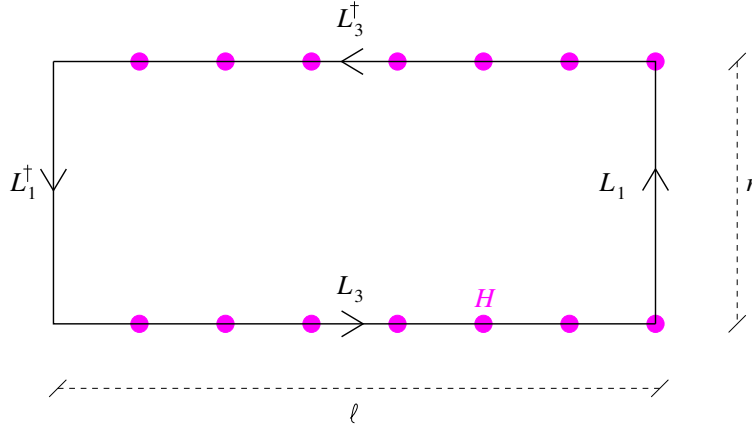
## 2. Soft contribution to jet quenching from a Euclidean lattice

Jet quenching can be described in terms of a phenomenological parameter  $\hat{q}$ , defined as the average increase in the squared transverse momentum component  $p_\perp$  of the hard parton per unit length. This quantity can be expressed in terms of a differential collisional rate between the parton and plasma constituents  $C(p_\perp)$ :

$$\hat{q} = \frac{\langle p_\perp^2 \rangle}{L} = \int \frac{d^2 p_\perp}{(2\pi)^2} p_\perp^2 C(p_\perp). \quad (2.1)$$

In turn,  $C(p_\perp)$  is related to the two-point correlation function of light-cone Wilson lines. Although the full computation of this correlator cannot be carried out on a Euclidean lattice, it is possible to extract the non-perturbative contributions to it from the soft sector, i.e. from physics at momentum scales up to  $gT$ , which can be proven to be time-independent [8, 9]. Evaluating the non-perturbative contribution from soft (and ultrasoft, of order  $g^2 T/\pi$ ) modes is important, since they are responsible for the peculiar analytical structure of weak-coupling computations in thermal QCD and for the large corrections affecting the corresponding perturbative series. A proper systematic framework to deal with these problems can be formulated in terms of dimensionally reduced effective theories [13]. In particular, the soft-scale dynamics can be described by electrostatic QCD (EQCD): an effective theory for the static QGP modes, given by three-dimensional Yang-Mills theory coupled to an adjoint scalar field,

$$\mathcal{L} = \frac{1}{4} F_{ij}^a F_{ij}^a + \text{Tr}((D_i A_0)^2) + m_E^2 \text{Tr}(A_0^2) + \lambda_3 (\text{Tr}(A_0^2))^2. \quad (2.2)$$



**Figure 1:** The “decorated” Wilson loop  $W(\ell, r)$  describing a two-point correlation function of light-cone Wilson lines involves Hermitian parallel transporters  $H(x)$  along the real-time direction.

Its parameters (the 3D gauge coupling  $g_E$  and the mass- and quartic-term coefficients) can be fixed by *matching* to the physics of high-temperature QCD, and the theory can be regularized on a lattice. We chose a setup corresponding to the dimensional reduction of QCD with  $n_f = 2$  light dynamical quark flavors, at two temperatures ( $T \simeq 398$  MeV and 2 GeV) approximately twice and ten times larger than the deconfinement temperature [14].

We simulate this theory and study (a gauge-invariant generalization of) the two-point correlator of light-cone Wilson lines, defined in terms of a lattice operator which involves parallel transporters  $H(x) = \exp[-ag_E^2 A_0(x)]$  along *real time*, which are Hermitian—rather than unitary—operators. This results in a “decorated” Wilson loop  $W(\ell, r)$  (see fig. 1) with well-defined renormalization properties [15]. From its expectation values (computed with the multilevel algorithm [16]) we extract a “potential”

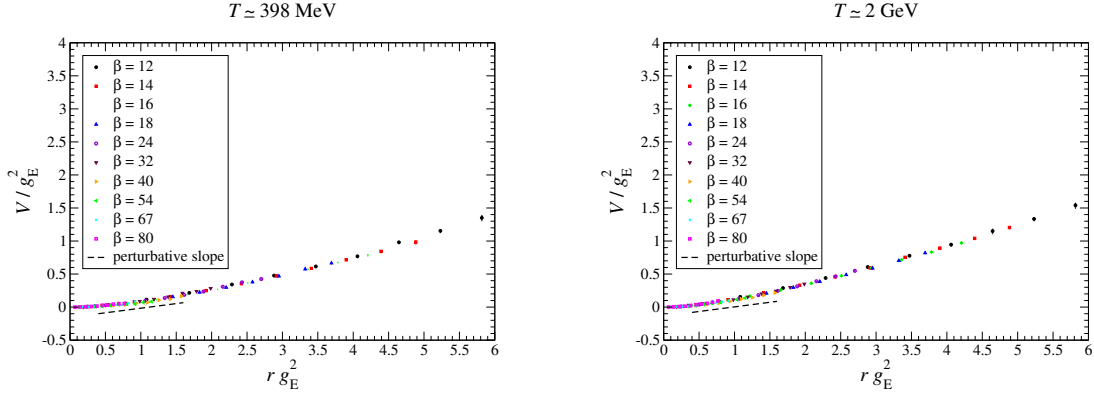
$$V(r) = -\frac{1}{\ell} \ln \langle W(\ell, r) \rangle, \quad (2.3)$$

which is equal to the transverse Fourier transform of  $C(p_\perp)$ .

At short distances our results for  $V(r)$  (shown in fig. 2) are compatible with perturbative expectations, which involve, in particular, a delicate cancellation between gluon and scalar propagators [8, 9]. The non-perturbative contributions to  $V(r)$  can be related to  $\hat{q}$ : the latter is given by the second moment of the distribution associated with  $C(p_\perp)$ , which corresponds to curvature terms in  $V(r)$ . Following an approach similar to ref. [10], we arrive at quite large values for the soft NLO contribution to the jet quenching parameter:  $0.55(5)g_E^6$  for  $T \simeq 398$  MeV, and  $0.45(5)g_E^6$  for  $T \simeq 2$  GeV. In turn, these numbers lead to a final estimate for  $\hat{q}$  around 6 GeV<sup>2</sup>/fm for RHIC temperatures, comparable with those from holographic estimates [5] and from computations with phenomenological input [17].

### 3. Conclusions and outlook

We have shown that, contrary to naïve intuition, the lattice study of certain real-time phenomena involving physics on the light cone is possible. Here we have discussed the phenomenon of jet



**Figure 2:** The “potential”  $V(r)$  extracted from the expectation values of  $W(\ell, r)$ , at  $T \simeq 398$  MeV (left-hand-side panel) and at  $T \simeq 2$  GeV (right-hand-side panel). Both  $V$  and  $r$  are shown in the appropriate units of the dimensionful 3D gauge coupling  $g_E$ . The slope predicted perturbatively for the potential at values  $rg_E^2 \gtrsim 1$  is also displayed.

quenching in thermal QCD, but related ideas have also been proposed for QCD at zero temperature [18].

By construction, the bosonic effective theory that we simulated in our approach allows one to separate the soft contributions to  $\hat{q}$  from those due to hard thermal modes, with momenta of order  $\pi T$ . It does so in a controlled, systematic way, consistent with the modern theoretical framework to study finite-temperature QCD [13, 19].

In the near future, we plan to improve our extrapolation of the potential  $V(r)$  to the continuum limit at short  $r$  by carrying out further simulations on finer lattices, and/or using improved actions [20]. It would also be interesting to study the dependence of  $\hat{q}$  on  $T$ , and on the number of color charges  $N$ . As it is well-known, the large- $N$  limit is characterized by a rich and interesting phenomenology [21], and lattice studies have shown that the static equilibrium properties of the QGP have very little dependence on  $N$ , both in four [22] and in three [23] spacetime dimensions.

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