

Hadronic B decays to open charm and time-independent γ results at LHCb

Susan Haines*[†]

University of Cambridge

E-mail: haines@hep.phy.cam.ac.uk

Studies of hadronic B decays to open charm at LHCb have led to first observations of several $B \rightarrow D\bar{D}'$ decays and of the decays $B^0 \rightarrow D^{*-}K^+\pi^-\pi^+$ and $B_s^0 \rightarrow \bar{D}^0K^-\pi^+$. The branching fractions of other $B \rightarrow D\bar{D}'$ decays, of $B^0 \rightarrow D^{*-}\pi^+\pi^-\pi^+$ and of $B^0 \rightarrow \bar{D}^0K^+\pi^-$ have also been measured and a limit has been set in the search for the decay $B_s^0 \rightarrow D^{*-}\pi^+$. In addition, constraints have been placed on the CKM angle γ and related parameters using time-independent ADS and GGSZ analyses of $B^\pm \rightarrow DK^\pm$ decays.

14th International Conference on B-Physics at Hadron Machines

April 8-12, 2013

Bologna, Italy

*Speaker.

[†]On behalf of the LHCb collaboration.

1. Hadronic B decays to open charm

Several studies of hadronic B decays to open charm have been performed at LHCb; details of the most recent measurements are given below. The inclusion of charge conjugated processes is implied throughout this section.

1.1 Studies of $B \rightarrow D\bar{D}'$ decays

$B \rightarrow D\bar{D}'$ decays can be used to probe CKM matrix elements [1] and to allow better theoretical understanding of the processes that contribute to B meson decay, in particular the contributions from weak exchange, penguin annihilation and rescattering [2, 3].

Measurements of $B \rightarrow D\bar{D}'$ decay branching fractions relative to various normalisation decays have been performed using LHCb data corresponding to an integrated luminosity of 1 fb^{-1} recorded at $\sqrt{s} = 7 \text{ TeV}$ [4]. The decays $\bar{B}_s^0 \rightarrow D^0\bar{D}^0$, $\bar{B}_s^0 \rightarrow D_s^+D^-$ and $\bar{B}_s^0 \rightarrow D^+D^-$ have been observed for the first time, with significances $\geq 10\sigma$; Fig. 1 shows the invariant mass distributions for these decays. The measured ratios of branching fractions are

$$\begin{aligned} \frac{Br(\bar{B}_s^0 \rightarrow D^+D^-)}{Br(\bar{B}^0 \rightarrow D^+D^-)} &= 1.08 \pm 0.20(stat.) \pm 0.10(syst.), \\ \frac{Br(\bar{B}_s^0 \rightarrow D_s^+D^-)}{Br(B^0 \rightarrow D_s^+D^-)} &= 0.050 \pm 0.008(stat.) \pm 0.004(syst.), \\ \frac{Br(\bar{B}_s^0 \rightarrow D^0\bar{D}^0)}{Br(B^- \rightarrow D^0\bar{D}_s^-)} &= 0.019 \pm 0.003(stat.) \pm 0.003(syst.), \\ \frac{Br(\bar{B}^0 \rightarrow D^0\bar{D}^0)}{Br(B^- \rightarrow D^0\bar{D}_s^-)} &= 0.0014 \pm 0.0006(stat.) \pm 0.0002(syst.), \\ \frac{Br(\bar{B}_s^0 \rightarrow D_s^+D_s^-)}{Br(B^0 \rightarrow D_s^+D^-)} &= 0.56 \pm 0.03(stat.) \pm 0.04(syst.), \\ \frac{Br(B^- \rightarrow D^0\bar{D}_s^-)}{Br(B^0 \rightarrow D_s^+D^-)} &= 1.22 \pm 0.02(stat.) \pm 0.07(syst.). \end{aligned}$$

1.2 Search for the decay $B_s^0 \rightarrow D^{*-}\pi^+$

The decay $B_s^0 \rightarrow D^{*-}\pi^+$ is expected to be mediated by weak exchange, with little contribution from rescattering [2]. A measurement of its branching fraction should therefore aid understanding of the mechanism behind the related decays $B_s^0 \rightarrow D\bar{D}'$ and $B_s^0 \rightarrow \pi^-\pi^+$ [5].

A search for the decay has been performed with LHCb data corresponding to an integrated luminosity of 1 fb^{-1} recorded at $\sqrt{s} = 7 \text{ TeV}$ [6]. The decay $B^0 \rightarrow D^{*-}\pi^+$, which is several orders of magnitude more abundant than $B_s^0 \rightarrow D^{*-}\pi^+$, is used as a normalisation channel. No significant signal is observed, so limits of $Br(B_s^0 \rightarrow D^{*-}\pi^+) < 6.1(7.8) \times 10^{-6}$ at 90% (95%) confidence level are set. The measured limit implies that rescattering may make substantial contributions to $B_s^0 \rightarrow D\bar{D}'$ and $B_s^0 \rightarrow \pi^-\pi^+$ decays, as recently suggested [2].

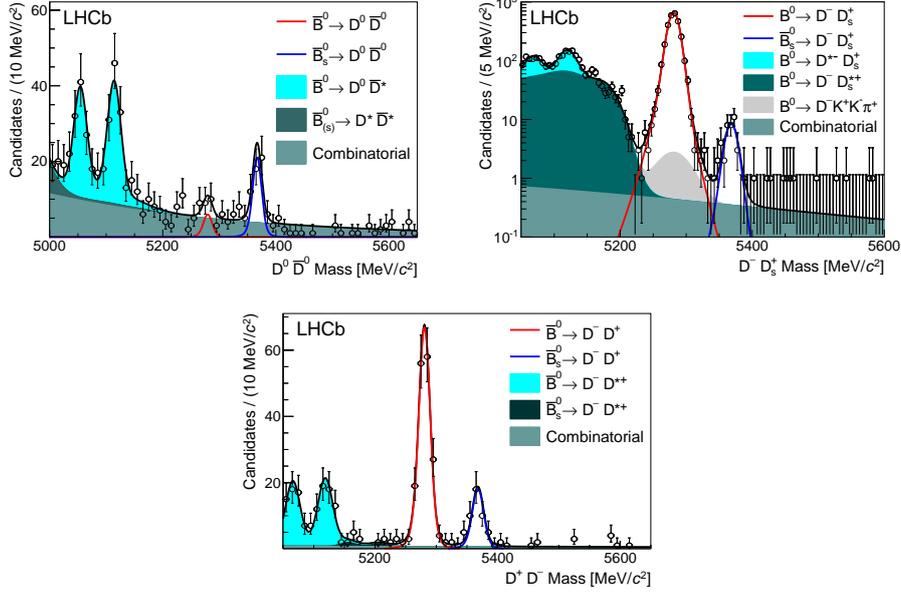


Figure 1: Invariant mass distributions for $\bar{B}_s^0 \rightarrow D^0 \bar{D}^0$, $\bar{B}_s^0 \rightarrow D_s^+ D^-$ and $\bar{B}_s^0 \rightarrow D^+ D^-$ candidate decays [4]. In the legends, “Combinatorial” denotes the combinatorial background component.

1.3 Measurement of $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$ and $B^0 \rightarrow D^{*-} K^+ \pi^- \pi^+$ branching fractions

$B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$ can be used as a normalisation decay for $B^0 \rightarrow D^{*-} \tau^+ (\rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}_\tau) \nu_\tau$; an excess of $B^0 \rightarrow D^{*-} \tau^+ (\rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}_\tau) \nu_\tau$ decays over the Standard Model (SM) expectation has recently been observed [7].

The branching fractions of $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$ and the related decay $B^0 \rightarrow D^{*-} K^+ \pi^- \pi^+$, relative to $Br(B^0 \rightarrow D^{*-} \pi^+)$ and $Br(B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+)$ respectively, have been measured with LHCb data corresponding to an integrated luminosity of 1 fb^{-1} recorded at $\sqrt{s} = 7 \text{ TeV}$ [8]. The resulting values are

$$\frac{Br(B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+)}{Br(B^0 \rightarrow D^{*-} \pi^+)} = 2.64 \pm 0.04(\text{stat.}) \pm 0.13(\text{syst.}),$$

$$\frac{Br(B^0 \rightarrow D^{*-} K^+ \pi^- \pi^+)}{Br(B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+)} = (6.47 \pm 0.37(\text{stat.}) \pm 0.35(\text{syst.})) \times 10^{-2};$$

the decay $B^0 \rightarrow D^{*-} K^+ \pi^- \pi^+$ has been observed for the first time.

A search for resonant structure within the $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$ decay has also been performed, resulting in a first observation of the decay $B^0 \rightarrow \bar{D}_1(2420)^0 (\rightarrow D^{*-} \pi^+) \pi^- \pi^+$ at 5.3σ significance; the measured branching fraction relative to $Br(B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+)$ is

$$\frac{Br(B^0 \rightarrow \bar{D}_1(2420)^0 (\rightarrow D^{*-} \pi^+) \pi^- \pi^+)}{Br(B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+)} = (2.04 \pm 0.42(\text{stat.}) \pm 0.22(\text{syst.})) \times 10^{-2}.$$

1.4 Measurement of $B_{(s)}^0 \rightarrow DK\pi$ branching fractions

$B^0 \rightarrow D^0/\bar{D}^0 K^+ \pi^-$ decays are sensitive to the CKM angle γ ; a future γ measurement using these decays will require careful treatment of the potential background from $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$ decays.

Inclusive branching fraction measurements of $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ and $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$ decays have been made using LHCb data corresponding to an integrated luminosity of 1 fb^{-1} recorded at $\sqrt{s} = 7 \text{ TeV}$ [9]. Figure 2 shows the invariant mass distribution for the candidate decays. The measured branching fraction values, quoted relative to the normalisation branching fraction of $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$, are

$$\frac{Br(B^0 \rightarrow \bar{D}^0 K^+ \pi^-)}{Br(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)} = 0.106 \pm 0.007(\text{stat.}) \pm 0.008(\text{syst.}),$$

$$\frac{Br(B_s^0 \rightarrow \bar{D}^0 K^- \pi^+)}{Br(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)} = 1.18 \pm 0.05(\text{stat.}) \pm 0.12(\text{syst.});$$

the inclusive $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$ decay has been observed for the first time.

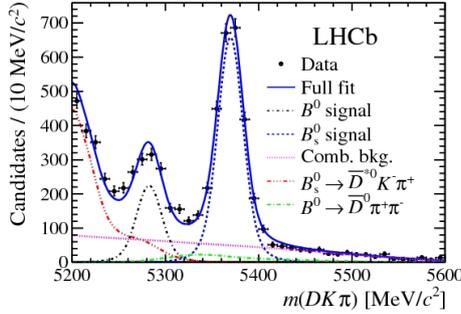


Figure 2: Invariant mass distribution for $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ and $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$ candidate decays [9].

2. Time-independent γ results

The CKM angle $\gamma = \arg(-(V_{ud}V_{ub}^*)/(V_{cd}V_{cb}^*))$ is the least well-constrained angle of the Unitarity Triangle. The current tightest experimental constraints on γ come from indirect measurements, giving a precision of $\approx 4^\circ$ [10, 11], but these may be sensitive to new, non-SM, physics effects in loop processes. It is therefore important to compare them with the SM benchmark obtained by measuring γ directly with tree-level decays. The world average values of γ from direct measurements are $\gamma = (66 \pm 12)^\circ$ [10] and $\gamma = (70.8 \pm 7.8)^\circ$ [11].

At LHCb, both time-independent and time-dependent¹ measurements of γ are performed. Time-independent measurements are made using tree-level $B \rightarrow DX$ decays, where D represents a D^0 or \bar{D}^0 meson; sensitivity to γ arises when D^0 or \bar{D}^0 decay to the same final state, due to interference effects. In conjunction with a measurement of γ , the related parameters r_B (the magnitude of the ratio of amplitudes of the interfering decays) and δ_B (the strong phase difference between them) are also measured.

¹For LHCb time-dependent γ results and γ average, see [12].

2.1 ADS analysis of $B^\pm \rightarrow D(\rightarrow K\pi\pi\pi)K^\pm$ and $B^\pm \rightarrow D(\rightarrow K\pi\pi\pi)\pi^\pm$ decays

The ADS method [13] uses $B \rightarrow DX$ decays with the D meson decaying to a final state which is not a CP eigenstate. The full decay can take one of two paths: in one case, the favoured B decay is followed by a doubly Cabibbo-suppressed D decay; in the other case the suppressed B decay is followed by a Cabibbo-allowed D decay. Overall, the sensitivity to γ is maximised because the interfering amplitudes from the two decay paths are comparable in size.

A study of $B^\pm \rightarrow D(\rightarrow K\pi\pi\pi)K^\pm$ and $B^\pm \rightarrow D(\rightarrow K\pi\pi\pi)\pi^\pm$ decays has been performed at LHCb using data corresponding to an integrated luminosity of 1 fb^{-1} recorded at $\sqrt{s} = 7 \text{ TeV}$ [14]. The D decay is treated inclusively, with no attempt made to separate the resonant structures of the decay. The suppressed ADS decays $B^\pm \rightarrow D(\rightarrow \pi^\pm K^\mp \pi^+ \pi^-)K^\pm$ and $B^\pm \rightarrow D(\rightarrow \pi^\pm K^\mp \pi^+ \pi^-)\pi^\pm$ have been observed for the first time, with significances of 5.1σ and $> 10\sigma$, respectively; Fig. 3 shows the invariant mass distributions for these decays.

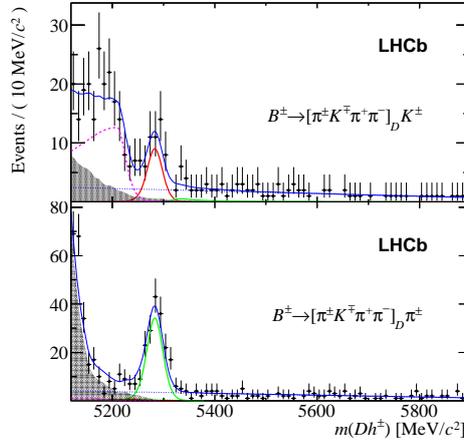


Figure 3: Invariant mass distributions for $B^\pm \rightarrow D(\rightarrow \pi^\pm K^\mp \pi^+ \pi^-)K^\pm$ and $B^\pm \rightarrow D(\rightarrow \pi^\pm K^\mp \pi^+ \pi^-)\pi^\pm$ candidate decays [14].

The ratios of suppressed to favoured decays, which are most sensitive to γ , r_B and δ_B , have been measured and are combined to obtain values for the ADS asymmetries and ratios,

$$\begin{aligned} A_{ADS(DK)}^{K3\pi} &= -0.42 \pm 0.22, & R_{ADS(DK)}^{K3\pi} &= 0.0124 \pm 0.0027, \\ A_{ADS(D\pi)}^{K3\pi} &= 0.13 \pm 0.10, & R_{ADS(D\pi)}^{K3\pi} &= 0.0037 \pm 0.0004, \end{aligned}$$

where the uncertainties are the combination of statistical and systematic contributions.

Using these results and measurements of parameters of the D decay from CLEO-c [15], a constraint $r_{B(DK)} = 0.097 \pm 0.011$ is evaluated; the measurements do not allow significant constraints to be placed on the other underlying physics parameters.

2.2 Dalitz (GGSZ) analysis of $B^\pm \rightarrow D(\rightarrow K_S^0 \pi^+ \pi^-, K_S^0 K^+ K^-)K^\pm$ decays

The GGSZ method [16, 17] allows γ to be measured from the differences in amplitude of the $D \rightarrow K_S^0 h^+ h^-$ Dalitz plots coming from $B^- \rightarrow DK^-$ and $B^+ \rightarrow DK^+$ decays. The structure of the multi-body D decay must be taken into account as it leads to a variation in amplitude across the

Dalitz plane. One possible “model-independent” approach is to bin the Dalitz plane [16, 18] and input the measured value of the strong phase difference between the D^0 and \bar{D}^0 decays in each bin from CLEO-c studies [19].

Samples of $B^\pm \rightarrow D(\rightarrow K_S^0 \pi^+ \pi^-) K^\pm$ and $B^\pm \rightarrow D(\rightarrow K_S^0 K^+ K^-) K^\pm$ decays, selected from data corresponding to an integrated luminosity of 2 fb^{-1} recorded at $\sqrt{s} = 8 \text{ TeV}$, have been used to measure the observables $x_\pm = r_{B(DK)} \cos(\delta_{B(DK)} \pm \gamma)$ and $y_\pm = r_{B(DK)} \sin(\delta_{B(DK)} \pm \gamma)$ with the model-independent approach [20]. The resulting preliminary values,

$$\begin{aligned} x_+ &= (-8.7 \pm 3.1(\text{stat.}) \pm 1.6(\text{syst.}) \pm 0.6(\text{extl.})) \times 10^{-2}, \\ y_+ &= (0.1 \pm 3.6(\text{stat.}) \pm 1.4(\text{syst.}) \pm 1.9(\text{extl.})) \times 10^{-2}, \\ x_- &= (5.3 \pm 3.2(\text{stat.}) \pm 0.9(\text{syst.}) \pm 0.9(\text{extl.})) \times 10^{-2}, \\ y_- &= (9.9 \pm 3.6(\text{stat.}) \pm 2.2(\text{syst.}) \pm 1.6(\text{extl.})) \times 10^{-2}, \end{aligned}$$

where the third uncertainties arise from the CLEO-c input measurements, are the most precise measurements of these observables to date. The results have been combined with previous GGSZ measurements, made using data corresponding to an integrated luminosity of 1 fb^{-1} recorded at $\sqrt{s} = 7 \text{ TeV}$ [21], to place constraints on γ , r_B and δ_B ,

$$\gamma = (57 \pm 16)^\circ, r_{B(DK)} = (8.8_{-2.4}^{+2.3}) \times 10^{-2}, \delta_{B(DK)} = (124_{-17}^{+15})^\circ;$$

two-dimensional projections of the confidence regions for the three parameters are shown in Fig. 4.

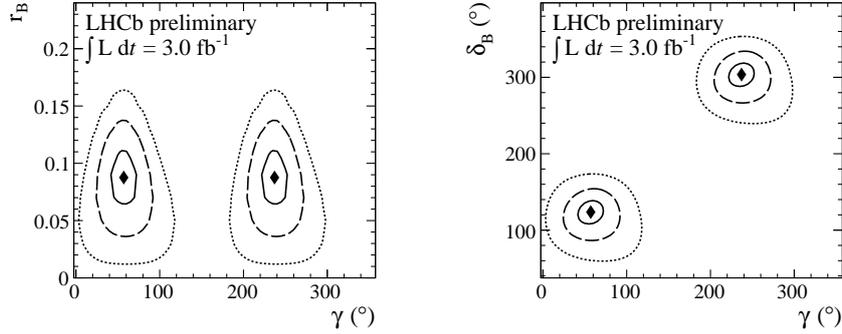


Figure 4: Two-dimensional projections of the confidence regions onto the $(\gamma, r_{B(DK)})$ and $(\gamma, \delta_{B(DK)})$ planes. The diamonds indicate the central values and the 1, 2 and 3σ boundaries are also shown [20].

3. Conclusions and prospects

Recent studies of hadronic B decays to open charm at LHCb have led to the observation of several new $B \rightarrow D\bar{D}'$ decay modes and of the decays $B^0 \rightarrow D^{*-} K^+ \pi^- \pi^+$ and $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$. The branching fractions of other $B \rightarrow D\bar{D}'$ decays, of $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$ and of $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ have also been measured and a limit has been set in the search for $B_s^0 \rightarrow D^{*-} \pi^+$. In addition, the suppressed ADS decays $B^\pm \rightarrow D(\rightarrow \pi^\pm K^\mp \pi^+ \pi^-) K^\pm$ and $B^\pm \rightarrow D(\rightarrow \pi^\pm K^\mp \pi^+ \pi^-) \pi^\pm$ have been observed for the first time, and ADS and GGSZ analyses of $B^\pm \rightarrow DK^\pm$ decays have allowed

constraints to be placed on the CKM angle γ and related parameters. Studies of new decay modes and analysis updates to include the data set recorded in 2012 will provide additional measurements and constraints on γ in the near future.

Acknowledgement

The speaker expresses her gratitude for the generous support of Newnham College, Cambridge, in funding her participation in the conference.

References

- [1] BaBar collaboration, *Measurements of time-dependent CP asymmetries in $B^0 \rightarrow D^{(*)+}D^{(*)-}$ decays*, *Phys. Rev. D* **79**, 032002 (2009) [hep-ex/0808.1866]; Belle collaboration, *Evidence for CP violation in $B^0 \rightarrow D^+D^-$ decays*, *Phys. Rev. Lett.* **98**, 221802 (2007) [hep-ex/0702031]; R. Aleksan et al., *The decay $B \rightarrow D\bar{D}^* + D^*\bar{D}$ in the heavy quark limit and tests of CP violation*, *Phys. Lett. B* **317**, 173 (1993); A. I. Sanda, Z. Z. Xing, *Towards determining ϕ_1 with $B \rightarrow D^{(*)}\bar{D}^{(*)}$* , *Phys. Rev. D* **56**, 341 (1997) [hep-ph/9702297]; Z. Z. Xing, *Measuring CP violation and testing factorization in $B_d \rightarrow D^{*\pm}D^{*\mp}$ and $B_s \rightarrow D_s^{*\pm}D_s^{*\mp}$ decays*, *Phys. Lett. B* **443**, 365 (1998) [hep-ph/9809496]; Z. Z. Xing, *CP violation in $B_d \rightarrow D^+D^-$, $D^{*+}D^-$, D^+D^{*-} and $D^{*+}D^{*-}$ decays*, *Phys. Rev. D* **61**, 014010 (2000) [hep-ph/9907455]; X. Y. Pham, Z. Z. Xing, *CP asymmetries in $B_d \rightarrow D^{*+}D^{*-}$ and $B_s \rightarrow D_s^{*+}D_s^{*-}$ decays: P wave dilution, penguin and rescattering effects*, *Phys. Lett. B* **458**, 375 (1999) [hep-ph/9904360]; A. Datta, D. London, *Extracting γ from $B_d^0(t) \rightarrow D^{(*)+}D^{(*)-}$ and $B_d^0 \rightarrow D_s^{(*)+}D_s^{(*)-}$ decays*, *Phys. Lett. B* **584**, 81 (2004) [hep-ph/0310252]; R. Fleischer, *Exploring CP violation and penguin effects through $B_d^0 \rightarrow D^+D^-$ and $B_s^0 \rightarrow D_s^+D_s^-$* , *Eur. Phys. J. C* **51**, 849 (2007) [arXiv:0705.4421]
- [2] M. Gronau, D. London, J. L. Rosner, *Rescattering contributions to rare B-meson decays*, *Phys. Rev. D* **87**, 036008 (2013) [hep-ph/1211.5785]
- [3] Y. Li, C.-D. Lu, Z.-J. Xiao, *Rare decays $B^0 \rightarrow D_s^{(*)+}D_s^{(*)-}$ and $B_s^0 \rightarrow D^{(*)+}D^{(*)-}$ in perturbative QCD approach*, *J. Phys. G* **31**, 273 (2005) [hep-ph/0308243]; J. Eeg, S. Fajfer, A. Hiorth, *On the color suppressed decay modes $\bar{B}_s^0 \rightarrow D_s^+D_s^-$ and $\bar{B}_s^0 \rightarrow D^+D^-$* , *Phys. Lett. B* **570**, 46 (2003) [hep-ph/0304112]
- [4] LHCb collaboration, *First observations of $\bar{B}_s^0 \rightarrow D^+D^-$, $D_s^+D^-$ and $D^0\bar{D}^0$ decays*, *LHCb-PAPER-2012-050*, to be published in *Phys. Rev. D* [hep-ex/1302.5854]
- [5] M. Gronau, O. F. Hernandez, D. London, J. L. Rosner, *Broken SU(3) symmetry in two-body B decays*, *Phys. Rev. D* **52**, 6356-6373 (1995) [hep-ph/9504326]; R. Fleischer, *New strategies to obtain insights into CP violation through $B_s \rightarrow D_s^\pm K^\mp$, $D_s^{*\pm}K^\mp$, ... and $B_d \rightarrow D^\pm \pi^\mp$, $D^{*\pm} \pi^\mp$, ... decays*, *Nucl. Phys. B* **671**, 459-482 (2003) [hep-ph/0304027]
- [6] LHCb collaboration, *Search for the decay $B_s^0 \rightarrow D^{*\mp} \pi^\pm$* , *Phys. Rev. D* **87**, 071101(R) (2013) [hep-ex/1302.6446]
- [7] BaBar Collaboration, *Evidence for an excess of $B \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau$ decays*, *Phys. Rev. Lett.* **109**, 101802 (2012) [hep-ex/1205.5442]
- [8] LHCb collaboration, *Study of $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$ and $B^0 \rightarrow D^{*-} K^+ \pi^- \pi^+$ decays*, *Phys. Rev. D* **87**, 092001 (2013) [hep-ex/1303.6861]

- [9] LHCb collaboration, *Measurement of the branching fractions of the decays $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$ and $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$* , LHCb-PAPER-2013-022, to be published in *Phys. Rev. D* [hep-ex/1304.6317]
- [10] CKMfitter Group (J. Charles et al.), *Eur. Phys. J. C* **41**, 1-131 (2005) [hep-ph/0406184], updated results and plots available at <http://ckmfitter.in2p3.fr>
- [11] UTfit Collaboration (A. Bevan et al.), results and plots available at www.utfit.org
- [12] M. Schiller, these proceedings
- [13] D. Atwood, I. Dunietz, A. Soni, *Enhanced CP violation with $B \rightarrow KD^0(\bar{D}^0)$ modes and extraction of the CKM angle γ* , *Phys. Rev. Lett.* **78** 3257-3260 (1997) [hep-ph/9612433]; D. Atwood, I. Dunietz, A. Soni, *Improved methods for observing CP violation in $B^\pm \rightarrow KD$ and measuring the CKM phase γ* , *Phys. Rev. D* **63** 036005 (2001) [hep-ph/0008090]
- [14] LHCb collaboration, *Observation of the suppressed ADS modes $B^\pm \rightarrow [\pi^\pm K^\mp \pi^+ \pi^-]_D K^\pm$ and $B^\pm \rightarrow [\pi^\pm K^\mp \pi^+ \pi^-]_D \pi^\pm$* , LHCb-PAPER-2012-055, to be published in *Phys. Lett. B* [hep-ex/1303.4646]
- [15] CLEO Collaboration, *Determination of the $D^0 \rightarrow K^- \pi^+ \pi^0$ and $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$ coherence factors and average strong-phase differences using quantum-correlated measurements*, *Phys. Rev. D* **80** 031105(R) (2009) [hep-ex/0903.4853]
- [16] A. Giri, Y. Grossman, A. Soffer, J. Zupan, *Determining γ using $B^\pm \rightarrow DK^\pm$ with multibody D decays*, *Phys. Rev. D* **68** 054018 (2003) [hep-ph/0303187]
- [17] A. Bondar, *Proceedings of BINP special analysis meeting on Dalitz analysis, 24-26th Sep. 2002, unpublished*
- [18] A. Bondar, A. Poluektov, *Feasibility study of model-independent approach to ϕ_3 measurement using Dalitz plot analysis*, *Eur. Phys. J. C* **47**, 347-353 (2006) [hep-ph/0510246]; A. Bondar, A. Poluektov, *The use of quantum-correlated D^0 decays for ϕ_3 measurement*, *Eur. Phys. J. C* **55**, 51-56 (2008) [hep-ex/0801.0840]
- [19] CLEO Collaboration, *Model-independent determination of the strong-phase difference between D^0 and $\bar{D}^0 \rightarrow K_{S,L}^0 h^+ h^-$ ($h = \pi, K$) and its impact on the measurement of the CKM angle γ/ϕ_3* , *Phys. Rev. D* **82**, 112006 (2010) [hep-ex/1010.2817]
- [20] LHCb collaboration, *Model-independent measurement of CP violation parameters in $B^\pm \rightarrow (K_S^0 h^+ h^-)_D K^\pm$ decays*, LHCb-CONF-2013-004
- [21] LHCb collaboration, *A model-independent Dalitz plot analysis of $B^\pm \rightarrow DK^\pm$ with $D \rightarrow K_S^0 h^+ h^-$ ($h = \pi, K$) decays and constraints on the CKM angle γ* , *Phys. Lett. B* **718**, 43-55 (2012) [hep-ex/1209.5869]