High Energy Jets at the LHC

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The High Energy Jets (HEJ) framework systematically resums the large logarithms which enhance the high order terms in the perturbation theory of QCD which arise in the study of wide-angle jet production the LHC. Our approximation is valid in the limit of hard outgoing partons all well separated in rapidity and is easily generalised to a wide range of LHC phenomena, including observables with multiple high energy jets accompanied by an electroweak boson. Some recent results comparing HEJ to experimental data is presented to highlight the importance of these enhanced terms.
A very high jet multiplicity has been observed in the test of QCD as well as being a background to other for the measurements of the Higgs boson. The observed cross-section ratios have been fitted with a pattern expected the statistical uncertainty on the data, and the hatched (shaded) bands the statistical and systematic uncertainties on data (prediction) added in quadrature.

2. High Energy Jets

In the limit of large invariant mass, $s_{ij} = 2p_i \cdot p_j$, between outgoing partons in a QCD scattering amplitude (the ‘High Energy Limit’) the traditional approach of perturbatively expanding observables in the strong coupling constant $\alpha_s$ begins to break down since each term is accompanied by a large logarithm, $\ln \left( \frac{s}{t} \right)$, where $s$ and $t$ are the usual Mandelstam variables. The high energy limit can also be stated in terms of the rapidities, $y_i$, and perpendicular momentum components, $p_{i\perp}$, of the outgoing partons (the ‘Multi-Regge Kinematic Limit’):

$$y_1 \gg y_2 \gg \cdots \gg y_n, \quad \left| p_{i\perp} \right| \sim \left| p_{j\perp} \right| \quad \forall i, j \tag{2.1}$$
and in terms of this limit it is clear that the region where large logarithms dominate is that of wide-angle hard scattering. In this limit it is possible \cite{1}\cite{2} to write down a factorised form for $2 \to n$ matrix element as follows

$$|\mathcal{M}_{ab \to agg\ldots gb}|^2 = \frac{1}{4(N_c^2 - 1)} ||S_{ab \to ab}||^2 \left( \frac{g_s^2 C_A}{t_i} \right) \left( \frac{g_s^2 C_Y}{t_{n-1}} \right) \prod_{i=1}^{n-2} \left( -\frac{g_s^2 C_A}{t_i t_{i+1}} V_\mu(q_i, q_{i+1}) V^\mu(q_i, q_{i+1}) \right) \prod_{j=1}^{n-2} \exp[a^0(q_j)(y_{j-1} - y_j)],$$

where $q_1 = p_a - p_1$, $q_{i+1} = q_i - p_i$ and $t_i = q_i^2$. The ‘spinor string’, $||S_{ab \to ab}||^2$, is given by:

$$||S_{ab \to ab}||^2 = \sum_{\text{polarisation}} |j_1(p_a, p_1) \cdot j_2(p_b, p_n)|^2,$$  \hspace{1cm} (2.2)

and comprises exact $2 \to 2$ scattering amplitude for the hard incoming partons $a$ and $b$ (summed and averaged over incoming and outgoing helicities/polarisations). $V_\mu(q_i, q_{i+1})$ is the aforementioned effective vertex for the inclusion of extra gluon emissions in the final state and the product of exponentials encodes the large logarithms described above. The above expression is readily generalised to more complicated final states involving electroweak bosons simply by the modification of the spinor string. For example, in the case where a $Z^0$ is emitted from the forward-incoming quark, $p_a/1$, $j_1(p_a, p_1)$ would be modified to a slightly more complicated form, shown diagrammatically in figure (2), given by

$$j'_\mu = \pi^{h_1}(p_1) \left( \gamma^\mu \frac{p_a + p_Z}{(p_1 + p_Z)^2} \gamma_\mu + \gamma_\mu \frac{p_a - p_Z}{(p_a - p_Z)^2} \gamma_\sigma \right) u^{h_2}(p_a) \times \pi^{k_2}(p_{e-}) \gamma_\sigma u^{k_1}(p_{e+})$$ \hspace{1cm} (2.3)

As indicated in figure (2) we also include the contribution from an off-shell photon being exchanged in place of the $Z^0$ and the interference between the two channels. The HEJ package also includes all of the contributions not included in our resummation up to and including states with 4 final state jets by matching the leading order matrix element program MadGraph \cite{7}. 

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Figure 2: The diagrammatic form for the ‘current’ describing emission of a $Z^*/\gamma^*$. 

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3. Comparisons

There have been many very detailed analyses done in recent years comparing HEJ to data (or to other Monte Carlos). Here we present a recent result showing the importance of the enhanced high order corrections included in our resummation. A recent $W^\pm$+jets analysis by the ATLAS collaboration [6], see figure (3), shows that in the limit of large invariant mass discussed above HEJ describes data well where other fixed-order tools struggle. It is also important to note that even at small values for $m_{12}$ (i.e. far outside the high energy limit) HEJ describes the data very well.

References