

Spectroscopy and Decay properties of *D* and *D*_s mesons with Martin-like confinement potential in Dirac formalism

P C Vinodkumar*

Department of Physics, Sardar Patel University, Vallabh Vidyanagar- 388 120, Gujarat, INDIA E-mail: p.c.vinodkumar@gmail.com

Manan Shah

Department of Physics, Sardar Patel University, Vallabh Vidyanagar- 388 120, Gujarat, INDIA E-mail: mnshah09@gmail.com

Bhavin Patel

P. D. Patel Institute of Applied Sciences, CHARUSAT, Changa, INDIA E-mail: azadpatel2003@gmail.com

We construct quark - antiquark bound states of open charm mesons by assuming that the constituent quark and antiquark are confined by an average Martin-like potential within the Dirac formalism. On fixing the model parameters using the ground state masses, other excited states of the *D* and *D_s* meson spectra are computed. The corresponding wave functions are then employed to compute the decay constants of *D* and *D_s* meson within the relativistic frame work. These decay constants play an important role in the leptonic and nonleptonic weak decays of the open flavour mesons. The present calculation yields the decay constant of *D* and *D_s* meson as 216.02 MeV and 235.18 MeV respectively as against the experimental values of 206.7 ± 8.9 MeV and 260.0 ± 5.4 MeV respectively. The present results are also in accordance with the QCD sum rule predictions (204 ± 6 MeV and 246 ± 6 MeV) and Lattice QCD (218.9 ± 11.3 MeV and 260.1 ± 10.8 MeV) for *D* and *D_s* mesons respectively. The branching ratio of the leptonic decays of *D* and *D_s* mesons in all the three leptonic channels are also computed and the results are in good agreement with the experimental values particularly in the case of *D_s* meson.

XV International Conference on Hadron Spectroscopy-Hadron 2013 4-8 November 2013 Nara, Japan

*Speaker.

1. Introduction

The recent experimental observations of open flavour mesonic states at charm sector have provided a boost to the theoretical attempts towards the understanding of the dynamics of light quarks in the company of heavy flavour quarks. The colour confinement of quarks is understood in terms of multi-gluon exchange processes at the non-perturbative regime of the hadronic size and it is not feasible to compute theoretically from the QCD first principles. The lattice QCD methods, QCD sum rules and potential models etc. are thus being employed to study the hadronic properties. Though lattice calculations are based on ab-initio method at some excited at some extent, it requires huge computing power and thus limited to the study of hadrons properties mainly to the ground states and few cases where excited states are being studied. In this context, other theoretical models particularly to potential models become a tool to study the properties of hadrons. The masses of heavy-light system for low-lying 1S and $1P_I$ states of D and D_s mesons are known from experiment [1]. Recently, many new resonances of D and D_s systems such as D_0^* (2400), D (2540), D^* (2610), D_s (2638), D_s (2710), D_J (2750), D_J^* (2760), D_s (2860), D_s (3040) are also reported by different experimental groups [2, 3, 4, 5]. But very few of them are comparable with the existing theoretical predictions [6, 7, 8, 9, 10, 11]. In this context, these newly discovered states are very important for theorists to fine tune their models for better understanding of the $Q\bar{q}$ dynamics.

2. Methodology

In the present study, we assume that the constituent quarks in a meson core is independently confined by an average potential of the form

$$V(r) = \frac{1}{2}(1+\gamma_0)(\lambda r^{0.1} + V_0)$$
(2.1)

To a first approximation, the confining part of the interaction is believed to provide the zeroth-order quark dynamics inside the meson through the quark Lagrangian density

$$\mathscr{L}_{q}^{0}(x) = \bar{\psi}_{q}(x) \left[\frac{i}{2} \gamma^{\mu} \overleftrightarrow{\partial_{\mu}} - V(r) - m_{q} \right] \psi_{q}(x).$$
(2.2)

The solution of Dirac equation resulting from the Lagrangian can be written as two component (positive and negative energies in the zeroth order) form as

$$\psi_{nlj}^{(+)}(\vec{r}) = N_{nlj} \begin{pmatrix} ig(r)/r \\ (\sigma.\hat{r})f(r)/r \end{pmatrix} \mathscr{Y}_{ljm}(\hat{r})$$
(2.3)

$$\boldsymbol{\psi}_{nlj}^{(-)}(\vec{r}) = N_{nlj} \begin{pmatrix} i(\boldsymbol{\sigma}.\hat{r})f(r)/r\\g(r)/r \end{pmatrix} (-1)^{j+m_j-l} \mathscr{Y}_{ljm}(\hat{r})$$
(2.4)

Here, N_{nlj} is the overall normalization constant, and $\mathscr{Y}_{ljm}(\hat{r})$ are the solid spherical harmonics and is expressed in terms of the spinor wave functions $\chi_{\frac{1}{2}m_s}$. The reduced radial part g(r) of the upper component and f(r) of the lower component of Dirac spinor $\psi_{nlj}(r)$ are numerically solved and normalized. The optimized model parameters employed for the present study are given below. The quark masses, $m_c = 1.27$ GeV, $m_s = 0.1$ GeV and $m_{u,d} = 0.003$ GeV are taken from PDG [1] while the potential strength (λ) for *D* and *D_s* meson is taken as (2.2903 + B) and (2.2655 + B) *GeV*^{v+1} respectively where the centrifugal parameter (B) is (n + 0.153) *GeV*⁻¹ for *l* = 0 and ((*n*+1)*0.1267) for *l* \neq 0. The constant potential parameter (*V*₀) for *D* and *D_s* is taken as -2.6706 GeV and -2.6160 GeV respectively. The computed mass spectra of *D* and *D_s* mesons are listed in Table 1 below.

D Meson					D_s Meson					
State	Present		Experiment [1]	[8]	[9]	Present		Experiment [1]	[8]	[9]
$1^{3}S_{1}$	2010.4	$D^{*}(2010)$	2010.28 ± 0.13	-	2010	2112.3	D_s^*	2112.3 ± 0.5	-	2111
$1^{1}S_{0}$	1869.6		1869.62 ± 0.15	-	1871	1968.6	D_s	1968.49 ± 0.32	-	1969
$1^{3}P_{2}$	2462.9	$D_2^*(2460)$	2462.6 ± 0.7	-	2460	2571.0	$D_{s2}(2573)$	2571.9 ± 0.8	-	2571
$1^{3}P_{1}$	2390.6			-	2469	2498.8	$D_{s1}(2460)$	2459.6 ± 0.6	-	2574
$1^{3}P_{0}$	2386.4	$D_0^*(2400)$	2318 ± 29	-	2406	2494.5	$D_{s0}^{*}(2317)$	2317.8 ± 0.6	-	2509
$1^{1}P_{1}$	2322.9	$D_1(2420)$	2421.3 ± 0.6	-	2426	2430.20	$D_{s1}(2536)$	2535.12 ± 0.13	-	2536
$2^{3}S_{1}$	2606.2	$D^*(2610)$	2608.7 [4]	2639	2632	2716.4	$D_s^*(2710)$	2710^{+12}_{-7} [2]	2728	2731
$2^{1}S_{0}$	2523.5	D(2540)	2539.4 [4]	2567	2581	2633.3	$D_s(2632)$	$2632.5 \pm 1.7 \ \text{[12]}$	2656	2688
$1^{3}D_{3}$	2835.1	$D_J^*(2760)$	2763.3 [4]	2760	2863	2947.4	$D_{sJ}^{*}(2860)$	2862^{+6}_{-3}	2840	2971
$1^{3}D_{2}$	2817.9			2810	2850	2929.8			2885	2961
$1^{3}D_{1}$	2802.9			2790	2788	2914.5			2870	2913
$1^{1}D_{2}$	2745.3	$D_J(2750)$	2752.4 [4]	2746	2806	2857.2			2828	2931
$2^{3}P_{2}$	2937.9			2965	3012	3051.2			3045	3142
$2^{3}P_{1}$	2891.1			2960	3021	3003.2	$D_{sJ}(3040)$	3044^{+30}_{-9} [3]	3020	3154
$2^{3}P_{0}$	2888.4			2880	2919	3000.4			2970	3054
$2^{1}P_{1}$	2841.9			2940	2932	2954.4			3040	3067
$3^{3}S_{1}$	3148.4			3125	3096	3262.6			3200	3242
$3^{1}S_{0}$	3087.8			3065	3062	3202.0			3140	3219
$2^{3}D_{3}$	3304.6			3212	3335	3419.5			3285	3469
$2^{3}D_{2}$	3292.4			-	3307	3406.9			-	3456
$2^{3}D_{1}$	3281.8			3215	3228	3395.8			3290	3383
$2^{1}D_{2}$	3236.6			-	3259	3351.3			-	3403

Table 1: Mass spectra of $D(c\bar{q}, q = d,u)$ and D_s mesons (in MeV).

3. The Decay constant of the charm flavored mesons

Following the procedure adopted by [13] the decay constant can be expressed through the meson wave function $\psi(p)$ in the momentum space as

$$f_P^2 = \frac{3|I_M|^2}{2\,\pi^2\,M_P\,J_M}\tag{3.1}$$

where

$$I_M = \int_0^\infty dp \ p^2 A(p) \sqrt{g_q(p) \ g_q^*(-p)}, \ J_M = \int_0^\infty dp \ p^2 g_q(p) \ g_q^*(-p)$$

Table 2	2: The	e decay	constant	f_P	of D	systems	(in
MeV).							

			f_P	
	1S	2S	3\$	4S
Present	216.02	185.99	168.14	155.39
Expt./PDG [1]	206.7 ± 8.9			
QCDSR [14]	204 ± 6			
LQCD [15]	218.9 ± 11.3			
LFQM [16]	205.8 ± 8.9			
BSM [17]	230 ± 25			

Table 3: The decay constant f_P of D_s systems (in MeV).

			f_P	
	1S	2S	3S	4S
Present	235.18	203.34	184.40	170.82
Expt./PDG [1]	260.0 ± 5.4			
QCDSR [14]	246 ± 6			
LQCD [15]	260.1 ± 10.8			
LFQM [16]	264.5 ± 17.5			
BSM [17]	248 ± 27			

$$A(p) = \frac{(E_{p_1} + m_{q_1})(E_{p_2} + m_{q_2}) - p^2}{[E_{p_1}E_{p_2}(E_{p_1} + m_{q_1})(E_{p_2} + m_{q_2})]^{\frac{1}{2}}} and E_{p_i} = \sqrt{p^2 + m^2}$$

The computed values are listed in Table 2 and 3.

4. The branching ratio of the leptonic decays of D and D_s mesons

Charged mesons produced from a quark and anti-quark can decay to charged lepton pair via a virtual W^{\pm} boson. The theoretical predications are very clean due to the absence of hadrons in the final state. The total leptonic width of *D* and *D_s* mesons are given by [18, 10, 11]

$$\Gamma(D_q^+ \to l^+ \nu_l) = \frac{G_F^2}{8\pi} f_{D_q}^2 |V_{cq}|^2 m_l^2 \left(1 - \frac{m_l^2}{M_{D_q}^2}\right)^2 M_{D_q} \quad where \ q = s, d, u.$$
(4.1)

where Fermi coupling constant (G_f) is $1.664 * 10^{-5}$ and the relevant CKM parameters are taken from PDG [1] as $V_{cs} = 1.006$ and $V_{cd} = 0.230$. The branching ratios of the total leptonic widths are obtained as $BR = \Gamma(D_q^+ \to \ell^+ \nu_\ell) \times \tau$, where the lifetime τ of the *D* and D_s mesons are taken from PDG [1]. The results are shown in Table 4.

 $\Gamma(M \to \ell \bar{v}_{\ell})$ $B(M \to \ell \bar{\nu}_{\ell})$ [19] Expt.[1] Present [19] Present (keV) (keV) (keV) (keV) Process $D_s \rightarrow \tau \bar{\nu_{\tau}}$ 13.258 × 10⁻⁸ 6.090 × 10⁻⁸ 5.844 × 10⁻² 4.3 × 10⁻² 5.43 × 10⁻² $D_s \rightarrow \mu \bar{v_{\mu}}$ 13.469 × 10⁻⁹ 6.240 × 10⁻⁹ **5.937** × 10⁻³ 4.41 × 10⁻³ 5.90 × 10⁻³ $D_s \rightarrow e \bar{v_e}$ 3.157 × 10⁻¹³ 1.391×10^{-7} - $< 1.2 \times 10^{-4}$ _ $D^+ \rightarrow \tau \bar{v_{\tau}}$ 15.288 × 10⁻¹⁰ 4.720 × 10⁻¹⁰ 2.433 × 10⁻³ 7.54 × 10⁻⁴ < 1.2 × 10⁻³ $D^+ \to \mu \bar{\nu_{\mu}} \ 5.641 \times 10^{-10} \ 1.795 \times 10^{-10} \ 8.977 \times 10^{-4} \ 2.87 \times 10^{-4} \ 3.82 \times 10^{-4}$ 2.105×10^{-8} $D^+ \rightarrow e \bar{v_e}$ 1.323 × 10⁻¹⁴ _ _ $< 8.8 \times 10^{-6}$

Table 4: The leptonic Branching Ratio (BR) of D and D_s mesons.

5. Results and Discussions

The predicted masses of S-wave of D_s meson state 2 ${}^{3}S_1$ (2716 MeV) and 2 ${}^{1}S_0$ (2633 MeV) are in very good agreement with experimental results 2710_{-7}^{+12} MeV [1] and 2638 MeV [12] respectively. $2{}^{3}S_1$ (2606 MeV) state and $2{}^{1}S_0$ (2523 MeV) of *D* meson are in good agreement with experimental [1] values of 2608 MeV and 2539 MeV reported by BABAR [4]. The expected results of other S-wave excited states of *D* and D_s meson are in accordance with the other results [8, 9]. The decay constant of *D* meson 216 MeV and D_s meson 235 MeV are also in agreement with the LQCD [15] result and with the QCD sum rule result [14] respectively. The predicted leptonic branching ratios of the D_s meson are in excellent agreement with the experimental results over other theoretical predictions [19].

6. Acknowledgements

The work is part of a Major research project NO. F.40-457/2011(SR) funded by UGC,INDIA. One of the authors (BP) acknowledges the support through Fast Track project (SR/FTP/PS-52/2011) funded by Department of Science and Technology (DST) and we thank DST and the organizers for their support during the conference.

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