

Description of $\rho(1700)$ with the FCA method

M. Bayar,^{ab} W. H. Liang,^{ac} T. Uchino^{*a} and C. W. Xiao^a

^a *Departamento de Física Teórica and IFIC, Centro Mixto Universidad de Valencia-CSIC, Institutos de Investigación de Paterna, Apartado 22085, 46071 Valencia, Spain*

^b *Department of Physics, Kocaeli University, 41380, Izmit, Turkey*

^c *Department of Physics, Guangxi Normal University, Guilin, 541004, P. R. China*

E-mail: melahat.bayar@kocaeli.edu.tr, liangwh@gxnu.edu.cn, uchino@ific.uv.es, chuwen.xiao@ific.uv.es

We study the $\rho K\bar{K}$ system with an aim to describe the $\rho(1700)$ resonance. The chiral unitary approach has achieved success in a description of systems of the light hadron sector. With this method, the $K\bar{K}$ system in the isospin sector $I = 0$, is found to be a dominant component of the $f_0(980)$ resonance. Therefore, by regarding the $K\bar{K}$ system as a cluster, the $f_0(980)$ resonance, we evaluate the $\rho K\bar{K}$ system applying the fixed center approximation to the Faddeev equations. We construct the ρK unitarized amplitude using the chiral unitary approach. As a result, we find a peak in the three-body amplitude around 1739 MeV and a width of about 227 MeV. The effect of the width of ρ and $f_0(980)$ is also discussed. We associate this peak to the $\rho(1700)$ which has a mass of 1720 ± 20 MeV and a width of 250 ± 100 MeV.

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*Speaker.

We study the $\rho K\bar{K}$ system in the sector $I(J^P) = 1(1^-)$ within the fixed center approximation (FCA) to obtain the $\rho(1700)$ resonance. A pair of $K\bar{K}$ is assumed to form the scalar cluster, the $f_0(980)$ resonance because the $K\bar{K}$ component in $f_0(980)$ is found to be dominant [1]. In order to obtain the unitarized ρK amplitude, we follow the schemes given by refs. [2, 3] and extend them to the isospin $I = 3/2$ sector. Basically we follow the formalism given by refs. [4, 5, 6, 7].

To implement the Faddeev equation within the fixed center approximation, we need the ρK ($\rho\bar{K}$) unitarized amplitude. Here we utilize the amplitude given in the previous work [2, 3] as to the vector-pseudoscalar interaction in the sector with strangeness $S = 1$ and isospin $I = 1/2$. Following the Bethe-Salpeter approach, we have the VP two-body scattering amplitude as

$$T = [1 + V\hat{G}]^{-1}(-V)\vec{\epsilon} \cdot \vec{\epsilon}', \quad (1)$$

where V is an interaction kernel which will be discussed later, \hat{G} is $(1 + \frac{1}{3}\frac{q_l^2}{M_l^2})G$ being a diagonal matrix and $\vec{\epsilon}(\vec{\epsilon}')$ represents a polarization vector of the incoming (outgoing) vector-meson. Thanks to the on-shell factorization and the dimensional regularization, a loop function of pseudoscalar and vector mesons G_l can be expressed as a function of the energy \sqrt{s}

$$G_l(\sqrt{s}) = \frac{1}{16\pi^2} \left\{ a(\mu) + \ln \frac{M_l^2}{\mu^2} + \frac{m_l^2 - M_l^2 + s}{2s} \ln \frac{m_l^2}{M_l^2} \right. \\ \left. + \frac{q_l}{\sqrt{s}} [\ln(s - (M_l^2 - m_l^2) + 2q_l\sqrt{s}) + \ln(s + (M_l^2 - m_l^2) + 2q_l\sqrt{s}) \right. \\ \left. - \ln(-s + (M_l^2 - m_l^2) + 2q_l\sqrt{s}) - \ln(-s - (M_l^2 - m_l^2) + 2q_l\sqrt{s})] \right\}, \quad (2)$$

where a momentum q_l is determined at the center of mass frame and μ is a scale parameter in this scheme. Furthermore in accordance with ref. [3], we take into account the effect of the propagation of unstable particles in terms of the Lehmann representation. Instead of the original loop function eq. (2), we use

$$\tilde{G}_l(\sqrt{s}) = \frac{1}{C_l} \int_{(M_l - 2\Gamma_l)^2}^{(M_l + 2\Gamma_l)^2} ds_V G_l(\sqrt{s}, \sqrt{s_V}, m_l) \times \left(-\frac{1}{\pi} \right) \text{Im} \left\{ \frac{1}{s_V - M_l^2 + iM_l\Gamma_l} \right\}, \quad (3)$$

with the normalization for the l th component

$$C_l = \int_{(M_l - 2\Gamma_l)^2}^{(M_l + 2\Gamma_l)^2} ds_V \times \left(-\frac{1}{\pi} \right) \text{Im} \left\{ \frac{1}{s_V - M_l^2 + iM_l\Gamma_l} \right\}, \quad (4)$$

with m_l , M_l , Γ_l , the mass of the pseudoscalar meson, mass of the vector and width of the vector respectively. We can obtain the interaction kernel V by the use of the WCCWZ approach [8, 9, 10] where the interaction Lagrangian stems from a nonlinear realization of chiral symmetry. By projecting over s -wave, we have the VP potential

$$V_{ij}(s) = -\frac{\vec{\epsilon} \cdot \vec{\epsilon}'}{8f^2} C_{ij} \left[3s - (M_i^2 + m_i^2 + M_j^2 + m_j^2) - \frac{1}{s} (M_i^2 - m_i^2)(M_j^2 - m_j^2) \right], \quad (5)$$

where the index $i(j)$ represents the VP channel of the incoming (outgoing) particles. The coefficients C_{ij} in eq. (5) for the $I = 1/2$ and $I = 3/2$ sector are tabulated in tables 1 and 2 respectively.

	ϕK	ωK	ρK	$K^* \eta$	$K^* \pi$
ϕK	0	0	0	$-\sqrt{\frac{3}{2}}$	$-\sqrt{\frac{3}{2}}$
ωK	0	0	0	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{3}}{2}$
ρK	0	0	-2	$-\frac{3}{2}$	$\frac{1}{2}$
$K^* \eta$	$-\sqrt{\frac{3}{2}}$	$\frac{\sqrt{3}}{2}$	$-\frac{3}{2}$	0	0
$K^* \pi$	$-\sqrt{\frac{3}{2}}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	0	-2

Table 1: Coefficients C_{ij} in the $I = 1/2$ sector.

	ρK	$K^* \pi$
ρK	1	1
$K^* \pi$	1	1

Table 2: Coefficients C_{ij} in the $I = 3/2$ sector.

In order to have an appropriate unitarized amplitude, we use the following parameter set chosen to reproduce $K_1(1270)$ in ref. [3] as $\mu = 900$ MeV, $a(\mu) = -1.85$, $f = 115$ MeV .

Under the fixed center approximation [4, 5, 6, 7], it is assumed that K and \bar{K} cluster together and the structure of the cluster is kept against the collision of ρ . This idea leads the three-body scattering amplitude T which can read a summation of the two following partition functions T_1 and T_2

$$\begin{aligned}
T_1 &= t_1 + t_1 G_0 T_2, \\
T_2 &= t_2 + t_2 G_0 T_1, \\
T &= T_1 + T_2,
\end{aligned} \tag{6}$$

where the subscripts $i = 1(2)$ of T_i and t_i represent the component particle $K(\bar{K})$ in the cluster and the diagrammatic sketches are depicted in fig. 1. In the present work, we can rewrite $t = t_1 = t_2$ and t is given as a mixture of the different isospin states of $I = 1/2$ and $I = 3/2$, $t = (2t_{\rho K}^{I=3/2} + t_{\rho K}^{I=1/2})/3$, where $t_{\rho K}$ is the ρK unitarized scattering amplitude given by eq. (1). By adopting the field normalization used in refs. [5, 6, 7], G_0 of eq. (6) reads as a function of the energy \sqrt{s}

$$G_0(\sqrt{s}) = \frac{1}{2M_{f_0}} \int \frac{d^3 q}{(2\pi)^3} F_{f_0}(q) \frac{1}{q^{02}(s) - \vec{q}^2 - m_\rho^2 + im_\rho \Gamma_\rho}, \tag{7}$$

where M_{f_0} is the mass of the $f_0(980)$ resonance and the width of the ρ is taken into account in the above propagator. The energy of the propagator q^0 is determined at the three-body rest frame, $q^0(\sqrt{s}) = (s + m_\rho^2 - M_{f_0}^2)/2\sqrt{s}$. Here we utilize the form factor F_{f_0} to give the momentum distribution of f_0 to the G_0 function by the use of the formalism developed in refs. [11, 12, 13]

$$F_{f_0}(q) = \frac{1}{\mathcal{N}} \int_{|\vec{p}-\vec{q}| < k_{\max}}^{p < k_{\max}} d^3 p \left(\frac{1}{2\omega_K(\vec{p})} \right)^2 \frac{1}{M_{f_0} - 2\omega_K(\vec{p})}$$

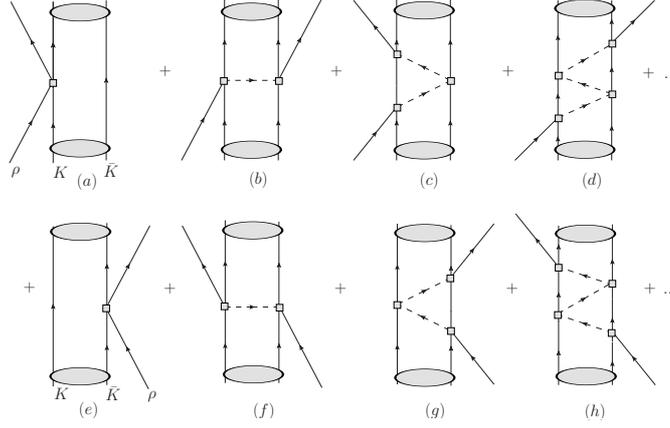


Figure 1: Diagrammatic representation of the fixed center approximation for the $\rho K\bar{K}$ system.

$$\times \left(\frac{1}{2\omega_K(\vec{p}-\vec{q})} \right)^2 \frac{1}{M_{f_0} - 2\omega_K(\vec{p}-\vec{q})}, \quad (8)$$

where the normalization \mathcal{N} is given by

$$\mathcal{N} = \int_{p < k_{\max}} d^3 p \left[\left(\frac{1}{2\omega_K(\vec{p})} \right)^2 \frac{1}{M_{f_0} - 2\omega_K(\vec{p})} \right]^2. \quad (9)$$

From ref. [1], we take $k_{\max} = \sqrt{\Lambda^2 - m_K^2}$ and $\Lambda = 1030$ MeV for getting the $f_0(980)$ from the $K\bar{K}$ cluster. Considering the S -matrix, we have a simple expression of the three-body scattering amplitude

$$T(s) = 2 [\tilde{t}(s') + \tilde{t}(s')G_0(s)\tilde{t}(s') + \dots] = 2 \frac{\tilde{t}(s')}{1 - \tilde{t}(s')G_0(s)}, \quad (10)$$

where t is replaced by $\tilde{t} = (2m_{f_0}/2m_K)t$ coming from the normalization of the fields and note that the unitarized amplitude t is a function of $s' = 1/2(s + M_\rho^2 + 2m_K^2 - M_{f_0}^2)$. Finally we consider the width of f_0 by replacing the mass of the cluster M_{f_0} in eqs. (8) and (9) with $M_{f_0} - i\Gamma_{f_0}/2$. The amplitude with the $f_0(980)$ and ρ width effect is shown in fig. 2 and the masses and widths of the dynamically generated state are listed in table 3. It is shown that the inclusion of the $f_0(980)$ width induces a suppression of the magnitude of the peak and the peak becomes broader as the width of the $f_0(980)$ increases. Furthermore it is also a remarkable feature that the peak position is not so affected by this prescription.

Through this work, we construct the $\rho K\bar{K}$ three-body amplitude by means of the fixed center approximation. In our framework, a pair of $K\bar{K}$ is considered to form a scalar meson cluster $f_0(980)$, based on ref. [1]. We use the ρK unitarized amplitude provided by refs. [2, 3] in a manner giving a respect to chiral symmetry. In the three-body amplitude, we have a peak at the energy around 1748 MeV rather independent of the width of the $f_0(980)$. Besides, it is seen that the inclusion of the $f_0(980)$ width makes the peak wider and gives a good agreement with the

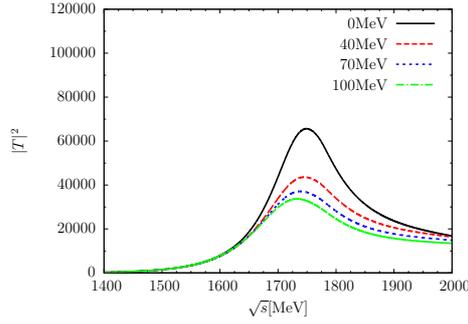


Figure 2: The $\rho K\bar{K}$ amplitude with the width effect for $\Gamma_{f_0} = 0, 40, 70, 100$ MeV, respectively.

	$\Gamma_{f_0} = 0$	$\Gamma_{f_0} = 40$	$\Gamma_{f_0} = 70$	$\Gamma_{f_0} = 100$	PDG [14]
Mass	1748.0	1743.6	1739.2	1734.8	1720 ± 20
Width	160.8	216.4	227.2	224.6	250 ± 100

Table 3: The masses and widths of dynamically generated states with the width effects. (in MeV)

experimental data of the $\rho(1700)$, both for the position and the width. Since the ρ decays into $\pi\pi$ mostly, the above results might be related to the dominant decay mode of the $\rho(1700)$, $\rho\pi\pi$ and 4π . Our approach to the $\rho K\bar{K}$ system provides the description of the $\rho(1700)$ as a dynamically generated state and then we conclude that the building block of the $\rho(1700)$ resonance are the ρ and $f_0(980)$.

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