

# Three-loop beta function for the Higgs self-coupling

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> In the last two years the renormalization group functions for the couplings and fields of the Standard Model have been computed at three-loop level [1–7]. The evolution of the self-coupling  $\lambda$ of the Standard Model Higgs boson is of particular importance due to its close connection with the stability of the Standard Model vacuum state. In this talk the three-loop corrections to the  $\beta$ -function for this crucial coupling are discussed.

> The calculation of three-loop  $\beta$ -functions and anomalous dimensions poses special technical challenges, such as the huge number of diagrams and the proper treatment of  $\gamma_5$  in dimensional regularization. In order to avoid infrared divergences resulting from setting external momenta to zero in the case of the Higgs self-coupling an auxiliary mass is used to compute the ultraviolet divergences needed for the renormalization constants. This method, first suggested in [8], is explained in some detail.

Finally, an update for the status of the vacuum stability problem in the Standard Model up to the Planck scale is presented.

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# 1. Motivation: The vacuum stability problem

The Standard Model of particle physics describes the interactions of fermions through the exchange of gauge bosons. In the covariant derivative

$$D^{\mu} = \partial^{\mu} - ig_1 Y B^{\mu} - i \frac{g_2}{2} \sigma^a W^{a\mu} - ig_s T^a A^{a\mu}.$$
(1.1)

the three gauge couplings  $g_s$ ,  $g_2$  and  $g_1$  of the  $SU(3) \times SU(2) \times U(1)$  group are defined.<sup>1</sup> In addition to the fermions and gauge bosons a scalar SU(2) doublet is introduced which aquires a vacuum expectation value (VEV) at the electroweak scale  $v \approx 246.2$  GeV. The fermion masses and the Higgs-fermion interaction are derived from the Yukawa sector of the Standard Model and the Higgs self-interaction is introduced to the Lagrangian in the classical Higgs potential

$$V(|\Phi|) = \left(m^2 \Phi^{\dagger} \Phi + \lambda \left(\Phi^{\dagger} \Phi\right)^2\right), \quad \Phi = \left(\begin{array}{c} \Phi_1\\ \Phi_2 \end{array}\right). \tag{1.2}$$

After spontaneous symmetry breaking we have the classical field strength

$$\Phi_{\rm cl} := \langle 0|\Phi|0\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0\\v \end{pmatrix}$$
(1.3)

and describe excitations from the ground state with four quantum fields, the Higgs field *H* and three Goldstone bosons  $\chi$ ,  $\Phi^{\pm}$ :

$$\Phi = \begin{pmatrix} \Phi_1 \\ \Phi_2 \end{pmatrix} \underbrace{\text{SSB}}_{\longrightarrow} \begin{pmatrix} \Phi^+ \\ \frac{1}{\sqrt{2}}(\nu + H - i\chi) \end{pmatrix}.$$
(1.4)

Due to radiative corrections the effective couplings evolve with the renormalization scale and we have to consider the effective Higgs potential [9] instead of the classical one. The effective potential develops a second minimum at high classical field strengths  $|\Phi_{cl}|$  if we extrapolate the Standard Model up to e.g. the Planck scale  $M_{\text{Planck}} \sim 10^{19}$  GeV. In the absence of physics beyond the Standard Model at the LHC so far this is a conceivable scenario. The effective potential is a function of  $\Phi_{cl}$  and is affected by the self-interactions of the scalar fields as well as the interactions of the scalar fields with all other fields. Hence it depends on all couplings of the theory.



Figure 1: Classical and effective Higgs potential

 $<sup>{}^{1}</sup>B^{\mu}$ ,  $W^{a\mu}$  and  $A^{a\mu}$  are the gauge fields of SU(3), SU(2) and U(1) respectively,  $\sigma^{a}$  are the Pauli matrices,  $T^{a}$  are the generators of SU(3) and Y the U(1) hypercharge of the field on which  $D^{\mu}$  acts.

Generic shapes of the classical Higgs potential and of the effective potential are shown in Fig. 1 for the cases of a Higgs mass larger and smaller than a critical value  $m_{\min}$ , the minimal stability bound. For  $M_{\rm H} > m_{\min}$  the second minimum is higher than the one at the electroweak scale and therefore the vacuum state with  $|\Phi_{\rm el}| = \frac{v}{\sqrt{2}}$  is stable. However, for  $M_{\rm H} < m_{\min}$  the second minimum is energetically favoured and the electroweak vacuum state is not stable against decay into this global ground state. Depending on whether the lifetime of the electroweak vacuum state is shorter or longer than the age of the universe this is called an unstable or metastable scenario. It has been demonstrated that the stability of the Standard Model vacuum is in good approximation equivalent to the question whether the Higgs self-interaction  $\lambda$  stays positive up to the maximum validity scale of the theory, e.g.  $M_{\rm Planck}$  [10–12]. A detailed analysis of the vacuum stability problem in the Standard Model can be found in [3, 13–20].

The evolution of any coupling is described by the respective  $\beta$ -function

$$\beta_X(\lambda, y_t, g_s, g_2, g_1) = \mu^2 \frac{d}{d\mu^2} X(\mu), \quad X \in \{\lambda, y_t, g_s, g_2, g_1\}.$$
(1.5)

Every  $\beta$ -function is a power series in all couplings of the theory which is why the  $\beta$ -functions for all numerically relevant couplings are needed. Recently, the  $\beta$ -functions for the gauge couplings [1,2,5], Yukawa couplings [3,7] and for the Higgs self-interaction [3,4,6] have been computed at three-loop level.

In order to determine the evolution of  $\lambda$  the coupled system of differential equations (1.5) needs to be solved using initial conditions for all couplings, e.g. their value at the scale of the top pole mass. In table 1 the values for the numerically largest couplings are given at this scale. These are derived by matching the experimentally accessible parameters  $G_F$ ,  $M_t$ ,  $M_H$ ,  $M_W$ ,  $M_Z$  and  $\alpha_s^{\overline{MS}}(M_Z)$  to the  $\overline{MS}$ -parameters  $g_s(M_t)$ ,  $g_2(M_t)$ ,  $g_1(M_t)$ ,  $y_t(M_t)$  and  $\lambda(M_t)$ . One-loop [21–23] and two-loop corrections [13, 15, 24–30] to this matching are taken into account. Except for  $y_t$  the Yukawa interactions  $y_b$ ,  $y_c$ , etc. can be neglected in this context due to their smallness. The same applies to the off-diagonal entries of the Yukawa matrices.

# 2. Calculating the $\beta$ -function for the Higgs self-interaction with an auxiliary mass

The  $\beta$ -function of a coupling is computed in dimensional regularization from the renormalization constant of a vertex proportional to this coupling and the renormalization constants for the external fields of this vertex. The calculation is performed in the unbroken phase of the Standard

coupling	value for $\mu = M_t$
$g_s$	1.1666
<i>8</i> 2	0.6483
$g_1$	0.3587
λ	0.1276
$y_t$	0.9369

**Table 1:** Standard Model couplings at the top pole mass scale for  $M_t = 173.34$  GeV [31],  $M_H = 125.9$  GeV [32–34] und  $\alpha_s(M_Z) = 0.1184$  [35] using the on-shell to  $\overline{\text{MS}}$ -relations given in [13].



**Figure 2:** One-loop diagrams contributing to the renormalization of the  $\Phi_1^4$ -vertex: An IR singularity appears in (c) if two external momenta are set to zero.

Model and the results are given in the  $\overline{\text{MS}}$ -scheme. There are many challenges to the computation of the three-loop  $\beta$ -function for the Higgs self-interaction. One is the huge number of Feynman diagrams, 573692 for the  $\Phi_1^4$ -vertex even if we factorize the full gauge group factor from the momentum space factor for each diagram (for details see [4]). Another issue is the proper treatment of  $\gamma_5$  in dimensional regularization. Whereas a naive treatment of  $\gamma_5$  does not work for the computation of  $\beta_{\gamma_t}$  we have shown in [3,4] that a naive treatment is sufficient for  $\beta_{\lambda}$  at three-loop level.

In the case of corrections to the quartic scalar vertex a problem arises already at one-loop level if we compute the renormalization constant setting two external momenta to zero and then evaluating propagator-like massless diagrams. In Fig. 2 we see that diagram (c) has an UV divergence as well as an IR one which cancel to give zero for the whole diagram. In order to avoid the IR singularity and to retrieve the correct contribution to the UV renormalization constant we introduce an auxiliary mass in the denominator of every propagator. Then we Taylor expand in the external momenta as far as needed in order to factorize the kinematic structure of the Greens function which we want to compute, e.g.  $q^2g^{\mu\nu} - q^{\mu}q^{\nu}$  for the gluon propagator. Now we can set the external momenta in the scalar part of the Greens function to zero because the UV divergence does not depend on those.

This method was suggested in [8] and further developed in [36]. In order to see why this method works let us consider the following decomposition of a propagator denominator [36]:

$$\frac{1}{(l+q)^2} = \frac{1}{l^2 - M^2} + \frac{-q^2 - 2l \cdot q - M^2}{l^2 - M^2} \frac{1}{(l+q)^2},$$
(2.1)

where l is a linear combination of loop momenta and q of external momenta. Using this formula recursively leads to the last term, which has q in the denominator, contributing only to the finite part of the integral because the power of the denominator is increased with every recursion. We consider now the case where two iterations are enough:

$$\frac{1}{(l+q)^2} = \frac{1}{l^2 - M^2} + \frac{-q^2 - 2l \cdot q}{(l^2 - M^2)^2} + \frac{(-q^2 - 2l \cdot q)^2}{(l^2 - M^2)^3} - \frac{M^2}{(l^2 - M^2)^2} + \frac{M^2(M^2 + 2q^2 + 4l \cdot q)}{(l^2 - M^2)^3} + \frac{(-q^2 - 2l \cdot q - M^2)^3}{(l^2 - M^2)^3} \frac{1}{(l+q)^2}.$$
(2.2)

This decomposition is exact and hence using the left side of (2.2) for every propagator denominator would give the correct and  $M^2$ -independent result. As we are only interested in the UV divergent



**Figure 3:** A divergent subgraph (a) with terms  $\propto M^2$  and  $\propto l^2$  leads to an  $M^2$ -independent but wrong contribution in (b) as the rest of the diagram produces a term  $\propto \frac{1}{M^2}$ . This must be compensated by a mass counterterm (c).

part of the integral we neglect the last term in (2.2). Furthermore, we notice that the first line of (2.2) is exactly the Taylor expansion in the external momenta mentioned above.

If we do not use this exact decomposition but simply put  $M^2$  in every propagator denominator and expand in the external momenta we neglect exactly the terms  $\propto M^2$  in the second line of (2.2). At one-loop level this is not a problem because we know that the exact result does not depend on  $M^2$ . We can therefore reconstruct the contribution from the terms  $\propto M^2$  in (2.2) as counterterms to the  $M^2$ -terms in our result.

These counterterms become important at higher orders where a divergent subgraph with a term  $\propto \frac{M^2}{\varepsilon}$  is multiplied with a term  $\propto \frac{1}{M^2}$  from the rest of the full diagram. Hence the wrong contribution  $\propto \frac{M^2}{\varepsilon}$  from the subgraph is not identifiable in the final result. This can be avoided by applying all possible counterterms  $\propto M^2$  which have been computed in lower orders. Using these counterterms  $\propto M^2$  we restore the  $M^2$ -terms of the exact decomposition (2.2) order by order in perturbation theory. An example is shown in Fig. 3. The one-loop diagram (a) has a divergent part  $\frac{l^2}{\varepsilon}C_{l^2} + \frac{M^2}{\varepsilon}C_{M^2}$  if we introduce the auxiliary mass  $M^2$  in the denominators of the two propagators and Taylor expand in the external momentum l. Only the scalar part  $C_{l^2}$  is needed in order to renormalize the Lagrangian of the (massless) theory. The counterterm  $M^2 \delta Z_{M^2}^{(2\Phi)} = -\frac{M^2}{\varepsilon} C_{M^2}$  however is needed at two-loop level in order to insure that only the part  $\frac{l^2}{\varepsilon} C_{l^2}$  of the subdiagram (a) of the full diagram (b) contributes to the final result.

To summarize the method, we introduce an auxiliary mass in every propagator denominator, expand in the external momenta as far as needed for the kinematic structure of the considered Greens function before setting them to zero in the scalar part of the Greens function. Then the UV divergent part of the Greens function is computed order in order in perturbation theory by evaluating massive Tadpole diagrams, for which we use MATAD [37]. In order to get the correct result we have to apply all possible regular UV counterterms as well as all possible counterterms  $\propto M^2$  to the lower order diagrams. In the Standard Model they have the form

$$\frac{M^2}{2} \delta Z_{M^2}^{(2g)} A^a_\mu A^{a\mu}, \quad \frac{M^2}{2} \delta Z_{M^2}^{(2W)} W^a_\mu W^{a\mu}, \quad \frac{M^2}{2} \delta Z_{M^2}^{(2B)} B_\mu B^\mu, \quad M^2 \delta Z_{M^2}^{(2\Phi)} \Phi^\dagger \Phi.$$
(2.3)

Other counterterms  $\propto M^2$  and of mass dimension four can not be constructed. For fermions this is obvious, for ghosts this is because of the kinematic structure of the ghost vertex which is al-

ways proportional to a momentum making only kinetic counterterms  $\propto (\partial_{\mu} \bar{c}^a)(\partial^{\mu} c^a)$  and no term  $\propto M^2 \bar{c}^a c^a$  possible.

Note, that the mass  $M^2$  is introduced by hand at the level of integrands and is not a parameter of the theory. Hence these counterterms do not appear in the Lagrangian and gauge invariance of the theory is not spoiled. The whole procedure is a mathematical trick to reduce the problem of UV renormalization counterterms to computing massive tadpoles with one scale.

The results of the calculation of the three-loop  $\beta$ -function for the Higgs self-interaction have been published in [3,4].

#### 3. The evolution of the Higgs self-coupling and vacuum stability

The evolution of  $\lambda$  up to the Planck scale  $M_{Planck} \sim 10^{19}$  GeV using the  $\beta$ -functions for  $\lambda, y_t, g_s, g_2$  and  $g_1$  as well as the initial conditions from Tab. 1 is shown in Fig. 4. Whereas the difference between the evolution using two-loop  $\beta$ -functions and the one using one-loop  $\beta$ -functions is significant, the curves for three-loop  $\beta$ -functions and two-loop  $\beta$ -functions are very close. The difference between these two curves represents the theoretical uncertainty stemming from truncating the perturbation series of the  $\beta$ -functions. This can be compared to the theoretical uncertainties stemming from the matching of on-shell to  $\overline{\text{MS}}$ -parameters which are of similar size [20] and to the uncertainties of the experimental input parameters. Here the main uncertainty stems from the top mass. In Fig. 4 we see the three-loop evolution of  $\lambda$  for the top pole mass shifted by one  $\sigma = 0.76$  GeV [31]. The uncertainties stemming from the Higgs mass and  $\alpha_s$  measurement are



**Figure 4:** Evolution of  $\lambda$  using 1, 2 and 3 loop  $\beta$ -functions, top mass uncertainty

significantly smaller than the one from the top mass but still larger than the theoretical ones (see e.g. [20]).

The stability of the electroweak vacuum state is a fundamental issue if the Standard Model extrapolated to high energies. In the absence of new physics the Higgs self coupling becomes negative at  $\text{Log}_{10} \left(\frac{\mu}{\text{GeV}}\right) \approx 10.36$  for the best fit input parameters. This makes a metastable scenario the most likely for the Standard Model up to the Planck scale. Due to the calculation of three-loop  $\beta$ -functions for the Higgs self-interaction and the other Standard Model couplings as well as due to improved precision in the matching relations between on-shell and  $\overline{\text{MS}}$ -parameters the theoretical uncertainties are well under control. A more precise measurement of the experimental input parameters, especially of the top mass at a linear e<sup>+</sup>e<sup>-</sup>-collider, is necessary to clarify this issue with certainty.

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# References

- L. N. Mihaila, J. Salomon, and M. Steinhauser, *Gauge coupling beta functions in the standard model to three loops*. Phys. Rev. Lett. **108** (2012) 151602.
- [2] L. N. Mihaila, J. Salomon, and M. Steinhauser, *Renormalization constants and beta functions for the gauge couplings of the Standard Model to three-loop order*. Phys. Rev. D 86 (2012) 096008, arXiv:1208.3357 [hep-ph].
- [3] K. Chetyrkin and M. Zoller, *Three-loop* β-functions for top-Yukawa and the Higgs self-interaction in the Standard Model. JHEP **1206** (2012) 033, arXiv:1205.2892 [hep-ph].
- [4] K. Chetyrkin and M. Zoller, β-function for the Higgs self-interaction in the Standard Model at three-loop level. JHEP 1304 (2013) 091, arXiv:1303.2890 [hep-ph].
- [5] A. Bednyakov, A. Pikelner, and V. Velizhanin, Anomalous dimensions of gauge fields and gauge coupling beta-functions in the Standard Model at three loops. JHEP 1301 (2013) 017, arXiv:1210.6873 [hep-ph].
- [6] A. Bednyakov, A. Pikelner, and V. Velizhanin, *Higgs self-coupling beta-function in the Standard Model at three loops*. Nucl. Phys. **B875** (2013) 552–565, arXiv:1303.4364.
- [7] A. Bednyakov, A. Pikelner, and V. Velizhanin, *Yukawa coupling beta-functions in the Standard Model at three loops*. Phys.Lett. **B722** (2013) 336–340, arXiv:1212.6829.
- [8] M. Misiak and M. Münz, Two loop mixing of dimension five flavor changing operators. Phys. Lett. B344 (1995) 308–318, arXiv:hep-ph/9409454.
- [9] S. Coleman and E. Weinberg, *Radiative Corrections as the Origin of Spontaneous Symmetry Breaking*. Phys. Rev. D 7 (1973) 1888–1910.

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- [10] G. Altarelli and G. Isidori, Lower limit on the Higgs mass in the standard model: An update. Physics Letters B 337 (1994) no.~1-2, 141–144.
- [11] N. Cabibbo, L. Maiani, G. Parisi, and R. Petronzio, Bounds on the Fermions and Higgs Boson Masses in Grand Unified Theories. Nucl. Phys. B158 (1979) 295–305.
- [12] C. Ford, D. Jones, P. Stephenson, and M. Einhorn, *The effective potential and the renormalization group*. Nucl. Phys. B395 (1993) 17–34, arXiv:hep-lat/9210033 [hep-lat].
- [13] D. Buttazzo, G. Degrassi, P. P. Giardino, G. F. Giudice, F. Sala, et al., Investigating the near-criticality of the Higgs boson. arXiv:1307.3536 [hep-ph].
- [14] I. Masina, *Higgs boson and top quark masses as tests of electroweak vacuum stability*. Phys. Rev. D87 (2013) no.~5, 053001, arXiv:1209.0393 [hep-ph].
- [15] F. Bezrukov, M. Y. Kalmykov, B. A. Kniehl, and M. Shaposhnikov, *Higgs Boson Mass and New Physics*. JHEP **1210** (2012) 140, arXiv:1205.2893 [hep-ph].
- [16] G. Degrassi, S. Di Vita, J. Elias-Miro, J. R. Espinosa, G. F. Giudice, et al., Higgs mass and vacuum stability in the Standard Model at NNLO. JHEP 1208 (2012) 098, arXiv:1205.6497 [hep-ph].
- [17] M. Zoller, Vacuum stability in the SM and the three-loop  $\beta$ -function for the Higgs self-interaction. arXiv:1209.5609 [hep-ph].
- [18] J. Elias-Miro, J. R. Espinosa, G. F. Giudice, G. Isidori, A. Riotto, et al., Higgs mass implications on the stability of the electroweak vacuum. Phys. Lett. B709 (2012) 222–228, arXiv:1112.3022 [hep-ph].
- [19] M. Holthausen, K. S. Lim, and M. Lindner, *Planck scale Boundary Conditions and the Higgs Mass.* JHEP 1202 (2012) 037, arXiv:1112.2415 [hep-ph].
- [20] M. Zoller, *Beta-function for the Higgs self-interaction in the Standard Model at three-loop level.* PoS (EPS-HEP 2013) 322, arXiv:1311.5085 [hep-ph].
- [21] R. Tarrach, The Pole Mass in Perturbative QCD. Nucl. Phys. B183 (1981) 384.
- [22] A. Sirlin and R. Zucchini, Dependence of the Higgs coupling hMS(M) on mH and the possible onset of new physics. Nucl. Phys. B 266 (1986) no.~2, 389–409.
- [23] R. Hempfling and B. A. Kniehl, On the relation between the fermion pole mass and MS Yukawa coupling in the standard model. Phys. Rev. D51 (1995) 1386–1394, arXiv:hep-ph/9408313 [hep-ph].
- [24] N. Gray, D. J. Broadhurst, W. Grafe, and K. Schilcher, *Three Loop Relation of Quark (Modified) Ms and Pole Masses*. Z. Phys. C48 (1990) 673–680.
- [25] F. Jegerlehner, M. Y. Kalmykov, and O. Veretin, *MS versus pole masses of gauge bosons: Electroweak bosonic two loop corrections*. Nucl. Phys. B641 (2002) 285–326, arXiv:hep-ph/0105304 [hep-ph].
- [26] F. Jegerlehner, M. Y. Kalmykov, and O. Veretin, *MS-bar versus pole masses of gauge bosons. 2. Two loop electroweak fermion corrections*. Nucl. Phys. B658 (2003) 49–112, arXiv:hep-ph/0212319 [hep-ph].
- [27] M. Faisst, J. H. Kühn, T. Seidensticker, and O. Veretin, *Three loop top quark contributions to the rho parameter*. Nucl. Phys. B665 (2003) 649–662, arXiv:hep-ph/0302275 [hep-ph].

- [28] D. Eiras and M. Steinhauser, Two-loop O(alpha alpha(s)) corrections to the on-shell fermion propagator in the standard model. JHEP 0602 (2006) 010, arXiv:hep-ph/0512099 [hep-ph].
- [29] F. Jegerlehner and M. Y. Kalmykov, O(alpha alpha(s)) correction to the pole mass of the t quark within the standard model. Nucl. Phys. B676 (2004) 365–389, arXiv:hep-ph/0308216 [hep-ph].
- [30] B. A. Kniehl and O. L. Veretin, *Two-loop electroweak threshold corrections to the bottom and top Yukawa couplings*. arXiv:1401.1844 [hep-ph].
- [31] ATLAS, CDF, CMS, D0 Collaboration, First combination of Tevatron and LHC measurements of the top-quark mass. arXiv:1403.4427 [hep-ex].
- [32] ATLAS Collaboration, G. Aad *et al.*, *Combined search for the Standard Model Higgs boson using up* to 4.9  $fb^{-1}$  of pp collision data at sqrt(s) = 7 TeV with the ATLAS detector at the LHC. Phys. Lett. **B710** (2012) 49–66, arXiv:1202.1408 [hep-ex].
- [33] CMS Collaboration, S. Chatrchyan *et al.*, Combined results of searches for the standard model Higgs boson in pp collisions at  $\sqrt{s} = 7$  TeV. Phys. Lett. B710 (2012) 26–48, arXiv:1202.1488 [hep-ex].
- [34] **TEVNPH (Tevatron New Phenomena and Higgs Working Group)** Collaboration, *Combined CDF* and D0 Search for Standard Model Higgs Boson Production with up to  $10.0 fb^{-1}$  of Data. arXiv:1203.3774 [hep-ex].
- [35] S. Bethke, World Summary of α<sub>s</sub> (2012). Nucl. Phys. Proc. Suppl. 234 (2013) 229–234, arXiv:1210.0325 [hep-ex].
- [36] K. G. Chetyrkin, M. Misiak, and M. Münz, *Beta functions and anomalous dimensions up to three loops*. Nucl. Phys. B518 (1998) 473–494, arXiv:hep-ph/9711266 [hep-ph].
- [37] M. Steinhauser, *MATAD: A program package for the computation of massive tadpoles*. Comput. Phys. Commun. **134** (2001) 335–364, arXiv:hep-ph/0009029.