

## Theoretical models of neutrino-nucleus cross sections

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In the present and future accelerator-based neutrino oscillation experiments nuclear targets (such as C, O, Ar and Fe) are involved. Hence the knowledge of neutrino-nucleus scattering is very important. In particular it is crucial for the determination of the neutrino energy which enters the expression of the oscillation probability, since this energy is reconstructed from the final states of the neutrino-nucleus reaction. The status of the different theoretical approaches treating the open channels in the few-GeV region, i.e. the quasielastic, the pion production and the multinucleon emission, is reviewed. Special emphasis is devoted to the multinucleon emission channel, which turned to be crucial to explain the unexpected behavior of the charged current quasielastic measurement performed by MiniBooNE. Up to last year, this channel was not included in the generators used for the analyses of the neutrino cross sections and oscillations experiments. The theoretical and experimental interest towards these multinucleon excitations continues to increase.

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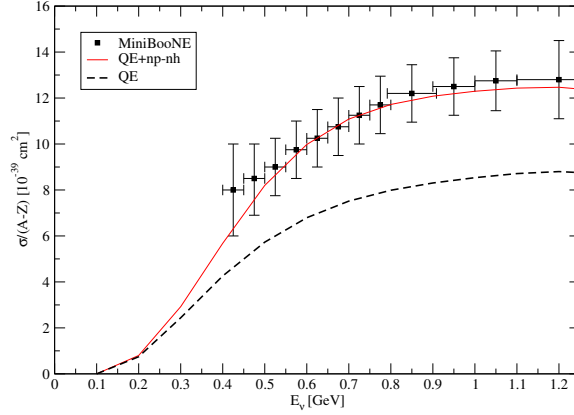
## 1. Introduction

Neutrino physics has undergone a spectacular development in the last decade, following the discovery of neutrino oscillations. In the present and future accelerator-based neutrino oscillation experiments nuclear targets, such as  $^{12}\text{C}$ ,  $^{16}\text{O}$ ,  $^{40}\text{Ar}$  or  $^{56}\text{Fe}$ , are involved, hence the knowledge of neutrino-nucleus scattering is very important. In particular it is crucial for the determination of the neutrino energy which enters the expression of the oscillation probability. In accelerator-based experiments the neutrino beams (at difference with respect to electron beams, for example) are not monochromatic but they span a wide range of energies, hence the incoming neutrino energy is reconstructed from the final states of the reaction. This determination is typically done through the charged current quasielastic (CCQE) events, commonly defined as those in which the emission product only includes one charged lepton. The reconstructed energy hypothesis used to obtain the neutrino energy from the measured charged lepton variables (energy and scattering angle) via a two-body formula is that the neutrino interaction in the nuclear target takes place on a nucleon at rest. The identification of the reconstructed neutrino energy with the real one is too crude. Several nuclear effects such as Pauli blocking, Fermi motion, collective aspects of the nuclear response and, very important, multinucleon emission, need to be taken into account. Furthermore, the fact that in the accelerator-based experiments the incoming neutrino beam exhibits a wide spectrum of energies implies that not only the quasielastic but also other reaction mechanisms, such as for example the pion production, contribute to the neutrino nucleus cross section. The status of the different theoretical approaches treating the open channels in the few-GeV region, i.e. the quasielastic, the pion production and the multinucleon emission, is here reviewed, devoting special emphasis to the multinucleon emission channel.

## 2. Quasielastic and multinucleon emission

The multinucleon emission channel in connection with the quasielastic has attracted a lot of attention in these last years. In fact, as illustrated in Fig. 1, the inclusion of this channel in the quasielastic cross section was suggested [1, 2] to be the possible explanation of the MiniBooNE CCQE total cross section on carbon [3], apparently too large with respect to many theoretical predictions employing the standard value of the axial mass. Since the MiniBooNE experiment, as well as other experiments involving Cherenkov detectors, defines a charged current “quasielastic” event as the one in which only a final charged lepton is detected, the ejection of a single nucleon (a genuine quasielastic event) is only one possibility, and one must in addition consider events involving a correlated nucleon pair from which the partner nucleon is also ejected, as discussed first by Marteau *et al.* in Ref. [4]. This leads to the excitation of 2 particle-2 hole (2p-2h) states; 3p-3h excitations are also possible. The inclusion in the quasielastic cross section of events in which several nucleons are ejected (np-nh excitations), leads to an excess over the genuine quasielastic value. Martini *et al.* [1, 2] have argued that this is the likely explanation of the MiniBooNE anomaly showing that their evaluation can account for the excess in the cross section without any modification of the axial mass. After this suggestion the interest of the neutrino scattering and oscillation communities on the multinucleon emission channel rapidly increased. Indeed this channel was not included in the generators used for the analyses of the neutrino cross sections and

oscillations experiments. Today there is an effort to include this np-nh channel in several Monte Carlo. Concerning the theoretical situation, nowadays several calculations agree on the crucial role of the multinucleon emission in order to explain the MiniBooNE neutrino [3] and antineutrino [5] data as well as the SciBooNE [6] and T2K [7] inclusive cross sections. Nevertheless there are some differences on the results obtained for this np-nh channel by the different theoretical approaches. The aim of this section is to review the current theoretical status on this subject.

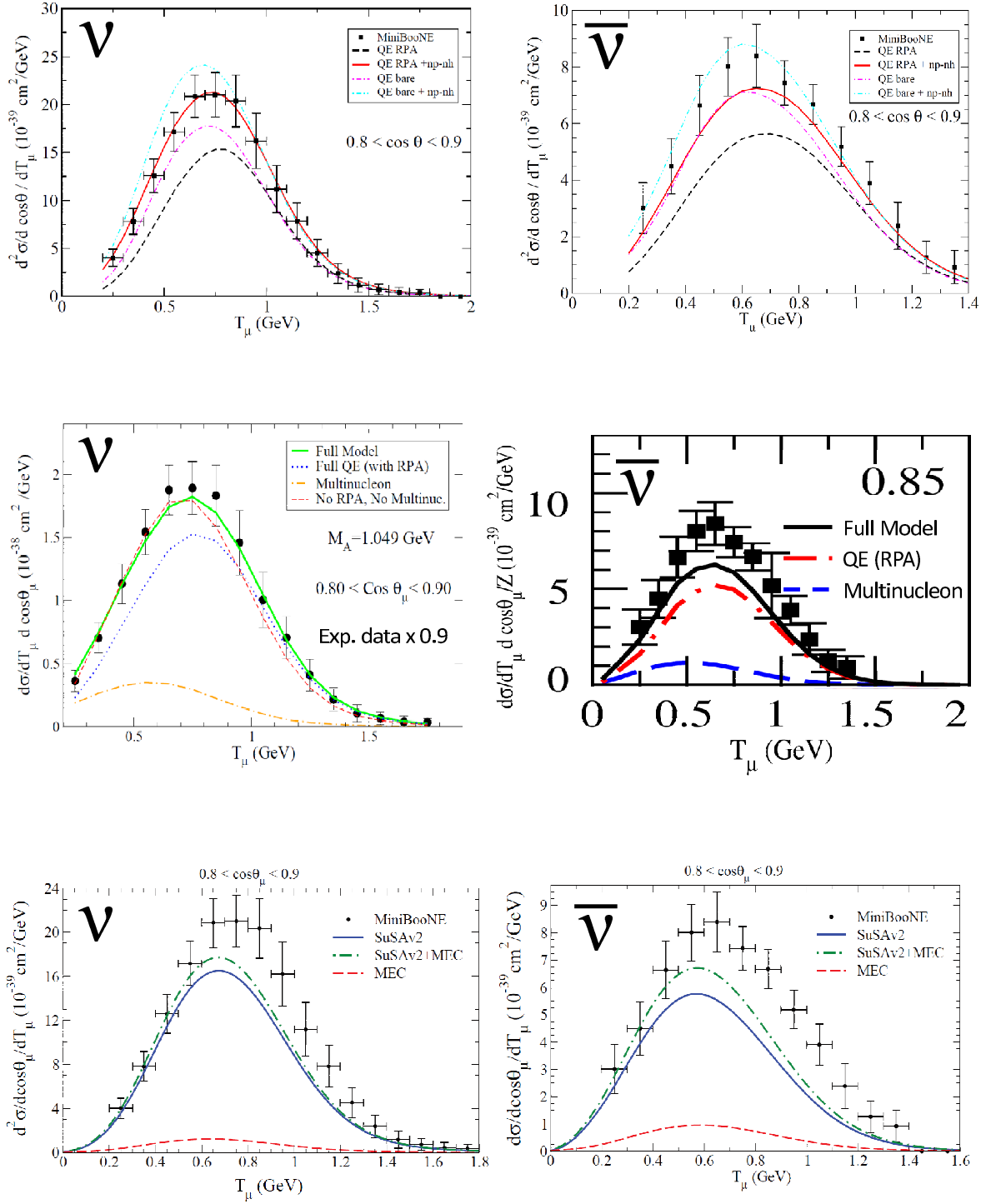


**Figure 1:** Charged current “Quasielastic” cross section on carbon measured by MiniBooNE [3] compared to Martini *et al.* calculations. The figure is taken from Ref. [1].

The theoretical calculations of np-nh excitations contributions to neutrino-nucleus cross sections are actually performed essentially by three groups. There are the works of Martini *et al.* [1, 2, 8, 9, 10, 11, 12, 13], the ones of Nieves *et al.* [14, 15, 16, 17, 18] and the ones of Amaro *et al.* [19, 20, 21, 22, 23, 24]. In the 2p-2h sector, these three approaches are based on the Fermi gas. We remind that there exist several two-body current contributions. We have first of all the Meson Exchange Currents (MEC), given by the pion-in-flight term, the contact term and the  $\Delta$ -intermediate state or  $\Delta$ -MEC term. Furthermore in the independent particle models, such as the Fermi gas, the nucleon-nucleon (NN) correlation must be taken into account. It is possible by including an additional two-body current, the correlation current. Even in the simple Fermi gas model, an exact relativistic calculation of all the two-body current contributions is difficult for several reasons. First of all it involves the computation of 7-dimensional integrals for a huge number of 2p-2h response Feynman diagrams. Second divergences in the NN correlations sector and in the angular distribution of the ejected nucleons [22, 23] may appear and need to be regularized. Furthermore the calculations should be performed for all the kinematics compatible with the experimental neutrino flux. For these reasons an exact relativistic calculation is computationally very demanding and as a consequence different approximations are employed by the different groups in order to reduce the dimension of the integrals and to regularize the divergences. The choice of subset of diagrams and terms to be calculated presents also important differences. In this connection Amaro *et al.* explicitly add to the genuine quasielastic only the MEC contributions and not the NN correlations-MEC interference terms. MEC contributions, NN correlations and NN correlations-MEC interference are present both in Martini *et al.* and Nieves *et al.* even if Martini *et al.* consider only the  $\Delta$ -MEC. On the other hand the treatment of Amaro *et al.* is fully relativistic as well as

the one of Nieves *et al.* while the results of Martini *et al.* are related to a non-relativistic reduction of the two-body currents. The interference between direct and exchange diagrams is neglected by Martini *et al.* and Nieves *et al.* Another important difference is that Amaro *et al.* consider the 2p-2h contribution only in the vector sector while Martini *et al.* and Nieves *et al.* also in the axial one. Fully relativistic calculations of Amaro *et al.* for the axial sector are in progress. Taking into account the existence of all these differences, is not surprising that these models produce different final results. This point is illustrated in Fig. 2 where the MiniBooNE neutrino and antineutrino flux folded double differential CCQE-like cross sections calculated in the different approaches are displayed. For sake of illustration the results are given for  $0.8 < \cos \theta < 0.9$  as function of the muon kinetic energy. The complete theoretical results in the different bins for neutrinos and antineutrinos are given in Refs. [8, 11] for Martini *et al.*, in Refs. [15, 17] for Nieves *et al.* and in Refs. [19, 21] for Amaro *et al.* An updated version of these last results is given by Megias *et al.* in Ref. [24] from which we take the results reported in the last two panels of Fig. 2. As one can observe from Fig. 2 the results of Martini *et al.* are in good agreement with the experimental data. In the case of Nieves *et al.* and Amaro *et al.* there is a tendency to underestimate the MiniBooNE data. Nevertheless also these results are compatible with MiniBooNE since an additional normalization error of 10% for neutrino and 17% for antineutrino is not shown in the error bars. An important point is that the relative role of the multinucleon contribution is different for neutrino and antineutrino in the different approaches. The nuclear cross-section difference for neutrinos and antineutrinos stands as a potential obstacle in the interpretation of experiments aimed at the measurement of the CP violation angle, hence has to be fully mastered. As discussed in Refs. [2, 21, 13] the difference between the neutrino and antineutrino results is due to the presence in the neutrino-nucleus cross section expression of the vector-axial interference term, which changes sign between neutrino and antineutrino, the basic asymmetry which follows from the weak interaction theory. Due to this vector-axial interference term, the relative weight of the different nuclear responses is different for neutrino and antineutrino. As a consequence also the relative weight of the np-nh contributions is different for neutrino and antineutrino. For example the fact that np-nh contributions are larger for antineutrinos with respect to neutrinos in the case of Amaro *et al.* is due to the fact that Amaro *et al.* consider the np-nh contributions only in the vector sector, hence not in the vector-axial interference term. In order to investigate the multinucleon content of the vector-axial interference term, Ericson and Martini have recently considered [13] the difference between the neutrino and antineutrino MiniBooNE quasielastic-like double-differential cross sections. They have shown that the model of Martini *et al.*, which includes the np-nh excitations in the vector-axial interference term, gives a good fit for the difference of the MiniBooNE cross sections reproducing well the data in the full range of muon energy and emission angle. This result represents an important test for the presence of the multinucleon component in the vector-axial interference term. A similar conclusion on a relevant two-body current contribution in the vector-axial interference term has been recently obtained by Lovato *et al.* [25, 26] who calculated the neutral weak current two-body contributions to sum rules and Euclidean responses in  $^{12}\text{C}$ .

Up to now we have discussed the theoretical models in connection with the MiniBooNE cross sections. For the moment the theoretical calculations for the np-nh excitations are restricted to the relatively small energy and momentum transfer, prevalent in the MiniBooNE and T2K experiments. As already mentioned fully relativistic calculations of Amaro *et al.* for the axial two-body current



**Figure 2:** MiniBooNE flux integrated neutrino (left panels) and antineutrino (right panels) CCQE-like double differential cross section on carbon per active nucleon for  $0.8 < \cos \theta < 0.9$  as a function of the muon kinetic energy. Top panels: Martini *et al.* [8, 11] results. Middle panels: Nieves *et al.* [15, 17] results. Bottom panels: Megias *et al.* [24] results representing an update of the Amaro *et al.* [19, 21] results.

contributions are still in progress. How the np-nh processes behave at large energy and momentum transfer is still an open question. Nevertheless Megias *et al.* [24] applied the model of Amaro *et al.* to neutrino energies of up to 100 GeV and compared their predictions also with MINERvA neutrino [27] and antineutrino [28] CCQE data. Gran *et al.* [18] applied the model of Nieves *et al.* to neutrino energies of up to 10 GeV. However they placed a cut on the three-momentum transfer of 1.2 GeV. They compared their results with the MINERvA neutrino and antineutrino CCQE  $Q^2$  distribution. A similar comparison has been performed also by Mosel *et al.* [29] using GiBUU. As a general remark, by comparing the results of Refs. [18, 24, 29] with MINERvA data, one can observe that the MINERvA  $Q^2$  distributions can be reproduced also without the inclusion of np-nh excitations. This is not the case of the MiniBooNE  $Q^2$  distributions [8, 11, 24]. As stressed by Mosel *et al.*, in the case of MINERvA the sensitivity to details of the treatment of np-nh contributions is smaller than the uncertainties introduced by the  $Q^2$  reconstruction and our insufficient knowledge of pion production. The MINERvA experiment being at higher energies with respect to the MiniBooNE one, the pion production channel becomes in this case more important hence the background subtraction to isolate genuine CCQE and 2p-2h events is delicate.

### 3. Pion production and inclusive cross sections

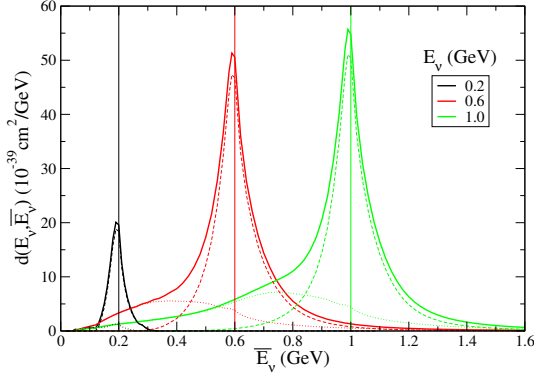
Turning to the other channels, in this section we rapidly discuss the present situation for the pion production and inclusive cross sections. In the one pion production channel some questions are still open. For instance there is a general tendency of theoretical calculations and Monte Carlo results to underestimate the MiniBooNE data [30, 31] and to overestimate the MINERvA ones [32]. Further investigations are needed. We remind the different energies of MiniBooNE and MINERvA neutrino beams.

The inclusive  $\nu_\mu$  CC double differential cross section on carbon has been published by T2K in Ref. [7]. The inclusive measurements are important because they are less affected by background subtraction with respect to exclusive channels measurements. Martini and Ericson have compared their predictions with the T2K experimental results in Ref. [12]. In this paper they have shown that in order to obtain an agreement with the T2K inclusive data one needs to consider not only the genuine quasielastic and the one pion production channels but also the multinucleon excitations. These results represent the first successful test of the necessity of the multinucleon emission channel in an experiment with another neutrino flux with respect to the one of MiniBooNE.

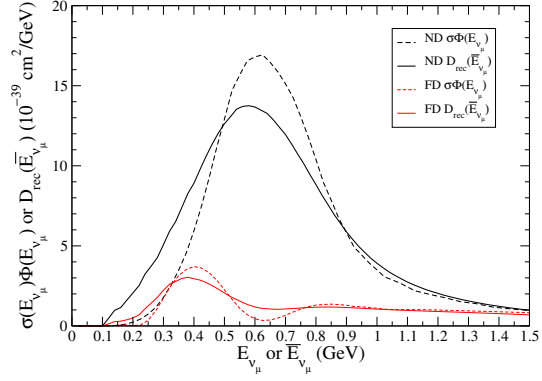
### 4. Neutrino energy reconstruction problems and neutrino oscillations

The neutrino energy reconstruction problem has been already mentioned in the introduction. The determination of the initial neutrino energy is commonly done through the charged current neutrino-nucleus quasielastic-like events. For these events where only the charged lepton is observed, the only measurable quantities are then its direction, i.e., its emission angle  $\theta$  with respect to the neutrino beam direction and its energy  $E_l$  (or kinetic energy  $T_l$  and momentum  $P_l$ ). The neutrino energy  $E_\nu$  is unknown. The usual reconstruction procedure assumes that we are dealing with a genuine quasielastic event on a nucleon at rest. The quasielastic condition then gives the value  $\overline{E_\nu}$  of the reconstructed energy:  $\overline{E_\nu} = \frac{E_l - m_l^2 / (2M)}{1 - (E_l - P_l \cos \theta) / M}$ . Several nuclear effects can influence this





**Figure 3:** The spreading function per neutron of  $^{12}\text{C}$  evaluated for three  $E_\nu$  values. The genuine quasielastic (dashed lines) and the multinucleon (dotted lines) contributions are also shown separately. The figure is taken from Ref. [10].



**Figure 4:** T2K distributions per neutrons of muon events before (dashed lines) and after (continuous lines) the energy reconstruction correction in the near and far detector. The figure is taken from Ref. [10].

expression. The most important are the np-nh events which have no reason to fulfill the quasielastic relation. This means that for a given set of lepton variables,  $E_l$  and  $\theta$ , an infinity of neutrino energy values, instead of the unique quasielastic value implemented in the neutrino energy reconstruction formula, is possible. Data on neutrino oscillation often involve reconstructed neutrino energies while the analysis implies the real neutrino energy. The corrections corresponding to the transformation from real to reconstructed energy and viceversa are discussed in details in Refs. [9, 10, 16, 33] to which we refer the reader. Here we just summarize some of the main results following the approach of Refs. [9, 10]. Starting from a theoretical distribution expressed with real energies, *i.e.* the product of the neutrino cross section  $\sigma(E_\nu)$  by the neutrino energy distribution of the beam  $\Phi(E_\nu)$ , a smearing procedure to deduce the corresponding distribution of the events,  $D_{rec}(\bar{E}_\nu)$ , in terms of the reconstructed energy can be performed. This distribution can be expressed in terms of the double differential neutrino-nucleus cross section, according to

$$D_{rec}(\bar{E}_\nu) = \int dE_\nu \Phi(E_\nu) \int_{E_l^{min}}^{E_l^{max}} dE_l \frac{ME_l - m_l^2/2}{\bar{E}_\nu^2 P_l} \left[ \frac{d^2\sigma}{d\omega d\cos\theta} \right]_{\omega=E_\nu-E_l, \cos\theta=\cos\theta(E_l, \bar{E}_\nu)}. \quad (4.1)$$

The second integral on the r.h.s. of Eq. (4.1) is denoted as  $d(E_\nu, \bar{E}_\nu)$ . It represents the spreading function and depends on  $E_\nu$  and  $\bar{E}_\nu$ . Some examples of its  $\bar{E}_\nu$  dependence for several  $E_\nu$  values are given in Fig. 3. As one can observe this spreading function is not symmetrical around  $E_\nu$ . The multinucleon excitations play a crucial role since they create a low energy tail. Similar results have been obtained in Refs. [16, 33]. In Fig. 4 is shown the application of the smearing procedure of Ref. [10] to the two distributions measured in T2K: the muonic distributions in the near detector (ND) and far detector (FD), hence related to the  $\nu_\mu$  disappearance studies. The influence of the reconstructed energy corrections is such that the events tend to escape from the region of high fluxes with a tendency to concentrate at lower energies. Furthermore the middle hole of the far detector results is largely filled. These effects are due to the multinucleon component of the quasielastic-like cross section. Similar results have been obtained in Ref. [33]. The effects are such that an analysis

which takes into account the smearing effect is likely to lead to some increase of the oscillation mass value.

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