

## Higgs production within $k_t$ -factorization with unintegrated gluon distributions

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We present differential cross sections for Higgs boson and/or two-photon production from intermediate (virtual) Higgs boson within the formalism of  $k_t$ -factorization. Resulting distributions for two photons from the Higgs boson are compared with recent ATLAS collaboration data. In contrast to a recent calculation the leading order  $gg \rightarrow H$  contribution is rather small compared to the ATLAS experimental data ( $\gamma\gamma$  transverse momentum and rapidity distributions). We include also higher-order contribution  $gg \rightarrow H(\rightarrow \gamma\gamma)g$ ,  $gg \rightarrow gHg$  and the contribution of the  $W^+W^-$  and  $Z^0Z^0$  exchanges. The  $gg \rightarrow Hg$  mechanism gives a similar contribution as the  $gg \rightarrow H$  mechanism. We argue that there is almost no double counting when adding  $gg \rightarrow H$  and  $gg \rightarrow Hg$  contributions due to different topology of corresponding Feynman diagrams. The final sum is comparable with the ATLAS two-photon data.

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## 1. Introduction

The Higgs boson was discovered at the LHC [1]. It has been observed in a few decay channels. The  $\gamma\gamma$  and  $Z^0 Z^{0,*}$  are particularly spectacular [2, 3, 4, 5].

After the discovery understanding the rapidity and transverse momentum distributions is particularly interesting. While the total cross section is well under control and was calculated in leading-order (LO), next-to-leading order (NLO) and even next-to-next-to-leading order (NNLO) approximation [6] the distribution in the Higgs boson transverse momentum is more challenging.

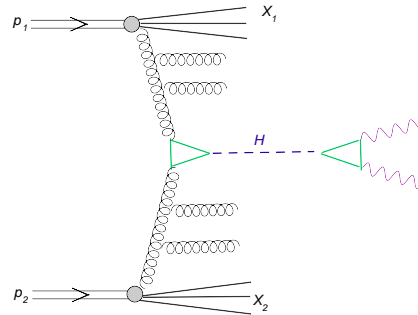
It was advocated recently that precise differential data for Higgs boson in the two-photon final channel could be very useful to test and explore unintegrated gluon distribution functions (UGDFs) [7]. It was claimed very recently [8] that the  $k_t$ -factorization formalism with commonly used UGDFs (Kimber-Martin-Ryskin (KMR) [9] and Jung CCFM [10]) gives a reasonable description of recent ATLAS data obtained at  $\sqrt{s} = 8$  TeV [11]. We perform similar calculation and draw rather different conclusions.

Here we report on our results from Ref.[12] obtained within  $k_t$ -factorization approach where we presented several differential distributions for the Higgs boson and photons from the Higgs boson decay at  $\sqrt{s} = 8$  TeV for various UGDFs from the literature.

There we have included both leading-order and next-to-leading order contributions. We shall critically discuss uncertainties and open problems in view of the recent ATLAS data.

## 2. A sketch of the formalism

The leading-order mechanism of Higgs boson production in the  $k_t$ -factorization is shown in Fig.2.



**Figure 1:**

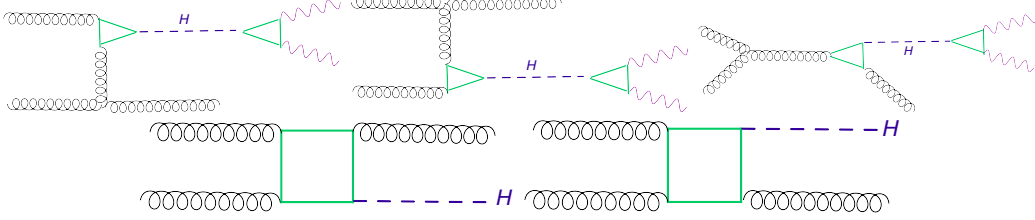
The leading-order diagram for Higgs boson production in the two-photon channel relevant for the  $k_t$ -factorization approach.

In the  $k_t$ -factorization approach the cross section for the Higgs boson production can be written somewhat formally as:

$$\sigma_{pp \rightarrow H} = \int \frac{dx_1}{x_1} \frac{dx_2}{x_2} \frac{d^2 q_{1t}}{\pi} \frac{d^2 q_{2t}}{\pi} \delta((q_1 + q_2)^2 - M_H^2) \sigma_{gg \rightarrow H}(x_1, x_2, q_1, q_2) \times \mathcal{F}_g(x_1, q_{1t}^2, \mu_F^2) \mathcal{F}_g(x_2, q_{2t}^2, \mu_F^2), \quad (2.1)$$

where  $\mathcal{F}_g$  are so-called unintegrated (or transverse-momentum-dependent) gluon distributions and  $\sigma_{gg \rightarrow H}$  is  $gg \rightarrow H$  (off-shell) cross section.

In Fig.2 we show next-to-leading order partonic subprocesses. While the processes with triangles are effectively included in a calculation related to the diagram shown in Fig.2, the diagrams with boxes (much larger contributions) have to be included extra.



**Figure 2:**

QCD NLO subprocesses with triangles (upper line) and boxes (lower line).

In the collinear approximation the corresponding cross section differential in Higgs boson rapidity ( $y_H$ ), associated parton rapidity ( $y_p$ ) and transverse momentum of each of them can be written as:

$$\begin{aligned} \frac{d\sigma}{dy_H dy_p d^2 p_t}(y_H, y_p, p_t) = & \frac{1}{16\pi^2 \hat{s}^2} \times \left\{ x_1 g_1(x_1, \mu^2) x_2 g_2(x_2, \mu^2) \overline{|\mathcal{M}_{gg \rightarrow Hg}|^2} \right. \\ & + \left[ \sum_{f_1=-3,3} x_1 q_{1,f_1}(x_1, \mu^2) \right] x_2 g_2(x_2, \mu^2) \overline{|\mathcal{M}_{qg \rightarrow Hq}|^2} \\ & + x_1 g_1(x_1, \mu^2) \left[ \sum_{f_2=-3,3} x_2 q_{2,f_2}(x_2, \mu^2) \right] \overline{|\mathcal{M}_{gq \rightarrow Hq}|^2} \\ & \left. + \sum_{f=-3,3} x_1 q_{1,f}(x_1, \mu^2) x_2 q_{2,-f}(x_2, \mu^2) \overline{|\mathcal{M}_{qq \rightarrow Hg}|^2} \right\}. \quad (2.2) \end{aligned}$$

The indices  $f$  in the formula above number both quarks ( $f > 0$ ) and antiquarks ( $f < 0$ ). Only three light flavours are included in actual calculations here.

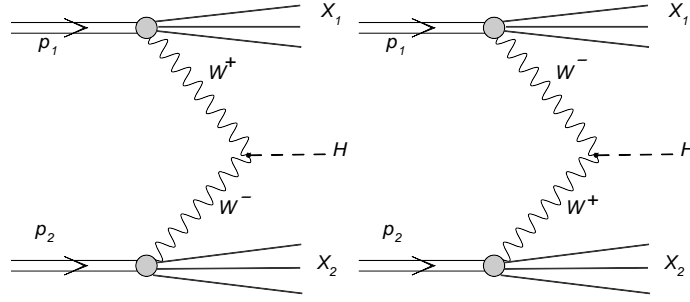
In Ref.[12] we have calculated the dominant  $gg \rightarrow Hg$  contribution also taking into account transverse momenta of initial gluons. In the  $k_t$ -factorization the NLO differential cross section can be written as:

$$\begin{aligned} \frac{d\sigma(pp \rightarrow HgX)}{dy_H dy_g d^2 p_{H,t} d^2 p_{g,t}} = & \frac{1}{16\pi^2 \hat{s}^2} \int \frac{d^2 q_{1t}}{\pi} \frac{d^2 q_{2t}}{\pi} \overline{|\mathcal{M}_{g^* g^* \rightarrow Hg}^{off-shell}|^2} \\ & \times \delta^2(\vec{q}_{1t} + \vec{q}_{2t} - \vec{p}_{H,t} - \vec{p}_{g,t}) \mathcal{F}(x_1, q_{1t}^2, \mu^2) \mathcal{F}(x_2, q_{2t}^2, \mu^2). \quad (2.3) \end{aligned}$$

How the matrix elements were calculated was explained in our original paper [12].

Also production of Higgs boson associated with two jets in the final state may play important role [12].

In addition to the QCD contributions discussed above one has to include also electroweak ones. Some examples are shown in Fig.2.

**Figure 3:**

Some examples of electoweak corrections with exchange of  $W$  bosons

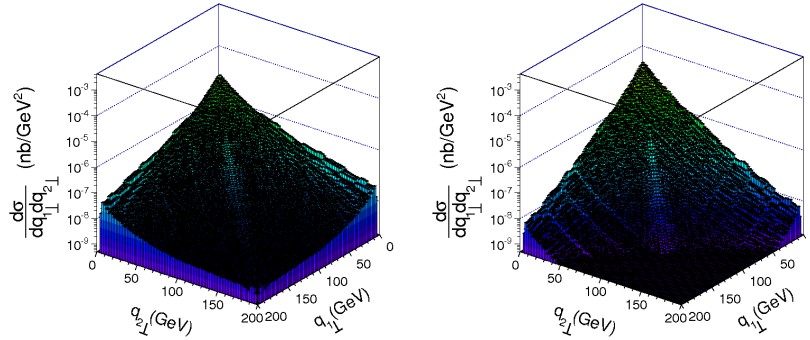
The corresponding proton-proton cross section can be written as

$$d\sigma = \mathcal{F}_{12}^{VV}(x_1, x_2) \frac{1}{2\hat{s}} \overline{|\mathcal{M}_{qq \rightarrow qqH}|^2} \frac{d^3 p_3}{(2\pi)^3 2E_3} \frac{d^3 p_4}{(2\pi)^3 2E_4} \frac{d^3 p_H}{(2\pi)^3 2E_H} \times (2\pi)^4 \delta^4(p_1 + p_2 - p_3 - p_4 - p_H) dx_1 dx_2. \quad (2.4)$$

### 3. Results

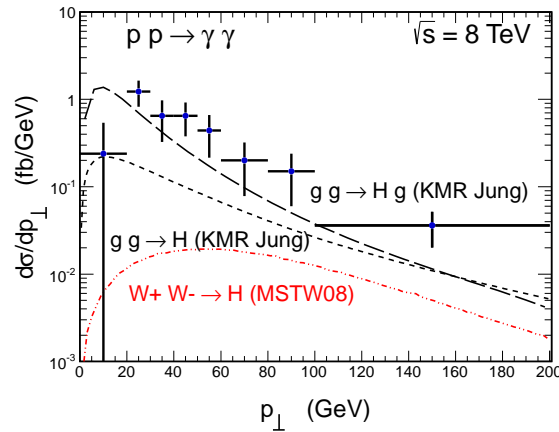
The different UGDFs in the literature have quite different dependence on gluon transverse momenta. In Fig. 4 we show an example of two-dimensional maps in  $q_{1t} \times q_{2t}$  (transverse momenta of the fusing gluons) for two UGDFs. Many more examples were presented in [12]. In Ref.[12] we concluded that a use of saturation inspired scale independent UGDFs is not sufficient for the Higgs boson production. They lead also to distributions in  $p_{1t}$  and  $p_{2t}$  which are peaked in extremely small  $p_{1t}$  and  $p_{2t}$ , at least for the leading order  $gg \rightarrow H$  subprocess. Quite large gluon transverse momenta ( $q_{1t}, q_{2t} \sim m_H$ ) enter the production of the Higgs boson for the KMR and Jung CCFM (setA0) UGDFs. For the KMR UGDF a clear enhancement at small  $q_{1t}$  or  $q_{2t}$  can be observed. This is rather a region of nonperturbative nature, where the KMR UGDF is rather extrapolated than calculated. We have checked, however, that the contribution of the region when  $q_{1t} < 2$  GeV or  $q_{2t} < 2$  GeV constitutes only less than 5% of the integrated cross section. This is then a simple estimate of uncertainty of the whole approach.

A distribution in Higgs boson transverse momentum is particularly interesting. In Fig. 5 we compare contributions of different mechanisms. The QCD contributions shown in this subsection were calculated with the KMR UGDF. Surprisingly the contribution of the next-to-leading order mechanism  $gg \rightarrow Hg$  is even slightly bigger than that for the  $gg \rightarrow H$  fusion, especially for intermediate Higgs boson transverse momenta. As discussed in our original paper [12] there is almost no double counting when adding the corresponding cross sections due to quite different topology of corresponding Feynman diagrams. As shown in the present analysis the  $gg \rightarrow H$  mechanism is not sufficient within the  $k_t$ -factorization approach. The  $2 \rightarrow 3$  contribution of the  $gg \rightarrow gHg$  subprocess is also not negligible but here one can expect that a big part is already contained in the  $gg \rightarrow H$  calculation especially with the KMR UGDF. Therefore we do not add this contribution explicitly when calculating  $d\sigma/dp_{t,sum}$ . The contribution of the  $WW, ZZ$  fusion is also fairly sizeable. In



**Figure 4:** Distribution in  $q_{1\perp}$  and  $q_{2\perp}$  for the  $gg \rightarrow H$  subprocess and for the KMR and Jung CCFM (setA0) UGDFs.

principle, the Higgs bosons (or photons from the Higgs boson) associated with the electroweak boson exchanges could be to some extent separated by requiring rapidity gaps i.e. production of Higgs boson isolated off other hadronic activity.



**Figure 5:** Transverse momentum distribution of the Higgs boson in the  $\gamma\gamma$  channels for the different mechanisms:  $gg \rightarrow H$  (solid line),  $gg \rightarrow Hg$  (dashed line) and  $WW \rightarrow H$  (dash-dotted line).

#### 4. Conclusions

We have presented results of our analysis of production of Higgs boson in the two-photon channel within  $k_t$ -factorization. Matrix elements and UGDFs are the ingredients of the approach.

We have found that different UGDFs (not discussed here) give quite different results. However, many of the UGDF models were adjusted to low- $x$  phenomena and cannot be used for production of relatively heavy Higgs boson, where rather large gluon transverse momenta are involved.

LO  $k_t$ -factorization underpredicts the two-photon data in contrast to recent claims. NLO corrections have to be taken into account and the  $gg \rightarrow Hg$  subprocess is especially important. Also a contribution of Higgs boson associated with quark/antiquark dijets is nonnegligible [12]. Electroweak corrections (here only  $W^+W^-$  fusion was discussed) were found to be large at large transverse momenta of the Higgs boson.

Only combined analysis including all ingredients can provide a possibility to describe experimental data and to test UGDFs. We expect that future run2 data will allow for better tests of UGDFs.

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