

Unpolarized TMD quark distribution functions at low Q^2 scales

H. Nematollahi^{a*}, M. M. Yazdanpanah^a and A. Mirjalili^b

^a*Faculty of Physics, Shahid Bahonar University of Kerman, Kerman, Iran*

^b*Faculty of Physics, Yazd University, Yazd, Iran*

E-mail: h.nematollahi@sci.uk.ac.ir, myazdan@uk.ac.ir,
a.mirjalili@yazduni.ac.ir

We calculate the unpolarized transverse momentum dependent (TMD) quark distributions in the modified chiral quark model (χQM). To this end, we use the integrated quark densities which are multiplied by a TMD Gaussian factor. These integrated distributions are computed applying the χQM at low Q^2 value ($Q^2 = 0.35 \text{ GeV}^2$). Finally, we compare our results with corresponding ones which were obtained in our previous work via a different approach. It is shown that our results have appropriate treatment which is expected for the TMD quark densities.

*The European Physical Society Conference on High Energy Physics
22–29 July 2015
Vienna, Austria*

*Speaker.

1. Introduction

To get a better understanding of the partonic substructure of the nucleon, it is needed to study the transverse momentum dependent parton distribution functions (TMDs) [1, 2, 3]. These densities have also been called the unintegrated parton distributions [4].

The description of some experimental observations is not possible without a three-dimensional picture of the nucleon including transverse motion. The integrated parton distribution functions (PDFs) can not give such 3-D picture of the nucleons, so the TMD densities are needed for this purpose [5, 6].

We calculated the unpolarized TMD quark distributions inside the proton using the modified chiral quark model in our previous work [7]. This model is valid at low Q^2 values. In Ref.[7], we first formulated the interactions which occur in the χQM at the first approximation in the TMD case and then obtained the TMD quark densities of the proton at $Q^2 = 0.35 \text{ GeV}^2$.

In this paper, we compute the TMD quark distributions via a different approach. In this approach, the integrated quark densities which are obtained applying the χQM are multiplied by a TMD Gaussian factor. Finally, we compare the results of this approach with the results of Ref.[7].

2. A relationship between the integrated PDFs and unpolarized TMDs

In this section, we use a phenomenological approach which creates a contact between the integrated quark distribution functions ($q(x)$) and the TMD ones ($q(x, p_T)$). In this approach, the x dependence of the TMD quark densities is factorized and a Gaussian form is used for its p_T dependence [8, 9, 10]. The transverse momentum dependence of these quark distributions is parametrized applying the TMD Gaussian factor (TMD GF) as following [8, 9, 10]:

$$q(x, p_T) = q(x) \frac{1}{\pi \langle p_T^2 \rangle} \exp\left(\frac{-p_T^2}{\langle p_T^2 \rangle}\right), \quad (2.1)$$

which [10]

$$\int \frac{1}{\pi \langle p_T^2 \rangle} \exp\left(\frac{-p_T^2}{\langle p_T^2 \rangle}\right) dp_T^2 = 1. \quad (2.2)$$

In above equation $\langle p_T^2 \rangle$ is the width of the TMD Gaussian factor which is adopted as $\langle p_T^2 \rangle = 0.2 \text{ GeV}^2$ [11]. We also use the results of the modified chiral quark model for the integrated quark distribution functions ($q(x)$) which is appeared in Eq.(1). We explain the method of calculating these integrated densities using the χQM in the next section:

3. Modified chiral quark model

In this section, we calculate the integrated quark distribution functions applying the modified chiral quark model. In this model, proton is considered as a bounded system of bare u and d quarks (u_0, d_0). In this system, the clouds of Goldstone (GS) bosons and gluons surround the bare quarks [12, 13, 14].

At the first approximation, two basic interactions are occurred in the χQM which are represented

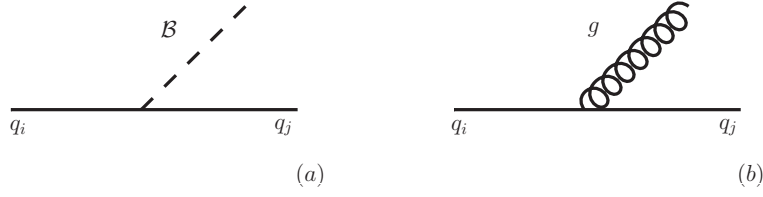


Figure 1: (a) The bare quark fluctuation into a GS boson \mathcal{B} and a struck quark q_j . (b) The bare quark emits a gluon. This picture has quoted from Ref.[7]

in Fig.1. For the interaction of Fig.1(a), the distribution of j quark is written as [12, 13, 14]:

$$q_j(x) = \int_x^1 \frac{dy}{y} P_{j\mathcal{B}/i}(y) q_{0,i}\left(\frac{x}{y}\right). \quad (3.1)$$

$P_{j\mathcal{B}/i}$ is the splitting function of the quark-GS boson vertex [12, 13, 14]:

$$P_{j\mathcal{B}/i}(y) = \frac{1}{8\pi^2} \int \left(\frac{g_A \bar{m}}{f}\right)^2 \frac{(m_j - m_i y)^2 + k_\perp^2}{y^2(1-y)(m_i^2 - M_{j\mathcal{B}}^2)^2} dk_\perp^2. \quad (3.2)$$

$M_{j\mathcal{B}}^2$ denotes the squared invariant mass of the final quark-GS boson state [12, 13, 14].

On the other hand, the interaction of Fig.1(b) is formulated as follows [14]:

$$q_j(x) = \int_x^1 \frac{dy}{y} P_{jg/i}(y) q_{0,i}\left(\frac{x}{y}\right), \quad (3.3)$$

where the quark-gluon vertex splitting function $P_{jg/i}$ is given as [14]:

$$P_{jg/i}(y) = \int C_f \frac{\alpha_s(Q^2)}{4\pi} \frac{1}{y(1-y)} G_{jg/i}^2 \frac{(ym_i - m_j)^2 + k_\perp^2}{y(m_i^2 - M_{jg}^2)^2} dk_\perp^2. \quad (3.4)$$

$G_{jg/i}$ is the quark-gluon vertex function [14].

According to above interactions, the quark distribution functions of the proton are obtained [12, 13, 14]:

$$u(x) = Z_u u_0(x) + P_{u\pi^-/d} \otimes d_0 + \frac{1}{2} P_{u\pi^0/u} \otimes u_0 + P_{ug/u} \otimes u_0, \quad (3.5)$$

$$d(x) = Z_d d_0(x) + P_{d\pi^+/u} \otimes u_0 + \frac{1}{2} P_{d\pi^0/d} \otimes d_0 + P_{dg/d} \otimes d_0, \quad (3.6)$$

$$s(x) = P_{sk^+/u} \otimes u_0 + P_{sk^0/d} \otimes d_0. \quad (3.7)$$

Z_u and Z_d are the renormalization constants for u_0 and d_0 , respectively. The bare quark distributions are obtained by solving the Dirac equation including a potential with the squared radial symmetry [14, 15, 16].

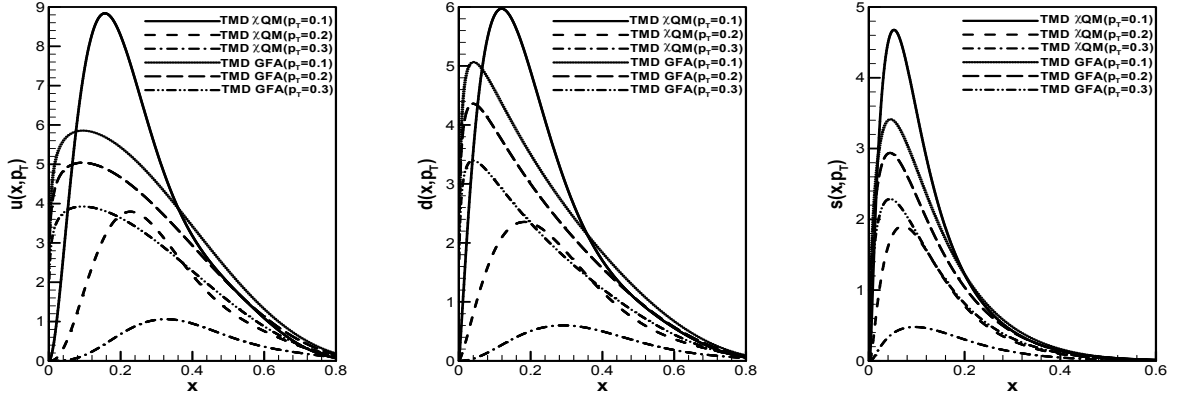


Figure 2: The TMD light quark densities with respect to x at $Q^2 = 0.35 \text{ GeV}^2$ for $p_T = 0.1, 0.2$ and 0.3 GeV . The results of the TMD Gaussian factor approach (TMD GFA) have been compared with the results of Ref.[7] (TMD χQM).

4. Results and discussion

We have calculated the unpolarized TMD quark distributions using Eq.(1). To this end, we have first obtained the integrated quark densities applying the modified chiral quark model at $Q^2 = 0.35 \text{ GeV}^2$. In Fig.2, we have depicted these TMD u, d and s quark distributions with respect to x at different values of transverse momentum p_T ($p_T = 0.1, 0.2$ and 0.3 GeV). In this figure, we have compared the result of this approximate approach (TMD GF approach) with the results of TMD χQM approach [7]. In Ref.[7], we extracted the TMD quark densities via the χQM , directly.

As can be seen in Fig.2, the results of both approaches show the same behaviour: the TMD distributions decrease by increasing the p_T value [7, 10, 17, 18]. This means that the probability of finding the quarks with larger p_T value, is lower.

We have also displayed the TMD u, d and s quark distributions with respect to p_T at different x values in Fig.3 and compared the results with the results of our previous work (TMD χQM). It is shown that the Gaussian width of these densities is x dependent [7, 10]. The width of the results of the TMD GF approach is larger than the TMD χQM ones. In the left side of Fig.3, the transverse momentum dependent quark distributions grow by increasing the x value in spite of the behaviour of the TMD quark densities in the right side of this figure [7].

References

- [1] J. C. Collins, *What exactly is a parton density?*, Acta Phys. Polon. B **34** (2003) 3103.
- [2] J. C. Collins, T. C. Rogers and A. M. Stasto, *Fully unintegrated parton correlation functions and factorization in lowest order hard scattering*, Phys. Rev. D **77** (2008) 085009.
- [3] F. Hautmann, *Endpoint singularities in unintegrated parton distributions*, Phys. Lett. B **655** (2007) 26.

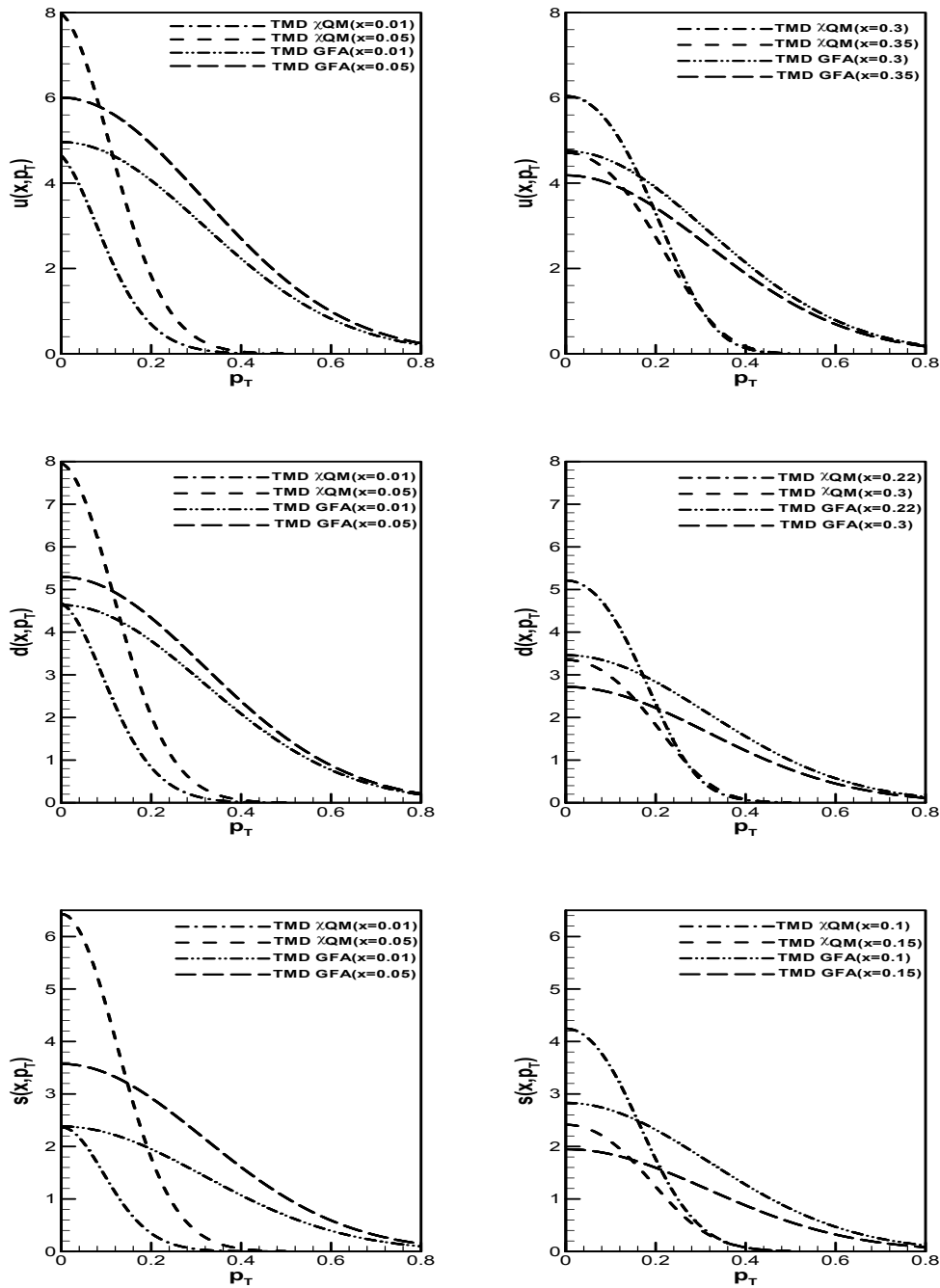


Figure 3: The TMD u , d and s quark distributions with respect to p_T at $Q^2 = 0.35 \text{ GeV}^2$. The results of the TMD Gaussian factor approach (TMD GFA) for different x values have been compared with the results of Ref.[7] (TMD χQM).

- [4] J. C. Collins, D. E. Soper, *Parton distribution and decay function*, Nucl. Phys. B **194** (1982) 445.
- [5] M. Barkardt, *Impact parameter dependent parton distributions and off forward parton distribution for $\zeta \rightarrow 0$* , Phys. Rev. D **62** (2000) 071503.
- [6] J. P. Ralston and B. Pire, *Femtophotography of protons to nuclei with deeply virtual compton scattering*, Phys. Rev. D **66** (2002) 111501.
- [7] H. Nematollahi, M. M. Yazdanpanah and A. Mirjalili, *Unpolarized transverse momentum dependent densities based on the modified chiral quark model*, Eur. Phys. J. Plus **129** (2014) 204.
- [8] Z. Lu and B-Q Ma, *Quark helicity distributions in transverse momentum space and transverse coordinate space*, Phys. Rev. D **87** (2013) 034037.
- [9] M. Anselmino and et al., *Unpolarized transverse momentum dependent distribution and fragmentation functions from SIDIS multiplicities*, JHEP **1404** (2014) 005.
- [10] P. Zavada, *Generalized Cahn effect and parton 3D motion in a covariant approach*, Phys. Rev. D **83** (2011) 014022.
- [11] S. M. Aybat, J. C. Collins, J. W. Qiu, and T. C. Rogers, *The QCD evolution of the Sivers function*, Phys. Rev. D **85** (2012) 034043.
- [12] K. Suzuki and W. Weise, *Chiral constituent quarks and their role in quark distribution functions of nucleon and pion*, Nucl. Phys. A **634** (1998) 141.
- [13] H. Song, X. Zhang and B-Q Ma, *Light flavor asymmetry of nucleon sea*, Eur. Phys. J. C **71** (2011) 1542.
- [14] H. Nematollahi, M. M. Yazdanpanah and A. Mirjalili, *Parton densities in the modified chiral quark model*, J. Phys. G: Nucl. Part. Phys. **39** (2012) 045009.
- [15] A. Faessler, Th. Gutsche, V.E. Lyubovitskij and K. Pumsa-ard, *Chiral dynamics of baryons in the quark model*, AIP Conf. Proc. **884** (2007) 43.
- [16] M. M. Yazdanpanah, A. Mirjalili and M. Dehghanzadeh, *Sea quark densities in the effective chiral quark model with generalized harmonic oscillator potential*, Eur. Phys. J. C **72** (2012) 2220.
- [17] H. Avakian and et al., *The transverse momentum distributions in the bag model*, Phys. Rev. D **81** (2010) 074035.
- [18] A. V. Efremov and et al., *The relation between TMDs and PDFs in the covariant parton model approach*, Phys. Rev. D **83** (2011) 054025.