In the system of neutral $B$ mesons CP-violation and meson mixing can be measured using time-dependent analyses, as performed at the LHCb experiment. For such analyses the knowledge of the flavour of the mesons at production is mandatory. This information is provided by "flavour tagging" techniques. A description of the flavour tagging algorithms used at the LHCb experiment during Run I in $pp$ collisions at $\sqrt{s} = 7,8\,\text{TeV}$ is reported.
1. Introduction

The aim of the Flavour Tagging algorithms is to determine the flavour of neutral $B$ mesons at their production. These algorithms are called taggers and can be classified into two groups. The same side (SS) taggers use charged particles which are created in the fragmentation process of the signal $b$ quark. The opposite side (OS) taggers infer the flavour of the non-signal $b$ quark of the $b\bar{b}$ pair produced in the $pp$ collision by looking e.g. for leptons originating from semileptonic $b \to cW$ transitions or kaons coming from $b \to c \to s$ transitions (Figure 1) [1].

The performance of the Flavour Tagging algorithms is characterised by the tagging efficiency

$$\varepsilon_{\text{tag}} = \frac{N_{\text{right}} + N_{\text{wrong}}}{N_{\text{all}}},$$

the probability of the tagging decision to be wrong

$$\omega = \frac{N_{\text{wrong}}}{N_{\text{right}} + N_{\text{wrong}}}$$

and the dilution $D = 1 - 2\omega$. The quantities $N_{\text{right}}$, $N_{\text{wrong}}$ and $N_{\text{all}}$ are the numbers of the right tagged, wrong tagged, and all candidates respectively, where the latter includes both the tagged and untagged candidates.

Each tagger provides a per-event tag decision $d$ and a probability $\eta$ of the decision to be wrong. This predicted mistag probability $\eta$ is calibrated with a function $\omega(\eta)$ with parameters obtained from data. Weighting each signal candidate with $D = 1 - 2\omega(\eta)$ leads to an corrected per-event dilution factor. The statistical power of a $CP$ or mixing asymmetry measurement using tagging algorithms is proportional to the effective tagging efficiency

$$\varepsilon_{\text{eff}} = \varepsilon_{\text{tag}} \frac{1}{N_{\text{tag}}} \sum_{i=1}^{N_{\text{tag}}} (1 - 2\omega_i(\eta))^2.$$ 

Thus any improvement to this effective tagging efficiency increases the statistical power of time dependent measurements using flavour tagging.

2. Flavour Tagging algorithms at LHCb

For the opposite side tagging algorithms there are mainly two different types of algorithms. Single particle taggers identify electrons, muons and kaons coming from the other $b$ hadron. To select these particles a large impact parameter significance with respect to the primary vertex and a large transverse momentum $p_T$ are required. For particle identification requirements on the difference between the logarithm of the likelihood for the muon, electron, kaon or proton and the pion hypothesis are applied. In case of multiple candidates from one tagging algorithm the candidate with the highest transverse momentum is chosen.

In contrast to this method the OS vertex charge tagger does not use single tracks but a weighted charge of a secondary vertex to arrive at a tag decision. The secondary vertex is reconstructed from two tracks which have the highest probability to originate from the OS $b$ hadron. From this seed
more tracks that are compatible with coming from the secondary vertex but not from the primary vertex are added to the vertex to form the final $b$ hadron candidate. Finally a weighted charge is calculated as a sum of the charges $Q_i$ of all tracks associated to the vertex

$$Q_{vtx} = \frac{\sum_i p_{T}^{k}(i)Q_i}{\sum_i p_{T}^{k}(i)},$$

weighted by their transverse momentum $p_T$ to the power $k$. The value $k$ optimises the effective tagging efficiency.

For the same side tagging one has to distinguish between $B^0_d$ and $B^0_s$ mesons as the accompanying quark is a $d$ or a $s$ quark, respectively. In case of a $B^0_d$ meson an additional charged pion from the $d$ quark, which can hadronise with an $u$ quark, emerges. Also pions from excited states as $B^*$ and $B^{**}$ have the same charge as pions from the direct fragmentation process with a $B^0$ meson. Therefore the pion candidates are required to be charged particles with high momentum and transverse momentum originating from the primary vertex \[11\]. If the signal $B$ meson is a $B^0_s$, a kaon can be formed from the additional $s$ quark and an $u$ quark.

### 2.1 SS kaon tagging using neural nets (NN)

The first version of the SS kaon tagger developed at the LHCb experiment uses a selection based on a sequential set of requirements on some discriminating variables to identify the tagging kaon and a neural net (NN) to estimate the mistag probability $\eta$. An updated version of this tagger, the SS kaon neural net tagger, uses two NN. The first NN distinguishes between fragmentation tracks and the underlying event tracks (see figure 2.1). The fragmentation tracks are the signal tracks for the SS kaon tagger, i.e. the tracks are the searched tagging particle tracks \[2\]. The second NN assigns the final tag and mistag \[3\].

Compared to the “cut-based” SS kaon, the SS kaon NN gives a relative improvement of 50% (41%) in $\epsilon_{\text{eff}}$ for $B^0 \rightarrow D^{-} \pi^+$ ($B^0 \rightarrow J/\psi \phi$). This improvements can be observed also when comparing the
2.2 OS charm tagger

A novel tagger introduced at the end of Run I is the OS charm tagger. It uses charm hadrons from the decay chain \( b \rightarrow c \) from the opposite side \( b \) quark to tag the initial flavour. The reconstructed \( D \) modes related to the OS \( b \) decay are listed in table 2.2. For each mode one boosted decision tree is used to calculate the mistag probability \( \eta \) and then the candidate with the best prediction is picked [9]. The OS charm tagger provides a relatively clean measure of the \( B \) flavour, i.e. it provides low values of \( \eta \). Depending on the decay mode its stand-alone effective tagging efficiency is between 0.30 % and 0.40 % [9].

3. Calibration of the Flavour Tagging

The mistag estimate \( \eta \) provided by the different tagging algorithms has to be corrected and transformed into the true mistag probability \( \omega \). This is achieved by using a linear calibration function

\[
\omega(\eta) = p_0 + p_1 (\eta - \langle \eta \rangle) \tag{3.1}
\]
Table 2: $D$ meson decay modes with their relative contributions to $\varepsilon_{\text{tag}}$ and $\varepsilon_{\text{eff}}$ which are used by the OS charm tagger.

<table>
<thead>
<tr>
<th>Decay mode</th>
<th>Relative $\varepsilon_{\text{tag}}$</th>
<th>Relative $\varepsilon_{\text{eff}}$</th>
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<tbody>
<tr>
<td>$D^0 \rightarrow K^- \pi^+$</td>
<td>10.0 %</td>
<td>24.0 %</td>
</tr>
<tr>
<td>$D^0 \rightarrow K^- \pi^+ \pi^+$</td>
<td>5.9 %</td>
<td>8.4 %</td>
</tr>
<tr>
<td>$D^+ \rightarrow K^- \pi^+$</td>
<td>10.3 %</td>
<td>2.6 %</td>
</tr>
<tr>
<td>$D^0, D^+ \rightarrow K^- \pi^+ X$</td>
<td>69.7 %</td>
<td>61.5 %</td>
</tr>
<tr>
<td>$D^0, D^+ \rightarrow K^- e^+ X$</td>
<td>0.5 %</td>
<td>0.2 %</td>
</tr>
<tr>
<td>$D^0, D^+ \rightarrow K^- \mu^+ X$</td>
<td>3.4 %</td>
<td>0.3 %</td>
</tr>
<tr>
<td>$\Lambda_c^+ \rightarrow p^+ K^- \pi^+$</td>
<td>0.2 %</td>
<td>2.4 %</td>
</tr>
</tbody>
</table>

where $\langle \eta \rangle$ is the mean mistag estimate. The parameters $p_0$ and $p_1$ of this calibration function are extracted in two different ways. Using charged decay modes as $B^+ \rightarrow J/\psi K^+$ and $B^+ \rightarrow D^0 \pi^+$ the true mistag $\omega$ can be extracted by comparing the tag decision with the charge of the kaon or pion in the final state. In neutral decay modes as $B^0 \rightarrow J/\psi K^*0$, $B^0 \rightarrow D^*^- \mu^+ \nu_\mu$ or $B^0_s \rightarrow D^- s \pi^+$ a full time-dependent analysis is needed to extract omega from the mixing asymmetry:

$$A_{\text{mix}}(t) \propto (1 - 2 \omega) \cos(\Delta m_d/s t)$$

(3.2)

In both cases the calculation of $\omega$ is done in bins of the mistag estimate $\eta$ and the linear function in Eq. 3.1 is fitted to the $(\omega, \eta)$ pairs. Figure 3 shows the time dependent mixing asymmetry of Eq. 3.2 in the case of the $B^0 \rightarrow J/\psi K^*0$ decay and the linear calibration function resulting from the simultaneous fit in all bins of $\eta$.

In time-dependent analyses of neutral $b$ mesons, systematic uncertainties coming from the Flavour Tagging are assigned for the uncertainties associated with the calibration method and for the portability of the calibration from the control to the signal decay mode as the calibration depends on the kinematics of the control decay. Adding these two categories of systematic uncertainties, the size of the systematic uncertainty is of the order of the size of the statistical uncertainty on the calibration. For most analyses during Run I the systematic uncertainties are much smaller than the
statistical uncertainties. Therefore for most analyses one calibration per tagger valid for all signal channels, taking into account the differences between all control channels, is provided. For analyses with systematic uncertainties of the order of the statistical uncertainties and with systematic uncertainties dominated by the uncertainties from the flavour tagging calibration an “ad-hoc” calibration using the best-suited control channel for the analyses is performed.

3.1 CP violation in \( B^0 \to J/\psi K^0_S (\sin 2\beta) \)

The measurement of CP violation in \( B^0 \to J/\psi K^0_S \) is performed on 1 fb\(^{-1} \) and updated using the full Run I dataset of 3 fb\(^{-1} \). The effective tagging power increases from \( \epsilon = 2.38\% \) (1 fb\(^{-1} \)) [10] to \( \epsilon = 3.02\% \) (3 fb\(^{-1} \)) [11]. This increase is mainly due to the use of the SS pion tagger which adds more than 0.376 % in the newest analysis. In this measurement, the statistical uncertainties are at the level of systematic uncertainties originating from the standard flavour tagging calibration. Thus, an “ad-hoc” calibration is performed: The OS taggers are calibrated with the control channel \( B^+ \to J/\psi K^+ \), the SS pion tagger is calibrated with \( B^0 \to J/\psi K^{*0} \). The two decay modes are ideal calibration channels for this measurement: The high event yields allow for a precise determination of the calibration function parameters, while the kinematic similarity to the signal mode ensures the portability of the calibration from the control to the signal mode. The latter is checked by reweighting the control modes in the kinematic variables that influence the tagging response according to the signal decay and repeating the calibration procedure. Only small changes in the calibration result are found, thus leading to a decrease of the systematic uncertainties originating from the flavour tagging 33 % of the total systematic uncertainty [11].

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