The Energy Content of Extensive Air Showers in the Radio Frequency Range of 30-80 MHz

Christian Glaser\textsuperscript{*a} for the Pierre Auger Collaboration\textsuperscript{b}

\textsuperscript{a}RWTH Aachen University, Aachen, Germany
\textsuperscript{b}Observatorio Pierre Auger, Av. San Martín Norte 304, 5613 Malargüe, Argentina
E-mail: auger_spokespersons@fnal.gov
Full author list: http://www.auger.org/archive/authors_2015_06.html

At the Auger Engineering Radio Array (AERA) of the Pierre Auger Observatory, we have developed a new method to measure the total amount of energy that is transferred from the primary cosmic ray into radio emission. We find that this radiation energy is an estimator of the cosmic ray energy. It scales quadratically with the cosmic ray energy, as expected for coherent emission. We measure 15.8 MeV of radiation energy for a 1 EeV air shower arriving perpendicular to the geomagnetic field at the Auger site, in the frequency band of the detector from 30 to 80 MHz. These observations are compared to the data of the surface detector of the Observatory, which provide well-calibrated energies and arrival directions of the cosmic rays. We find energy resolutions of the radio reconstruction of 22\% for the complete data set, and 17\% for a high-quality subset containing only events with at least five stations with signal.

\textsuperscript{*}Speaker.
1. Introduction

The detection of ultra-high energy cosmic rays via short radio pulses that are emitted during the air shower development has become an active field of research in recent years [1, 2, 3, 4, 5, 6, 7]. One advantage of this technique is a detection of cosmic rays that is sensitive to the particle type at close to a 100% duty cycle. The potential for a large scale radio detector is currently being explored in several experiments.

Much progress has been achieved in the understanding of the radio emission process. The dominant process is the geomagnetic emission that is due to the deflection of charged shower particles in the Earth’s magnetic field which is polarized in the direction of the Lorentz force that acts on the shower particles [1, 3, 8]. The second component is polarized radially with respect to the axis of the air shower and results from the negative charge excess in the shower front [9, 10, 11, 12]. Its relative strength is on average 14% at the Auger site for an air shower arriving perpendicular to the geomagnetic field [13]. The constructive and destructive interference of the two emission processes lead to a radial asymmetry of the lateral signal distribution function (LDF) [14, 15, 16] that can be modeled with a two-dimensional LDF [17, 18].

The Auger Engineering Radio Array (AERA) [19] at the Pierre Auger Observatory [20] is the world’s largest cosmic ray radio detector. In its latest stage of expansion, it consists of 153 radio detector stations that cover an area of approximately 17 km$^2$. AERA can take advantage of the fluorescence and surface detectors (SD) of the Pierre Auger Observatory that provide well-calibrated energies and arrival directions of the cosmic rays. The radio detector (RD) stations of AERA are located in an area of denser detector spacing of the SD array. This region, with SD station spacing of 0.75 km, allows the detection of cosmic ray energies down to about 0.1 EeV.

2. Data selection and event reconstruction

In this work we are using RD and SD data recorded between April 2011 and March 2013 when AERA was operating in its first phase. In this phase, AERA consisted of 24 antenna stations with a spacing of 144 m. The stations are equipped with logarithmic-periodic dipole antennas and measure over a frequency range of 30 to 80 MHz [21]. We use only events that have been measured by the radio and surface detectors in coincidence.

The raw data are reconstructed using the software framework Offline of the Pierre Auger Collaboration [22, 23]. We correct for the influence of the analog signal chain using the absolute calibration of the AERA station and reconstruct a three-dimensional electric field by using the direction of the shower and applying the simulated antenna response [21]. An example of a reconstructed electric field trace $\vec{E}(t)$ is shown in Fig. 1.

We determine the energy density $u$ of the incoming electromagnetic radio pulse at each radio station by calculating the time integral over the absolute value of the Poynting vector. We add up the square of the magnitude of the electric field trace in a time-window of 200 ns ($[t_1,t_2]$) around the pulse maximum. The pulse maximum has been determined from the Hilbert envelope of the trace. We subtract the contribution of background noise (determined in the noise window $[t_3,t_4]$) under the assumption that the main contribution is white noise. The energy density $u$, in units of
eV/m², is given by

\[ u = \varepsilon_0 c \left( \Delta t \sum_{t_1}^{t_2} |\vec{E}(t)|^2 - \Delta t \frac{t_2 - t_1}{t_4 - t_3} \sum_{t_1}^{t_4} |\vec{E}(t)|^2 \right), \]  

(2.1)

where \( \varepsilon_0 \) is the vacuum permittivity, \( c \) is the speed of light in vacuum, \( \Delta t \) is the size of one time bin. To approximate the uncertainty the noise level is used. In addition, the amplification of the signal chain adds 5% uncertainty in \( u \) that is added in quadrature.

We apply quality cuts on the data of the surface detector [24]. The most important cuts are that the core position be surrounded by a hexagon of active stations and that the zenith angle of the incoming direction be less than 55°. Furthermore, we require that the reconstructed incoming direction from the radio and the surface detectors agree within 20°, that the event not be recorded during thunderstorms and we impose a cut on the measured polarization to efficiently reject noise pulses. 134 events remain after all cuts.

3. Radiation energy and energy estimator

To reconstruct the radiation energy, i.e., the energy that has been transferred from the cosmic ray into radiation in the 30 to 80 MHz regime, the energy density – measured at the individual radio stations – is interpolated spatially and integrated. We use a two-dimensional lateral signal distribution function that describes all main features seen in simulated and measured cosmic ray radio events [17]. We parametrize the function with four free parameters, namely the amplitude \( A \), the slope parameter \( \sigma \) and the particle core position \( \vec{r}_{\text{core}} \). The remaining constants \( C_0 \) – \( C_4 \) are estimated from Monte Carlo simulations for the AERA site (see Tab. 1). Thus we find

\[ u(\vec{r}) = A \left[ \exp \left( - \left( \overrightarrow{\vec{r}} + C_1 \vec{e}_{\vec{v} \times \vec{B}} - \vec{r}_{\text{core}} \right)^2 / \sigma^2 \right) - C_0 \exp \left( - \left( \overrightarrow{\vec{r}} + C_2 \vec{e}_{\vec{v} \times \vec{B}} - \vec{r}_{\text{core}} \right)^2 / (C_3 e^{C_4} \sigma^2) \right) \right]. \]  

(3.1)

All coordinates are in the shower plane and \( \overrightarrow{\vec{r}} \) denotes the station position. \( \vec{e}_{\vec{v} \times \vec{B}} \) is the unit vector pointing into the polarization direction of the geomagnetic emission. The LDF is fitted to the data.

Figure 1: Reconstructed electric field trace of one of the measured cosmic ray radio events. An upsampling by a factor of five was applied. The shown Hilbert envelope (dashed line) is the square root of the quadratic sum of the Hilbert envelopes of the three polarization components.
Figure 2: Lateral signal distribution of an air shower with an energy of 0.65 EeV and arriving at a zenith angle of 21° and from 31° east of north. Left: Two dimensional distribution of the RD energy density in the shower plane. The coordinate origin is the RD shower core. The star indicates the SD core position. Circles and squares mark the positions of the radio stations. The color shows the measured energy density. Stations with signal below threshold are marked with gray squares. The background map shows the LDF parametrization. Right: One-dimensional projection of the LDF. Blue squares show the measured energy density and gray squares denote the sub-threshold stations. Gray circles denote the value of the LDF parametrization at the position of the measurement. The radial fall-off of the LDF along a line connecting the radio core position with each station position is shown as gray curves. Also shown are the residuals in units of the uncertainty of the measurement.

using a chi-square minimization. In case of low station multiplicity, the particle core position is taken from the SD reconstruction, which enables us to also use events with signals in only three or four radio stations. After a quality cut on the LDF fit, 126 events remain. An example of one air shower of our data set is shown in Fig. 2.

The radiation energy is the spatial integral of the LDF and will be given in units of eV. To obtain a cosmic ray energy estimator we correct for the different emission strengths at different angles $\alpha$ between the shower axis and the magnetic field by dividing the radiation energy by $\sin^2 \alpha$:

$$S_{\text{radio}} = \frac{1}{\sin^2 \alpha} \int_{\mathbb{R}^2} u(\vec{r}) \, d^2 \vec{r} = \frac{A \pi}{\sin^2 \alpha} \left( \sigma^2 - C_0 C_2^2 e^{2C_4 \sigma} \right),$$

(3.2)

where $\mathbb{R}^2$ denotes the shower plane. The formula is valid for values of $\alpha > 10^\circ$. For smaller values of $\alpha$ the geomagnetic emission is not the dominant contribution and the $\sin^2 \alpha$ correction becomes invalid. However, due to the reduced emission strength the number of detections for arrival directions within 10° of the geomagnetic axis is suppressed. In our data set all events have arrival directions further away from the magnetic field axis.

The dominant event by event uncertainties of the energy estimator are the uncertainty of the LDF fit, the antenna response pattern (10%) and the temperature dependence of the amplifiers (8%) that is not yet corrected for. The average fit uncertainty of $S_{\text{radio}}$ is 46% and reduces to 24% in case of events with five or more stations with signal. The absolute scale uncertainty of the energy estimator is dominated by the absolute scale uncertainty of the antenna response pattern (25%) [21] and the analog signal chain (12%) and amounts to 28%. All uncertainties are added in quadrature. Please note that as the energy estimator scales quadratically with the cosmic ray...
energy, the resulting uncertainty of the cosmic ray energy will be only half of the uncertainty of the energy estimator.

The energy estimator $S_{\text{radio}}$ is calibrated using air showers measured with AERA and the surface detector in coincidence. $S_{\text{radio}}$ shows a clear correlation with the cosmic ray energy measured by the surface detector (cf. Fig. 3). The calibration function $S_{\text{radio}} = A \times 10^7 \text{eV} (E_{\text{SD}}/10^{18} \text{eV})^B$ is obtained by maximizing a likelihood function that takes all measurement uncertainties, detector efficiencies and the steeply falling energy spectrum into account. This method was previously used in [25, 26] and is documented in [27]. The result of the calibration fit is $A = 1.58 \pm 0.07$ and $B = 1.98 \pm 0.04$. For a high quality subset of events with at least five radio stations with signal (47 events) the fit gives a compatible result of $A = 1.60 \pm 0.08$ and $B = 1.99 \pm 0.05$.

To estimate the energy resolution of AERA we subtract the known SD energy resolution from the scatter around the calibration curve, assuming that the energy estimators of the SD and RD are uncorrelated for a fixed cosmic ray energy. We find a resolution of 22% for the full data set and 17% for the high quality set. We also compare the observed and the expected scatter that can be calculated from the likelihood function and the uncertainties of the SD energy estimator and $S_{\text{radio}}$.
discussed above and we find that the observed scatter is compatible with our expectation. As the radio energy estimator is calibrated with SD data, we inherit the systematic uncertainty of the SD energy scale. It is 14% at energies $\geq 10^{18}$ eV [28] and increases to 16% at $10^{17.5}$ eV.

4. The energy content of extensive air showers in the radio frequency range of 30 to 80 MHz

We can generalize our results to other locations by normalizing the calibration function to the local magnetic field. Then, we can predict the radiation energy in the frequency range of 30 to 80 MHz by

$$E_{30-80\text{MHz}} = (15.8 \pm 0.7\text{(stat)} \pm 6.7\text{(sys)}) \text{MeV} \left( \frac{\sin \alpha}{10^{18}\text{eV}} \frac{B_{\text{Earth}}}{0.24\text{G}} \right)^2,$$

where $E$ is the cosmic ray energy, $B_{\text{Earth}}$ denotes the local magnetic field strength and 0.24 G is the magnetic field strength at the AERA site. We found that it is sufficient to correct only for the dominant geomagnetic emission process. However, this formula will become invalid for radio detectors at high altitudes because the amount of radiation energy decreases as – depending on the zenith angle – a significant part of the air shower is clipped away at the ground.

The direct measurement of the radiation energy holds further potential for a precise determination of the cosmic ray energy scale. Radio emission originates only from the electromagnetic part of an air shower. Therefore, the radiation energy can be predicted by Monte Carlo simulations from first principles [16, 29], as the emission arises from the acceleration/deceleration of charges which is described by classical electrodynamics [30]. In addition, no relevant propagation uncertainties arise as the atmosphere is transparent for radio emission. Then, in turn, the energy scale of the radio detector can be propagated to the other detection techniques.

5. Conclusions

We have presented a direct measurement of the radiation energy of an extensive air shower in the 30 to 80 MHz regime. The AERA radio stations are well calibrated which enables the reconstruction of the energy density of the radio pulse at each detector position. The radiation energy is then the integral of the two-dimensional lateral signal distribution function that is fitted to the data. We measure 15.8 MeV of radiation energy for a 1 EeV cosmic ray arriving perpendicular to the local magnetic field.

As a cosmic ray energy estimator we use this radiation energy corrected for different emission strengths at different angles between the shower axis and the geomagnetic field. We calibrate the energy estimator using the reconstructed energy from the surface detector of the Pierre Auger Observatory and find that the radio energy estimator scales quadratically with the cosmic ray energy. We analyze the scatter around the calibration and find an energy resolution of the radio detector of 22%. The resolution improves to 17% for a high quality subset of the data where only events with at least five radio stations with signal are used.

We generalize our result by normalizing the calibration function to the local magnetic field strength at the Auger site. This leads to a universal prediction of the radiation energy that can be used at any location.
Table 1: Parameters $C_0 - C_4$ of Eq. (3.1). $C_3 = 16.25 \text{m}$ and $C_4 = 0.0079 \text{m}^{-1}$. The zenith angle dependent values used to predict the emission pattern are given for zenith angle bins up to 60°.

<table>
<thead>
<tr>
<th>Zenith Angle</th>
<th>$C_0$</th>
<th>$C_1$ [m]</th>
<th>$C_2$ [m]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0° - 10°</td>
<td>0.41</td>
<td>8.0 ± 0.3</td>
<td>-21.2 ± 0.4</td>
</tr>
<tr>
<td>10° - 20°</td>
<td>0.41</td>
<td>10.0 ± 0.4</td>
<td>-23.1 ± 0.4</td>
</tr>
<tr>
<td>20° - 30°</td>
<td>0.41</td>
<td>12.0 ± 0.3</td>
<td>-25.5 ± 0.3</td>
</tr>
<tr>
<td>30° - 40°</td>
<td>0.41</td>
<td>20.0 ± 0.4</td>
<td>-32.0 ± 0.6</td>
</tr>
<tr>
<td>40° - 50°</td>
<td>0.46</td>
<td>25.1 ± 0.9</td>
<td>-34.5 ± 0.7</td>
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<tr>
<td>50° - 60°</td>
<td>0.71</td>
<td>27.3 ± 1.0</td>
<td>-9.8 ± 1.5</td>
</tr>
</tbody>
</table>

References


A. Schulz for the Pierre Auger Collaboration, *The measurement of the energy spectrum of cosmic rays above $3 \times 10^{17}$ eV with the Pierre Auger Observatory*, Proc. **33rd ICRC**, Rio de Janeiro, Brazil (2013) [1307.5059v1].


