

# A DIS Event Shape at N<sup>3</sup>LL \*

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A high precision calculation of the event shape DIS thrust, with next-to-next-to-next-to-leadinglogarithmic resummation and a rigorous treatment of hadronization corrections, is presented. Perturbative resummation uncertainties in the cross section are reduced to the 2% level for a significant region of the HERA phase space in *x* and *Q*, thus allowing for new accurate measurements of  $\alpha_s(m_Z)$ .

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Event shapes provide a key method of measuring jets in deep-inelastic scattering (DIS). This was done successfully by H1 and ZEUS [1, 2, 3, 4, 5, 6] and compared with theoretical calculations with next-to-leading-logarithmic (NLL) resummation [7, 8]. Here we consider the event shape DIS thrust,  $\tau$ , which is defined in the Breit frame using the momentum of the exchanged  $\gamma$  or Z-boson to determine the z-axis, q = (0,0,0,Q). It can be measured solely from events in the current hemisphere where z > 0 via  $\tau = 1 - (2/Q) \sum_{i \in \mathcal{H}_j} p_{iz}$ , thus avoiding the lack of detector coverage in parts of the beam region. The event shape  $\tau$  also does not suffer from non-global logarithms [8].

Recently an all orders factorization theorem was derived for  $d\sigma/d\tau$  [9], which enables higher order perturbative results to be obtained, and a more rigorous treatment of power corrections,

$$\frac{1}{\sigma_0}\frac{d\sigma}{dxdQ^2d\tau} = QH(Q,x,\mu)\int dt_B dt_J d^2 p_\perp B_q(t_B,x,\vec{p}_\perp^2,\mu) J_q(t_J-\vec{p}_\perp^2,\mu) S\left(Q\tau-\frac{t_B+t_J}{Q},\mu\right).$$
(1)

Results with a resummation of the singular  $\alpha_s^k \ln^j \tau/\tau$  terms at next-to-next-to-leading-log (NNLL) order were given in [9]. Here we extend this analysis to one higher order, N<sup>3</sup>LL, by exploiting the recent 2-loop calculation of the quark beam function  $B_q$  [10, 11], the 2-loop DIS soft function S [12, 13, 14, 15], and known results for the 2-loop hard function H and jet function  $J_q$ , and their 3-loop anomalous dimensions [16, 17, 18]. The smaller nonsingular contributions to  $d\sigma/d\tau$  are also now known analytically at  $\mathcal{O}(\alpha_s)$  [19], while numerical results are available at  $\mathcal{O}(\alpha_s^2)$  [20, 21]. Power corrections are encoded by a hadronic matrix element  $\Omega_1$  appearing in S, using formalism developed in Refs. [22, 23, 24, 25, 9]. (The DIS thrust  $\tau$  is equal to the Breit frame 1-jettiness DIS variables were obtained in Refs. [27, 28, 29, 9], currently up to NNLL order.)

Fits for  $\alpha_s(m_Z)$  in the tail region of the DIS  $\tau$  distribution, should simultaneously fit for the power correction  $\Omega_1$  (similar to the highly successful fits for the  $e^+e^-$  thrust event shape in [30]). This is facilitated by considering  $d\sigma/d\tau$  from multiple *x* and *Q* values. Interestingly, the factorization theorem in Eq. (1) remains valid for relatively small *x*, and the fractional contribution from the nonsingular corrections even decreases with decreasing *x*, as shown at  $\mathcal{O}(\alpha_s)$  in [31].

In Fig. 1 we show the convergence of the DIS thrust cross section and decrease in the perturbative resummation uncertainty when going from NLL to NNLL to N<sup>3</sup>LL order. Results are displayed for a representative value of x and Q, while cross sections for other values can be found in [31]. In Fig. 2 we show the percent uncertainty of  $d\sigma/d\tau$  for various values of x and Q in the region accessible by HERA, demonstrating that the theoretical resummation uncertainties become as low as 2% in accessible regions of the phase space. Values are obtained as the average uncertainty in  $d\sigma/d\tau$  in the tail region  $0.15 < \tau < 0.35$ . In Fig. 3 we show how much the cross section changes with variations of the input parameters  $\alpha_s(m_Z)$  and  $\Omega_1$ , as well as comparing the  $\alpha_s(m_Z)$ sensitivity to the N<sup>3</sup>LL resummation uncertainties, and to the uncertainties from the NNLO MSTW parton distributions [32]. Figures for other values of x and Q are available in [31]. The degeneracy between  $\alpha_s(m_Z)$  and  $\Omega_1$  is broken by measurements at multiple Q. The theoretical precision of our N<sup>3</sup>LL cross section indicates that measurements with 1-2% uncertainty in  $\alpha_s(m_Z)$  should now be possible. A measurement of  $\Omega_1$  from DIS is also of broader use, since this same  $\Omega_1$  parameter occurs in  $pp \rightarrow Z + 1$ -jet, where it yields the power correction for the jet-mass that is linear in the jet radius [33].



**Figure 1:** Convergence of the DIS thrust distribution. Results at three orders are shown along with their perturbative uncertainty. Left panel shows  $\tau d\sigma/d\tau$ . Right panel shows the relative uncertainty for  $d\sigma/d\tau$ .



**Figure 2:** Percent uncertainty of our N<sup>3</sup>LL cross section for the region in *x* and *Q* accessible at HERA. Uncertainties are for the tail of the DIS thrust distribution which can be used to measure  $\alpha_s(m_Z)$ . Also shown are the points used for past DIS event shape measurements.



**Figure 3:** Sensitivity of the DIS thrust cross section to changes in  $\alpha_s(m_Z)$  and  $\Omega_1$  (left panel) and compared with PDF and N<sup>3</sup>LL uncertainties (right panel).

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