

Observable Gravitational Waves From Kinetically Modified Non-Minimal Inflation

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We consider Supersymmetric (SUSY) and non-SUSY models of chaotic inflation based on the simplest power-law potential with exponents $n = 2$ and 4. We propose a convenient non-minimal coupling to gravity and a non-minimal kinetic term which ensure, mainly for $n = 4$, inflationary observables favored by the BICEP2/Keck Array and *Planck* results. Inflation can be attained for subplanckian inflaton values with the corresponding effective theories retaining the perturbative unitarity up to the Planck scale.

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1. Introduction

Kinetically modified *Non-minimal (chaotic) inflation* (nMI) [1] is a variant of nMI which arises in the presence of a non-canonical kinetic term for the inflaton ϕ – apart from the non-minimal coupling $f_R(\phi)$ between ϕ and the Ricci scalar curvature, R which is required by definition in any model of nMI [2]. In this talk we focus on inflationary models based on a synergy between f_R and the inflaton potential V_{CI} , which are selected [1, 3, 4] as follows

$$V_{\text{CI}}(\phi) = \lambda^2 \phi^n / 2^{n/2} \quad \text{and} \quad f_R = 1 + c_R \phi^{n/2} \quad \text{with} \quad n = 2, 4. \quad (1.1)$$

Below, we first (in Sec. 1.1) briefly review the basic ingredients of nMI in a non-*Supersymmetric* (SUSY) framework and constrain the parameters of the models in Sec. 1.3 taking into account a number of observational and theoretical requirements described in Sec. 1.2. Then (in Sec. 1.4) we focus on the problem with perturbative unitarity that plagues [5, 6] these models at the strong coupling and motivate the form of f_K analyzed in our work.

Throughout the text, the subscript χ denotes derivation *with respect to* (w.r.t) the field χ , charge conjugation is denoted by a star (*) and we use units where the reduced Planck scale $m_p = 2.43 \cdot 10^{18}$ GeV is set equal to unity.

1.1 Coupling non-Minimally the Inflaton to Gravity

The action of the inflaton ϕ in the *Jordan frame* (JF), takes the form:

$$S = \int d^4x \sqrt{-g} \left(-\frac{f_R}{2} R + \frac{f_K}{2} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - V_{\text{CI}}(\phi) \right). \quad (1.2)$$

where g is the determinant of the background Friedmann-Robertson-Walker metric, $g^{\mu\nu}$ with signature $(+, -, -, -)$, $\langle f_R \rangle \simeq 1$ to guarantee the ordinary Einstein gravity at low energy and we allow for a kinetic mixing through the function $f_K(\phi)$. By performing a conformal transformation [3] according to which we define the *Einstein frame* (EF) metric $\hat{g}_{\mu\nu} = f_R g_{\mu\nu}$ we can write S in the EF as follows

$$S = \int d^4x \sqrt{-\hat{g}} \left(-\frac{1}{2} \hat{R} + \frac{1}{2} \hat{g}^{\mu\nu} \partial_\mu \hat{\phi} \partial_\nu \hat{\phi} - \hat{V}_{\text{CI}}(\hat{\phi}) \right), \quad (1.3a)$$

where hat is used to denote quantities defined in the EF. We also introduce the EF canonically normalized field, $\hat{\phi}$, and potential, \hat{V}_{CI} , defined as follows:

$$\frac{d\hat{\phi}}{d\phi} = J = \sqrt{\frac{f_K}{f_R} + \frac{3}{2} \left(\frac{f_{R,\phi}}{f_R} \right)^2} \quad \text{and} \quad \hat{V}_{\text{CI}} = \frac{V_{\text{CI}}}{f_R^2}, \quad (1.3b)$$

where the symbol ϕ as subscript denotes derivation w.r.t the field ϕ . Plugging Eq. (1.1) into Eq. (1.3b), we obtain

$$J^2 = \frac{f_K}{f_R} + \frac{3n^2 c_R^2 \phi^{n-2}}{8f_R^2} \quad \text{and} \quad \hat{V}_{\text{CI}} = \frac{\lambda^2 \phi^n}{2^{n/2} f_R^2}. \quad (1.4)$$

In the pure nMI [2–4] we take $f_K = 1$ and, for $c_R \gg 1$, we infer from Eq. (1.3b), that f_R determines the relation between $\hat{\phi}$ and ϕ and controls the shape of \hat{V}_{CI} affecting thereby the observational predictions – see below.

1.2 Inflationary Observables – Constraints

A model of nMI can be qualified as successful, if it can become compatible with the following observational and theoretical requirements:

- (i) The number of e-foldings \widehat{N}_* that the scale $k_* = 0.05/\text{Mpc}$ experiences during this nMI must be enough for the resolution of the horizon and flatness problems of standard Big Bang, i.e., [7]

$$\widehat{N}_* = \int_{\widehat{\phi}_f}^{\widehat{\phi}_*} d\widehat{\phi} \frac{\widehat{V}_{\text{Cl}}}{\widehat{V}_{\text{Cl},\widehat{\phi}}} \simeq 55, \quad (1.5)$$

where $\phi_* [\widehat{\phi}_*]$ are the value of ϕ [$\widehat{\phi}$] when k_* crosses the inflationary horizon. Also $\phi_f [\widehat{\phi}_f]$ is the value of ϕ [$\widehat{\phi}$] at the end of nMI, which can be found, in the slow-roll approximation, from the condition

$$\max\{\widehat{\varepsilon}(\phi_f), |\widehat{\eta}(\phi_f)|\} = 1, \quad \text{where}$$

$$\widehat{\varepsilon} = \frac{1}{2} \left(\frac{\widehat{V}_{\text{Cl},\widehat{\phi}}}{\widehat{V}_{\text{Cl}}} \right)^2 = \frac{1}{2J^2} \left(\frac{\widehat{V}_{\text{Cl},\phi}}{\widehat{V}_{\text{Cl}}} \right)^2 \quad \text{and} \quad \widehat{\eta} = \frac{\widehat{V}_{\text{Cl},\widehat{\phi}\widehat{\phi}}}{\widehat{V}_{\text{Cl}}} = \frac{1}{J^2} \left(\frac{\widehat{V}_{\text{Cl},\phi\phi}}{\widehat{V}_{\text{Cl}}} - \frac{\widehat{V}_{\text{Cl},\phi}}{\widehat{V}_{\text{Cl}}} \frac{J_{,\phi}}{J} \right). \quad (1.6)$$

It is evident from the formulas above that non trivial modifications on f_K and thus to J may have an pronounced impact on the parameters above modifying thereby the inflationary observables too.

- (ii) The amplitude A_s of the power spectrum of the curvature perturbation generated by ϕ at k_* has to be consistent with data [7], i.e.,

$$\sqrt{A_s} = \frac{1}{2\sqrt{3}\pi} \frac{\widehat{V}_{\text{Cl}}(\widehat{\phi}_*)^{3/2}}{|\widehat{V}_{\text{Cl},\widehat{\phi}}(\widehat{\phi}_*)|} = \frac{1}{2\pi} \sqrt{\frac{\widehat{V}_{\text{Cl}}(\widehat{\phi}_*)}{6\widehat{\varepsilon}_*}} \simeq 4.627 \cdot 10^{-5}, \quad (1.7)$$

where the variables with subscript $*$ are evaluated at $\phi = \phi_*$.

- (iii) The remaining inflationary observables (the spectral index n_s , its running a_s , and the tensor-to-scalar ratio r) – estimated through the relations:

$$(a) n_s = 1 - 6\widehat{\varepsilon}_* + 2\widehat{\eta}_*, \quad (b) a_s = \frac{2}{3} (4\widehat{\eta}_*^2 - (n_s - 1)^2) - 2\widehat{\xi}_* \quad \text{and} \quad (c) r = 16\widehat{\varepsilon}_*, \quad (1.8)$$

with $\widehat{\xi} = \widehat{V}_{\text{Cl},\widehat{\phi}} \widehat{V}_{\text{Cl},\widehat{\phi}\widehat{\phi}\widehat{\phi}} / \widehat{V}_{\text{Cl}}^2$ – have to be consistent with the data [7], i.e.,

$$(a) n_s = 0.968 \pm 0.009 \quad \text{and} \quad (b) r \leq 0.12, \quad (1.9)$$

at 95% confidence level (c.l.) – pertaining to the $\Lambda\text{CDM}+r$ framework with $|a_s| \ll 0.01$. Although compatible with Eq. (1.9b) the present combined *Planck* and *BICEP2/Keck Array* results [8] seem to favor r 's of order 0.01 since $r = 0.048_{-0.032}^{+0.035}$ at 68% c.l. has been reported.

- (iv) The effective theory describing nMI has to remain valid up to a UV cutoff scale Λ_{UV} to ensure the stability of our inflationary solutions, i.e.,

$$(a) \widehat{V}_{\text{Cl}}(\phi_*)^{1/4} \leq \Lambda_{\text{UV}} \quad \text{and} \quad (b) \phi_* \leq \Lambda_{\text{UV}}. \quad (1.10)$$

It is expected that $\Lambda_{\text{UV}} \simeq m_{\text{p}}$, contrary to the pure nMI with $c_R \gg 1$ where $\Lambda_{\text{UV}} \ll m_{\text{p}}$ – see Sec. 1.4.

1.3 The Two Regimes of Synergistic nMI

The models of nMI based on Eq. (1.1) exhibit the following two regimes:

(i) The *weak* c_R regime with $c_R \ll 1$. In this case from Eq. (1.3b) we find $J \simeq 1/f_R$ and applying Eqs. (1.5) and (1.6), the slow-roll parameters and \widehat{N}_* read

$$\widehat{\varepsilon} \simeq \frac{n^2}{2\phi^2 f_R}, \quad \widehat{\eta} \simeq 2 \left(1 - \frac{1}{n}\right) \widehat{\varepsilon} - \frac{4+n}{2n} c_R \phi^{\frac{n}{2}} \widehat{\varepsilon} \quad \text{and} \quad \widehat{N}_* \simeq \frac{\phi_*^2}{2n}. \quad (1.11)$$

Imposing the condition of Eq. (1.6) and solving then the latter equation w.r.t ϕ_* we arrive at

$$\phi_f \simeq n/\sqrt{2} \quad \text{and} \quad \phi_* \simeq \sqrt{2n\widehat{N}_*}. \quad (1.12)$$

Inflation is attained, thus, only for $\phi > 1$. On the other hand, Eq. (1.7) implies

$$\lambda = \sqrt{6A_s f_{n*} \pi n^{(2-n)/4} / \widehat{N}_*^{(2+n)/4}}, \quad (1.13)$$

where $f_{n*} = f_R(\phi_*) = 1 + c_R(2n\widehat{N}_*)^{n/4}$. Applying Eq. (1.8) we find that the inflationary observables are c_R -dependent and can be marginally consistent with Eq. (1.9) – see Sec. 3.2. Indeed,

$$n_s = 1 - (4 + n + n/f_{n*})/4\widehat{N}_*, \quad r = 4n/f_{n*}\widehat{N}_*, \quad (1.14a)$$

$$a_s = (n^2 - n(n+4)f_{n*} - 4(n+4)f_{n*}^2)/16f_{n*}^2\widehat{N}_*^2. \quad (1.14b)$$

In the limit $c_R \rightarrow 0$ or $f_{n*} \rightarrow 1$ the results of the simplest power-law chaotic inflation – with $f_R = f_K = 1$ and V_{CI} given in Eq. (1.1) – are recovered. These are by now disfavored by Eq. (1.9).

(ii) The *strong* c_R regime with $c_R \gg 1$. In this case, from Eq. (1.3b) we find

$$J \simeq \sqrt{3}n c_R \phi^{n/2-1} / 2\sqrt{2}f_R \quad \text{and} \quad \widehat{V}_{CI} \simeq \lambda^2 / 2^{n/2} c_R^2. \quad (1.15)$$

We observe that \widehat{V}_{CI} exhibits an almost flat plateau. From Eqs. (1.5) and (1.6) we find

$$\widehat{\varepsilon} \simeq 4/3c_R^2 \phi^n, \quad \widehat{\eta} \simeq -4/3c_R \phi^{n/2} \quad \text{and} \quad \widehat{N}_* \simeq 3c_R \phi_*^{n/2} / 4. \quad (1.16)$$

Therefore, ϕ_f and ϕ_* are found from the condition of Eq. (1.6) and the last equality above, as follows

$$\phi_f = \max\{(4/3c_R^2)^{1/n}, (4/3c_R)^{2/n}\} \quad \text{and} \quad \phi_* = (4\widehat{N}_*/3c_R)^{2/n}. \quad (1.17)$$

Consequently, nMI can be achieved even with subplanckian ϕ values for $c_R \gtrsim (4\widehat{N}_*/3)^{2/n}$. Also the normalization of Eq. (1.7) implies the following relation between c_R and λ

$$A_s^{1/2} \simeq 2^{-(10+n)/4} \frac{\lambda c_R \phi^n}{\pi f_R} \Big|_{\phi=\phi_*} \Rightarrow \lambda \simeq \frac{3 \cdot 2^{n/4}}{\widehat{N}_*} \sqrt{2A_s} \pi c_R. \quad (1.18)$$

From Eq. (1.8) we obtain the c_R -independent values for the observables:

$$n_s \simeq 1 - 2/\widehat{N}_* \simeq 0.965, \quad a_s \simeq -2/\widehat{N}_*^2 \simeq -6.4 \cdot 10^{-4} \quad \text{and} \quad r \simeq 12/\widehat{N}_*^2 \simeq 4 \cdot 10^{-3}, \quad (1.19)$$

which are in agreement with Eq. (1.9), although with low enough r values.

1.4 The Ultraviolet (UV) Cut-off Scale

In the highly predictive regime with large c_K , the models violate perturbative unitarity for $n > 2$. To see this we analyze the small-field behavior of the theory in order to extract the UV cut-off scale Λ_{UV} . The result depends crucially on the value of J in Eq. (1.3b) in the vacuum, $\langle \phi \rangle = 0$. Namely we have

$$\langle J \rangle = \begin{cases} \sqrt{3/2}c_R & \text{for } n = 2, \\ 1 & \text{for } n \neq 2. \end{cases} \quad (1.20)$$

For $n = 2$ and any c_R we obtain $\hat{\phi} \neq \phi$. Expanding the second and third term of S in the right-hand side of Eq. (1.3a) about $\langle \phi \rangle = 0$ in terms of $\hat{\phi}$ we obtain:

$$J^2 \dot{\phi}^2 = \left(1 - \sqrt{\frac{8}{3}} \hat{\phi} + 2\hat{\phi}^2 - \dots \right) \dot{\hat{\phi}}^2 \quad \text{and} \quad \hat{V}_{CI} = \frac{\lambda^2 \hat{\phi}^2}{3c_R^2} \left(1 - \sqrt{\frac{8}{3}} \hat{\phi} + 2\hat{\phi}^2 - \dots \right). \quad (1.21)$$

As a consequence $\Lambda_{UV} = m_P$ since the expansions above are c_R independent. On the contrary, for $n > 2$ we have $\hat{\phi} = \phi$ and the expansions of the same terms in Eq. (1.3a) are c_R dependent:

$$J^2 \dot{\phi}^2 = \left(1 - c_R \hat{\phi}^{\frac{n}{2}} + \frac{3n^2}{8} c_R^2 \hat{\phi}^{n-2} + c_R^2 \hat{\phi}^n - \dots \right) \dot{\hat{\phi}}^2; \quad (1.22a)$$

$$\hat{V}_{CI} = \frac{\lambda^2 \hat{\phi}^n}{2} \left(1 - 2c_R \hat{\phi}^{\frac{n}{2}} + 3c_R^2 \hat{\phi}^n - 4c_R^3 \hat{\phi}^{\frac{3n}{2}} + \dots \right). \quad (1.22b)$$

Since the term which yields the smallest denominator for $c_R > 1$ is $3n^2 c_R^2 \hat{\phi}^{n-2}/8$ we find [5, 6]:

$$\Lambda_{UV} = m_P / c_R^{2/(n-2)} \ll m_P. \quad (1.23)$$

However, if we introduce a *non-canonical kinetic mixing* of the form

$$f_K(\phi) = c_K f_R^m \quad \text{where} \quad c_K = (c_R / r_{RK})^{4/n} \quad \text{and} \quad m \geq 0, \quad (1.24)$$

no problem with the perturbative unitarity emerges for $r_{RK} \leq 1$, even if c_R and/or c_K are large – the latter situation is expected if we wish to achieve efficient nMI with $\phi \leq 1$. E.g., for $m = 0$ the expansions in Eqs. (1.22a) and (1.22b) can be rewritten replacing c_R with r_{RK} and λ with $\lambda / c_K^{n/4}$ – similar expressions can be obtained for other m , too. In other words, the perturbative unitarity can be preserved up to m_P if we select a non-trivial f_K such that $\langle J \rangle \neq 1$. This requirement lets a functional uncertainty as regards the form of f_K during nMI which can be parameterized as shown in Eq. (1.24) given that $\langle f_R \rangle \simeq 1$ – see Sec. 1.1.

We below describe a possible formulation of this type of nMI in the context of *Supergravity* (SUGRA) – see Sec. 2 – and we then analyze the inflationary behavior of these models in Sec. 3. We conclude summarizing our results in Sec. 4.

2. Supergravity Embeddings

The models above – defined by Eqs. (1.1) and (1.24) – can be embedded in SUGRA if we use two gauge singlet chiral superfields $z^\alpha = \Phi, S$, with Φ ($\alpha = 1$) and S ($\alpha = 2$) being the inflaton and a “stabilizer” field respectively. The EF action for z^α 's can be written as [9]

$$S = \int d^4x \sqrt{-\hat{g}} \left(-\frac{1}{2} \hat{R} + K_{\alpha\bar{\beta}} \hat{g}^{\mu\nu} \partial_\mu z^\alpha \partial_\nu z^{*\bar{\beta}} - \hat{V} \right), \quad (2.1a)$$

where summation is taken over the scalar fields z^α , K is the Kähler potential with $K_{\alpha\bar{\beta}} = K_{,z^\alpha z^{\bar{\beta}}}$ and $K^{\alpha\bar{\beta}} K_{\bar{\beta}\gamma} = \delta_\gamma^\alpha$. Also \widehat{V} is the EF F-term SUGRA potential given by

$$\widehat{V} = e^K \left(K^{\alpha\bar{\beta}} D_\alpha W D_{\bar{\beta}}^* W^* - 3|W|^2 \right), \quad (2.1b)$$

where $D_\alpha W = W_{,z^\alpha} + K_{,z^\alpha} W$ with W being the superpotential. Along the inflationary track determined by the constraints

$$S = \Phi - \Phi^* = 0, \text{ or } s = \bar{s} = \theta = 0 \quad (2.2)$$

if we express Φ and S according to the parametrization

$$\Phi = \phi e^{i\theta} / \sqrt{2} \quad \text{and} \quad S = (s + i\bar{s}) / \sqrt{2}, \quad (2.3)$$

V_{CI} in Eq. (1.1) can be produced, in the flat limit, by

$$W = \lambda S \Phi^{n/2}. \quad (2.4)$$

SUPERFIELDS:	S	Φ
$U(1)_R$	1	0
$U(1)$	-1	$2/n$

Table 1: Charge assignments of the superfields.

The form of W can be uniquely determined if we impose an R and a global $U(1)$ symmetry with charge assignments shown in Table 1.

On the other hand, the derivation of \widehat{V}_{CI} in Eq. (1.4) via Eq. (2.1b) requires a judiciously chosen K . Namely, along the track in Eq. (2.2) the only surviving term in Eq. (2.1b) is

$$\widehat{V}_{\text{CI}} = \widehat{V}(\theta = s = \bar{s} = 0) = e^K K^{SS^*} |W_S|^2. \quad (2.5)$$

The incorporation f_R in Eq. (1.1) and f_K in Eq. (1.24) dictates the adoption of a logarithmic K [9] including the functions

$$F_R(\Phi) = 1 + 2^{\frac{n}{4}} \Phi^{\frac{n}{2}} c_R, \quad F_K = (\Phi - \Phi^*)^2 \quad \text{and} \quad F_S = |S|^2 - k_S |S|^4. \quad (2.6)$$

Here, F_R is an holomorphic function reducing to f_R , along the path in Eq. (2.2), F_K is a real function which assists us to incorporate the non-canonical kinetic mixing generating by f_K in Eq. (1.24), and F_S provides a typical kinetic term for S , considering the next-to-minimal term for stability/heaviness reasons [9]. Indeed, F_K lets intact \widehat{V}_{CI} , since it vanishes along the trajectory in Eq. (2.2), but it contributes to the normalization of Φ . Taking for consistency all the possible terms up to fourth order, K is written as

$$K_1 = -3 \ln \left(\frac{1}{2} (F_R + F_R^*) + \frac{c_K}{3 \cdot 2^{m+1}} (F_R + F_R^*)^m F_K - \frac{1}{3} F_S + \frac{k_\Phi}{6} F_K^2 - \frac{k_{S\Phi}}{3} F_K |S|^2 \right). \quad (2.7a)$$

Alternatively, if we do not insist on a pure logarithmic K , we could also adopt the form

$$K_2 = -3 \ln \left(\frac{1}{2} (F_R + F_R^*) - \frac{1}{3} F_S \right) - \frac{c_K}{2^m} \frac{F_K}{(F_R + F_R^*)^{1-m}}. \quad (2.7b)$$

Moreover, if we place F_S outside the argument of the logarithm similar results are obtained by the following K 's – not mentioned in Ref. [1]:

$$K_3 = -2 \ln \left(\frac{1}{2} (F_R + F_R^*) + \frac{c_K}{2^{m+2}} (F_R + F_R^*)^m F_K \right) + F_S, \quad (2.7c)$$

$$K_4 = -2 \ln \frac{F_R + F_R^*}{2} - \frac{c_K}{2^m} \frac{F_K}{(F_R + F_R^*)^{1-m}} + F_S. \quad (2.7d)$$

FIELDS	EINGESTATES	MASSES SQUARED			
		SYMBOL	$K = K_1$	$K = K_2$	$K = K_{i+2}$
2 real scalars	$\hat{\theta}$	\hat{m}_θ^2	$4\hat{H}_{\text{CI}}^2$	$6\hat{H}_{\text{CI}}^2$	
1 complex scalar	$\hat{s}, \hat{\bar{s}}$	\hat{m}_s^2	$6(2k_S f_R - 1/3)\hat{H}_{\text{CI}}^2$	$12k_S \hat{H}_{\text{CI}}^2$	
4 Weyl spinors	$\hat{\psi}_\pm$	$\hat{m}_{\psi_\pm}^2$	$3n^2 \hat{H}_{\text{CI}}^2 / 2c_K \phi^2 f_R^{1+m}$		

Table 2: Mass-squared spectrum for $K = K_i$ and $K = K_{i+2}$ ($i = 1, 2$) along the path in Eq. (2.2).

Note that for $m = 0$ [$m = 1$], F_R and F_K in K_1 and K_3 [K_2 and K_4] are totally decoupled, i.e. no higher order term is needed. Also we use only integer prefactors for the logarithms avoiding thereby any relevant tuning – cf. Ref. [10]. Our models, for $c_K \gg c_R$, are completely natural in the 't Hooft sense because, in the limits $c_R \rightarrow 0$ and $\lambda \rightarrow 0$, the theory enjoys the enhanced symmetries

$$\Phi \rightarrow \Phi^*, \Phi \rightarrow \Phi + c \quad \text{and} \quad S \rightarrow e^{i\alpha} S, \quad (2.8)$$

where c is a real number. It is evident that our proposal is realized more attractively within SUGRA than within the non-SUSY set-up, since both f_K and f_R originate from the same function K .

To verify the appropriateness of K 's in Eqs. (2.7a) – (2.7d), we can first remark that, along the trough in Eq. (2.2), these are diagonal with non-vanishing elements K_{SS^*} and $K_{\Phi\Phi^*} = J^2$, where J is given by Eq. (1.4) for $K = K_i$ and Eq. (1.4) replacing $3/8$ by $1/4$ for $K = K_{i+2}$. Substituting into Eq. (2.5) $K^{SS^*} = 1/K_{SS^*}$ and $\exp K = 1/f_R^N$, where

$$K_{SS^*} = \begin{cases} 1/f_R & \text{and } N = \begin{cases} 3 \\ 2 \end{cases} \quad \text{for } K = \begin{cases} K_i \\ K_{i+2} \end{cases} \quad \text{with } i = 1, 2, \end{cases} \quad (2.9)$$

we easily deduce that \hat{V}_{CI} in Eq. (1.4) is recovered. If we perform the inverse of the conformal transformation described in Eqs. (1.3a) and (1.2) with frame function $\Omega/N = -e^{-K/N}$ we can easily show that $f_R = -\Omega/N$ along the path in Eq. (2.2). Note, finally, that the conventional Einstein gravity is recovered at the SUSY vacuum, $\langle S \rangle = \langle \Phi \rangle = 0$, since $\langle f_R \rangle \simeq 1$.

Defining the canonically normalized fields via the relations $d\hat{\phi}/d\phi = \sqrt{K_{\Phi\Phi^*}} = J$, $\hat{\theta} = J\theta\phi$ and $(\hat{s}, \hat{\bar{s}}) = \sqrt{K_{SS^*}}(s, \bar{s})$ we can verify that the configuration in Eq. (2.2) is stable w.r.t the excitations of the non-inflaton fields. Taking the limit $c_K \gg c_R$ we find the expressions of the masses squared $\hat{m}_{\chi^\alpha}^2$ (with $\chi^\alpha = \theta$ and s) arranged in Table 2, which approach rather well the quite lengthy, exact formulas. From these expressions we appreciate the role of $k_S > 0$ in retaining positive \hat{m}_s^2 . Also we confirm that $\hat{m}_{\chi^\alpha}^2 \gg \hat{H}_{\text{CI}}^2 = \hat{V}_{\text{CI}0}/3$ for $\phi_f \leq \phi \leq \phi_*$. In Table 2 we display the masses $\hat{m}_{\psi_\pm}^2$ of the corresponding fermions too with eignestates $\hat{\psi}_\pm = (\hat{\psi}_\Phi \pm \hat{\psi}_S)/\sqrt{2}$, defined in terms of $\hat{\psi}_S = \sqrt{K_{SS^*}}\psi_S$ and $\hat{\psi}_\Phi = \sqrt{K_{\Phi\Phi^*}}\psi_\Phi$, where ψ_Φ and ψ_S are the Weyl spinors associated with S and Φ respectively. Note, finally, that $\hat{m}_{\chi^\alpha} \ll m_P$, for any χ^α , contrary to similar cases [11] where the inflaton belongs to gauge non-singlet superfields.

Inserting the derived mass spectrum in the well-known Coleman-Weinberg formula, we can find the one-loop radiative corrections, $\Delta\hat{V}_{\text{CI}}$ to \hat{V}_{CI} . It can be verified that our results are immune from $\Delta\hat{V}_{\text{CI}}$, provided that the renormalization group mass scale Λ , is determined conveniently and $k_{S\Phi}$ and k_S are confined to values of order unity.

3. Results

The present inflationary scenario depends on the parameters: n , m , r_{RK} , $\lambda/c_K^{n/4}$. Note that the two last combinations of parameters above replace c_K , c_R and λ . This is because, if we perform a rescaling $\phi = \tilde{\phi}/\sqrt{c_K}$, Eq. (1.2) preserves its form replacing ϕ with $\tilde{\phi}$ and f_K with f_R^m where f_R and V_{CI} take, respectively, the forms

$$f_R = 1 + r_{RK}\tilde{\phi}^{n/2} \quad \text{and} \quad V_{CI} = \lambda^2 \tilde{\phi}^n / 2^{n/2} c_K^{n/2}, \quad (3.1)$$

which, indeed, depend only on r_{RK} and $\lambda^2/c_K^{n/2}$. Imposing the restrictions of Sec. 1.2 we can delineate the allowed region of these parameters. Below we first extract some analytic expressions – see Sec. 3.1 – which assist us to interpret the exact numerical results presented in Sec. 3.2.

3.1 Analytic Results

Assuming $c_K \gg c_R$, Eq. (1.3b) yields $J \simeq \sqrt{c_K}/f_R^{(1-m)/2}$. Inserting the last one and \hat{V}_{CI} from Eq. (1.1) in Eq. (1.6) we extract the slow-roll parameters for this model as follows – cf. Eq. (1.11):

$$\hat{\epsilon} = n^2/2\phi^2 c_K f_R^{1+m} \quad \text{and} \quad \hat{\eta} = 2(1-1/n)\hat{\epsilon} - (4+n(1+m))c_R\phi^{n/2}\hat{\epsilon}/2n. \quad (3.2)$$

Given that $\phi \ll 1$ and so $f_R \simeq 1$, nMI terminates for $\phi = \phi_f$ found by the condition

$$\phi_f \simeq \max\{n/\sqrt{2c_K}, \sqrt{(n-1)n/c_K}\}, \quad (3.3)$$

in accordance with Eq. (1.6). Since $\phi_* \gg \phi_f$, from Eq. (1.5) we find

$$\hat{N}_* = \frac{c_K\phi_*^2}{2n} {}_2F_1\left(-m, 4/n; 1+4/n; -c_R\phi_*^{n/2}\right) = \begin{cases} c_K\phi_*^2/2n & \text{for } m=0, \\ (f_R^{1+m}-1)/8(1+m)r_{RK} & \text{for } n=4, \end{cases} \quad (3.4)$$

where ${}_2F_1$ is the Gauss hypergeometric function. Concentrating on the cases with $m=0$ or $n=4$, we solve Eq. (3.4) w.r.t ϕ_* with results

$$\phi_* \simeq \begin{cases} \sqrt{2n\hat{N}_*/c_K} & \text{for } m=0, \\ \sqrt{f_{m*}-1}/\sqrt{r_{RK}c_K} & \text{for } n=4, \end{cases} \quad (3.5)$$

where $f_{m*}^{1+m} = 1 + 8(m+1)r_{RK}\hat{N}_*$. In both cases there is a lower bound on c_K , above which $\phi_* < 1$ and so, our proposal can be stabilized against corrections from higher order terms – e.g., for $n=4, m=1$ and $r_{RK}=0.03$ we obtain $140 \lesssim c_K \lesssim 1.4 \cdot 10^6$ for $3.3 \cdot 10^{-4} \lesssim \lambda \lesssim 3.5$. The correlation between λ and $c_K^{n/4}$ can be found from Eq. (1.7). For $m=0$ this is given by Eq. (1.13) replacing λ with $\lambda/c_K^{n/4}$ and c_R with r_{RK} in the definition of f_{n*} . For $n=4$ we obtain

$$\lambda = 16\sqrt{3A_s}\pi c_K r_{RK}^{3/2}/(f_{m*}-1)^{3/2} f_{m*}^{(1+m)/2}. \quad (3.6)$$

As regards the inflationary observables, these are obviously given by Eqs. (1.14a) and (1.14b) for the trivial case with $m=0$. For $m \neq 0$, however, these are heavily altered. In particular, for $n=4$ we obtain

$$n_s = 1 - 8r_{RK} \frac{m-1-(m+2)f_{m*}}{(f_{m*}-1)f_{m*}^{1+m}}, \quad r = \frac{128r_{RK}}{(f_{m*}-1)f_{m*}^{1+m}}, \quad (3.7a)$$

$$a_s = \frac{64r_{RK}^2(1+m)(m+2)}{(f_{m*}-1)^2 f_{m*}^{4(1+m)}} f_{m*}^2 \left(f_{m*}^{2m} \left(\frac{1-m}{m+2} + \frac{2m-1}{m+1} f_{m*} \right) - f_{m*}^{2(1+m)} \right). \quad (3.7b)$$

The formulae above is valid only for $r_{RK} > 0$ – see Eq. (3.5) – and is simplified [1] for low m 's.

4. Conclusions

We reviewed the implementation of kinetically modified nMI in both a non-SUSY and a SUSY framework. The models are tied to the potential V_{CI} and the coupling function of the inflaton to gravity given in Eq. (1.1) and the non-canonical kinetic mixing in Eq. (1.24). This setting can be elegantly implemented in SUGRA too, employing the super- and Kähler potentials given in Eqs. (2.4) and (2.7a) – (2.7d). Prominent in this realization is the role of a shift-symmetric quadratic function F_K in Eq. (2.6) which remains invisible in the SUGRA scalar potential while dominates the canonical normalization of the inflaton. Using $m \geq 0$ and confining r_{RK} to the range $(3.3 \cdot 10^{-3} - 1)$, where the upper bound does not apply to the $n = 2$ case, we achieved observational predictions which may be tested in the near future and converge towards the “sweet” spot of the present data – especially for $n = 4$. These solutions can be attained even with subplanckian values of the inflaton requiring large c_K 's and without causing any problem with the perturbative unitarity. It is gratifying, finally, that the most promising case of our proposal with $n = 4$ can be studied analytically and rather accurately.

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References

- [1] C. Pallis, *Phys. Rev. D* **91**, 123508 (2015) [arXiv:1503.05887].
- [2] D. S. Salopek, J. R. Bond and J.M. Bardeen, *Phys. Rev. D* **40**, 1753 (1989);
F.L. Bezrukov and M. Shaposhnikov, *Phys. Lett. B* **659**, 703 (2008) [arXiv:0710.3755].
- [3] C. Pallis, *Phys. Lett. B* **692**, 287 (2010) [arXiv:1002.4765];
C. Pallis and Q. Shafi, *Phys. Rev. D* **86**, 023523 (2012) [arXiv:1204.0252].
- [4] R. Kallosh, A. Linde, and D. Roest, *Phys. Rev. Lett.* **112**, 011303 (2014) [arXiv:1310.3950].
- [5] J.L.F. Barbon and J.R. Espinosa, *Phys. Rev. D* **79**, 081302 (2009) [arXiv:0903.0355];
C.P. Burgess, H.M. Lee, and M. Trott, *JHEP* **07**, 007 (2010) [arXiv:1002.2730].
- [6] A. Kehagias, A.M. Dizgah, and A. Riotto, *Phys. Rev. D* **89**, 043527 (2014) [arXiv:1312.1155].
- [7] *Planck* Collaboration, arXiv:1502.02114.
- [8] P.A.R. Ade *et al.*, *Phys. Rev. Lett.* **114**, 101301 (2015) [arXiv:1502.00612].
- [9] M.B. Einhorn and D.R.T. Jones, *JHEP* **03**, 026 (2010) [arXiv:0912.2718];
H.M. Lee, *JCAP* **08**, 003 (2010) [arXiv:1005.2735];
S. Ferrara *et al.*, *Phys. Rev. D* **83**, 025008 (2011) [arXiv:1008.2942];
C. Pallis and N. Toumbas, *JCAP* **02**, 019 (2011) [arXiv:1101.0325].
- [10] C. Pallis, *JCAP* **10**, 058 (2014) [arXiv:1407.8522];
C. Pallis and Q. Shafi, *JCAP* **03**, 023 (2015) [arXiv:1412.3757].
- [11] G. Lazarides and C. Pallis, arXiv:1508.06682;
C. Pallis, to appear.
- [12] P. Creminelli *et al.*, arXiv:1502.01983.