Pupil Localization Algorithm based on Hough Transform and Harris Corner Detection

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In order to realize the pupil’s positioning algorithm and solve the problem of complexity in the present stage, this paper hereby puts forward a kind of accurate location of the pupil from coarse to precise algorithm. Firstly, the position of the eye is located in the position of the human eye by grayscale integral projection; secondly, the precise position of the eye pupil center is detected by using the Hough transform. Finally the corner points are detected by Harris corner detection algorithm. The proposed algorithm is proved to be simple and accurate by MATLAB.
1. Introduction

The study of the eye and its movement is the key to understand the human visual mechanism, understand the human's emotion and behavior as well as the human eyes’ movement. Eye detection and tracking is a necessary step in terms of the face recognition, facial expression recognition, eye movement analysis, iris recognition and other technologies. It involves many subjects such as image processing, computer vision, pattern recognition and so on.

In recent years, many eyes location algorithm methods are presented, in which the typical method of anthropometry based on standard[1], the detection method based on skin color model[2] and the statistical learning methods based on training data[3]. The one based on statistical learning algorithm is a hot spot in current eye detection algorithm because this kind of method is of high applicability, can have a more in-depth study in the field of artificial intelligence and pattern recognition. On the basis of the application of statistical learning algorithm for eye detection is mainly Adaboost algorithm[4] and deep learning algorithm[5], the two algorithms have exerted sound effect in the human eye measurement field; however, these algorithms are basically positioning for pupil image which is located in the center of eye pupil and accurate position cannot detect the exact rotation of the pupil. In order to locate and track the pupil accurately, this paper presents an accurate positioning algorithm:

1) Using the gray level integration algorithm to find the approximate position of the eye position in the human face.
2) Using the Hough transform to locate the precise position of the eye pupil center.
3) Using Harris corner detection algorithm to find the corner of the eye.
4) Determine the exact position of the pupil by the coordinate location of the pupil and the eye corner.

As every step of the algorithm can be realized quickly, with the traditional eye detection algorithm compared, the algorithm is simple and fast positioning.

The eye detection is based on the extracted face images, this paper uses Adaboost algorithm to extract the face images [6].

2. Rough Extraction Of Human Eye

At this stage, the human eyes’ detection method can be divided into the statistics-based method and the image processing method. The method based on statistics can also be called the processing method of pattern recognition based on learning. The main algorithm is Adaboost algorithm and learning deep neural network algorithm. The characteristics of this kind of method is the intelligent algorithm. The Adaboost algorithm has good effect on low quality images with the various positions of eyes. But the learning method based on a large number of training samples is needed, and the training process and classifier complexity in the process of human rough detection, the detection accuracy is not high; but there is a high demand in terms of the speed of detection, so this paper adopts the method based on the image processing.

2.1 Gray Level Gradient Integral Projection In Vertical Direction
As eye area in face has the maximum changes of gray level on vertical direction, using the gray integral projection can easily find out the eyes in the face vertical position of the vertical facial expression for the gray integral projection:

\[ P_y(x) = \sum_{y=1}^{W} I(x, y) \] (2.1)

\( I(x, y) \) is the gray value of the image line \( x \), column \( y \), \( W \) is the width of the image, \( P_y(x) \) is the gray integral value of the line \( x \) of the image, the curve is shown in Fig. 1 (a).

As shown in Fig. 1 (a), ordinary gray integral projection cannot accurately find the position of the human eye in the vertical direction, because it is only the simple sum of gray value, and cannot reflect the change of gray value of each line; as a result, we calculate the gradient value of each row of the image and calculate the gray gradient integral projection. The gradient value of the image is obtained by using the average value of the pixels in the image. The algorithm uses the gradient operator and the image convolution:

1) Computing \( l \), the length of scale-invariant gradient operator \( L \):

\[ l = \text{round} \left( \frac{W}{100} \right) \times 2 + 1 \] (2.2)

In the formula, \( \text{round} \) represents rounding function operator.

2) Construct the gradient scale invariant operator \( L \), where \( n \) represents the serial number of operators:

\[ L(n) = \begin{cases} 
1, & n < (l - 1)/2 \\
0, & n = (l - 1)/2 \\
-1, & n > (l - 1)/2 
\end{cases} \] (2.3)

3) Using the gradient operator to get the gradient map \( I' \), after convolution the original image \( I \):

\[ I' = L \ast I \] (2.4)

4) Computing the gray level gradient integral projection of face in vertical direction \( P'_{y|x} \):

\[ P'_{y|x} = \sum_{y=1}^{W} I'(x, y) \] (2.5)

The gray gradient integral projection curve as shown in Fig. 1(b). It can be seen that the gray gradient of eye position is significantly larger than other positions of the gradient integral value, the maximum value of the curve can be located in the vertical direction of the eye. As the eye location is an interval, it is generally believed that the width of the eye in the vertical direction of the face is 1/5. At the maximum, use the coordinate plus the length 1/10 of the face, and then cut the length 1/10 of the face. The range is the range of the eye in the face.

**Figure 1:** (a) The gray level integral projection in vertical direction (b) The gray vertical gradient integral projection in vertical direction
2.2 Gray Level Gradient Integral Projection In Horizontal Direction

In the horizontal direction, the image is extracted from the edge value of the image. There are a lot of algorithms to extract the edge value. At the present stage, there are Sobel algorithm, Prewitt algorithm, Laplacian of Gaussian Roberts algorithm, Zero-Cross algorithm and Canny algorithm. The basic idea of the algorithms is the composition operator and the image convolution and then recalculate the image gray value; finally, select the appropriate threshold to determine the image edge points; the difference lies in the different algorithm to select different convolution operators. In this thesis, use Sobel algorithm to realize the function of edge extraction. Sobel operator:

\[
S_x = \begin{pmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{pmatrix} \quad S_y = \begin{pmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{pmatrix}
\]

(2.6)

First, use the original image convolution with \( S_x \) and \( S_y \) to get horizontal and vertical gradient values of each pixel of the original image \( G_x \) and \( G_y \):

\[
G_x = S_x \ast I \quad G_y = I \ast S_y
\]

(2.7)

Then calculate the new gray value of each pixel:

\[
G = \sqrt{G_x^2 + G_y^2}
\]

(2.8)

Finally, select the appropriate threshold to decide whether the pixel is edge point. The resulting binary images are shown in Fig. 2. As the gray value of the image is much higher than that of other places, the integral projection curve of Fig. 2 can be obtained, and the left and right boundaries of the face are determined by the two peak positions of the curves. Concrete realization method:

1. Using binary image to do the integral processing on horizontal direction (add the value of each column), the integral curve as shown in Fig. 2.
2. Divide the face into two halves, find the maximum values of the right and the left side respectively, marked as \( y_1 \) and \( y_2 \).
3. Find the horizontal coordinates \( x_1 \) and \( x_2 \) which corresponding to \( y_1 \) and \( y_2 \). \( x_1 \) and \( x_2 \) are the left and right boundaries of the human face.

**Figure 2:** Point Integral Projection of Horizontal Direction

In the face of the eyes were determined by integral projection position in vertical and horizontal directions, the eye position roughly as shown in Fig. 3, for next step pupil precise localization.
3. Pupil Precise Localization

A rough image of the human eye is divided into left and right images of the left and right two images respectively, and then the obtained images are extracted by THE Sobel operator. Get results as shown in Fig. 4.

Figure 4: (a) the left edge value extraction image (b) the right edge value extraction image

From Fig. 4, the pupil edge is a regular circle, the center can be obtained by determining the pupil edge of the pupil center location. This paper uses the Hough transform to find the center of the pupil. The basic principle of Hough transform for the center: according to the mathematical expression of the circle:

\[(x-a)^2 + (y-b)^2 = r^2\]  \hspace{1cm} (3.1)

Determine the center coordinates \((a, b)\) and the radius \(r\), you can obtain the coordinates of all points \((x, y)\) on the circumference. In turn, know the point \((x, y)\) on the circumference of a circle equation can be calculated and represented by \((a, b, r)\). Find the circle equation \((a, b, r)\) which corresponds to the most points on the picture, you can find the circular center coordinates of the pupil in the picture. Specific implementation is shown as follows:

1. Establish a three-dimensional array \((A, B, R)\) to count the number of points \((x, y)\) corresponding to each circle. Where A and B is the height and width of the image, R is the smaller value of A/2 and B/2.

2. Traverse the image \((x, y)\), take each point \((x, y)\) which possible belong to the circle equation \((a, b, r)\) store in the array \((A, B, R)\).

3. Find the maximum value in the array \((A, B, R)\), \((a, b, r)\) which is corresponding to the pupil circle equation; coordinate\((a, b)\) is coordinate corresponding to the pupil center.

The final pupil center is shown in Fig. 5.

Figure 5: Location Map of the Pupil Center

4. Calculate the Pupil Coordinates
Upon finding the coordinates of the center position of the pupil, we have to find proper coordinate axis to express the pupil location coordinates. With the establishment of coordinate axis and the location of the pupil is relatively constant, this paper selects the midpoint of the inner corner of the eye corner as the origin of coordinates and the connection as \( X \) axis coordinate system. The pupil radius is unit 1 and the pupil position is mapped to the new coordinate system.

There are many corner detection methods, such as Harris corner detection algorithm, Susan algorithm and CSS(Curvature Scale Space) algorithm. This paper uses Harris algorithm to detect the position of the corner of the eye. According to the basic principle of Harris algorithm, the points can be divided into three types: the flat region, which the gray value changes of the point in the horizontal and vertical directions are not large; the edge region, the gray value changes of the point is larger at the horizontal or vertical direction; the corner, the gray value changes of the points in the horizontal direction and the vertical direction is very large. According to this method, the corner can be distinguished from of the picture. Specific implementation methods are shown as follows:

1. Select the appropriate area \( I \) as the corner of the eye to the detection area.
2. Structure the gradient operator in the horizontal direction \( H_x \) and the vertical direction of the gradient operator \( H_y \). The composition of the gradient operator can be selected from the ordinary Harris corner extraction Type (4.1) and the improved Harris corner extraction operator Type (4.2):
   \[
   H_x = [-2, -1, 0, 1, 2] \quad H_y = [-2, -1, 0, 1, 2]
   \]
   \[
   H_x = \begin{pmatrix}
   -1 & 0 & 1 \\
   -1 & 0 & 1 \\
   -1 & 0 & 1
   \end{pmatrix}, \quad H_y = \begin{pmatrix}
   -1 & -1 & -1 \\
   0 & 0 & 0 \\
   1 & 1 & 1
   \end{pmatrix}
   \]
3. Use the horizontal direction gradient operator \( H_x \) and the vertical direction gradient operator \( H_y \) convolution with the image \( I \) to get the horizontal gradient matrix \( I_x \) and the vertical gradient matrix \( I_y \):
   \[
   I_x = H_x * I, \quad I_y = H_y * I
   \]
4. Use Gaussian smoothing operator of image convolution matrix \( M \) once again:
   \[
   M = \begin{pmatrix}
   I_x^2 & I_x I_y \\
   I_x I_y & I_y^2
   \end{pmatrix}
   \]
5. According to the matrix \( M \) calculation of angle function \( R \):
   \[
   R = \text{det}(M) - k \times \text{tr}^2(M)
   \]
   Where \( k \) is the value of experience, usually 0.04–0.06, \( \text{det}(M) \) said the determinant of the matrix \( M \) and \( \text{tr}(M) \) is the trace of matrix \( M \).
6. Find the points which satisfy the two conditions as the corners: \( R \) value is greater than a predetermined threshold; \( R \) value is the maximum value of a given region.
7. In general, there are more than one points can be find. As the gray value of the corner of the eye is smaller in the region so that the coordinates of the gray value of the corner points are chosen as the coordinates of the corner points.

Finally get the corner point position as shown in Fig. 6.
**Figure 6:** Corner Point Positioning Map

By transforming the corner of the eye point coordinates to the coordinates of the pupil coordinates, finally get the pupil’s precise coordinates of the location, as shown in Fig. 7. Compared to the original picture, although the camera position relative to the face is not a horizontal position, with the coordinate transformation, the center of the pupil can be transformed to the same horizontal direction.

**Figure 7:** Pupil Precise Location Coordinates

**5. Experimental Results**

The experiments will be carried out by the the algorithm in MATLAB programming verification, the computer CPU is Intel (R) Core (TM) i7-4500U, CPU Clock Speed is 1.80GHz, RAM is 8.00GB, the operating system is 64 bits. The images uses ordinary camera to get the image and choose different pupil poses of the face of the test. The final experimental results are shown in Fig. 8. The average processing time is less than 0.3s and all tests can be accurately located.

**Figure 8:** Different Pupil Position and Corner Point Positioning Map

**6. Conclusion**

This paper presents an algorithm for locating the eye pupil by rough to precise. Accurate positioning of the pupil by using gray integral algorithm, Hough transform and Harris corner detection algorithm. On the matlab algorithm, the algorithm is proved to be simple and accurate.
After this paper, we will study the pupil tracking algorithm and use this paper to get accurate position of the pupil so as to accurate track the pupil.

At the same time in the experimental process, there may be incorrect positioning of the Hough transform to detect the pupil center when the pupils are covered by eyelid. It is necessary to solve the optimization problems in the future research.

References


