

## Associated production of gauge bosons and $D/B$ mesons at the LHCb and double parton interactions

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We study the production of weak gauge bosons in association with heavy flavored mesons at the LHCb conditions in both single (SPS) and double (DPS) parton scattering mechanisms. We find that the usual DPS factorization formula needs to be corrected for the limited partonic phase space, and that including the relevant corrections reduces discrepancies in the associated  $ZD$  production. We conclude finally that double parton scattering dominates the production of same-sign  $W^\pm D^\pm$  states, as well as the production of  $W^-$  bosons associated with  $B$ -mesons. The latter processes can thus be regarded as new useful DPS indicators.

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Recently we have shown [1] that the same-sign  $WD^{(*)}$  production in ATLAS kinematics region can be an indicative process, in which DPS contribution can dominate over single parton scattering. Our consideration was only restricted to central region because only CMS and ATLAS collaborations provided the data. However, it is interesting to expand our analysis to the forward kinematics region of LHCb, since one can expect even clearer domination of DPS contributions in that region. Also we would like to include into our consideration the processes of  $WB$  and  $ZD$  production.

Calculation of DPS contributions usually relies on some assumptions concerning the factorization of DPS distribution functions. First, it is supposed, that the DPS distribution function is factorized to transversal and longitudinal parts. Second, the latter reduces to the diagonal product of two independent single parton distribution functions:

$$D_p^{ij}(x_1, x_2; Q_1^2, Q_2^2) = D_p^i(x_1; Q_1^2) D_p^j(x_2; Q_2^2) \quad (1)$$

(here  $x_1$  and  $x_2$  are the longitudinal momentum fractions of the partons  $i$  and  $j$  entering the hard subprocesses at the probing scales  $Q_1$  and  $Q_2$ ). These approximations lead to a simple factorization formula (for details see the reviews [2] and references therein):

$$\sigma_{\text{DPS}}^{AB} = \sigma_{\text{SPS}}^A \sigma_{\text{SPS}}^B / \sigma_{\text{eff}}, \quad (2)$$

where  $\sigma_{\text{eff}}$  is a normalization constant that encodes all ‘‘DPS unknowns’’ into a single phenomenological parameter. However, this formula is valid only for small longitudinal momenta fractions, where the evident restriction on the total parton momenta  $x_1 + x_2 < 1$  can be neglected. This is not the case for the LHCb conditions, especially with respect to as heavy systems as electroweak bosons.

Setting the boundary condition in the form of theta-function  $\Theta(1-x_1-x_2)$  would result in a step-like discontinuity at the edge of the phase space. This does not seem physically consistent for the parton densities. In a more accurate approach [3–10],

$$D_p^{ij}(x_1, x_2; Q_1^2, Q_2^2) = D_p^i(x_1; Q_1^2) D_p^j(x_2; Q_2^2) (1-x_1-x_2)^n, \quad (3)$$

the kinematical constraints are smoothly put into play with the correction factor  $(1-x_1-x_2)^n$ , where  $n > 0$  is a parameter to be fixed phenomenologically. The integrand and its derivative remain continuous at the phase space border. One often chooses  $n = 2$ . This choice can be partly justified [3,5] in the framework of perturbative QCD and gives DPS distribution functions which satisfy the momentum sum rules [4] reasonably well. To feel the size of the possible effect we also tried  $n = 3$ . A numerical value of  $\sigma_{\text{eff}} \simeq 15$  mb was earlier obtained empirically from fits to  $p\bar{p}$  and  $pp$  data. This will be taken as the default value throughout the paper. As we will see, variations within some reasonable range  $\sigma_{\text{eff}} \simeq 15 \pm 5$  mb would affect our DPS predictions (with the respective errors presented in the tables), though without changing our basic conclusions.

The parameters of our numerical calculations [11] were the following. We employ the  $k_T$ -factorization approach (see, for instance, [12]) with KMR  $k_T$ -dependent parton distributions [13] for relatively light states ( $c\bar{c}$  or  $b\bar{b}$ ) and conventional collinear factorization with MSTW2008 parton densities [14] for states containing  $W$  or  $Z$  bosons. We used running strong and electroweak coupling constants normalized to  $\alpha_s(m_Z^2) = 0.118$ ;  $\alpha(m_Z^2) = 1/128$ ;  $\sin^2 \Theta_W = 0.2312$ ; the factorization and renormalization scales were chosen as  $\mu_R^2 = \mu_F^2 = m_T^2(W/Z) \equiv m_{W/Z}^2 + p_T^2(W/Z)$  for gauge

channel	data	SPS	DPS ( $n=0$ )	DPS ( $n=2$ )	DPS ( $n=3$ )
$Z^0 D^0$	2.50	0.6	$2.4 \pm 0.6$	$1.15 \pm 0.38$	$0.95 \pm 0.32$
$Z^0 D^+$	0.44	0.25	$0.95 \pm 0.32$	$0.50 \pm 0.17$	$0.40 \pm 0.13$
sum	2.94	0.85	$3.35 \pm 0.92$	$1.65 \pm 0.55$	$1.35 \pm 0.45$

**Table 1:** Comparison of the measured and predicted cross-sections (in pb) for  $Z$  bosons produced in association with open charm mesons in the fiducial region  $p_T(\mu^\pm) > 20$  GeV,  $2 < \eta(\mu^\pm) < 4.5$ ,  $2 < p_T(D) < 12$  GeV,  $2 < y(D) < 4$ . The SPS and DPS contributions are shown separately, with  $n$  indicating the power of the correction factor (3).

boson production, and  $\mu_R^2 = \mu_F^2 = m^2(c/b)$  for heavy quark pair production; the quark masses were set to  $m_c = 1.5$  GeV,  $m_b = 4.5$  GeV,  $m_t = 175$  GeV.  $c$ - and  $b$ -quarks were converted into  $D^+$  and  $B$  mesons using Peterson fragmentation function [15] with  $\varepsilon_c = 0.06$  and  $\varepsilon_b = 0.006$ , respectively, and normalized to  $f(c \rightarrow D^+) = 0.268$ ,  $f(b \rightarrow B^-) = 0.40$  and  $f(b \rightarrow \bar{B}^0) = 0.40$ . For the indirect contributions we also assumed 100% branching fraction for  $t \rightarrow bW$  and used inclusive branching fractions  $Br(\bar{B}^0 \rightarrow D^+ X) = 37\%$ ,  $Br(B^0 \rightarrow D^+ X) = 3\%$ ,  $Br(B^- \rightarrow D^+ X) = 10\%$ ,  $Br(B^+ \rightarrow D^+ X) = 2.5\%$ .

Now we turn to our numerical results [11]. First, we present our results on the charm-associated  $Z$  production [16]. For the LHCb fiducial phase space we obtain  $\sigma_{\text{incl}}(D^+) + \sigma_{\text{incl}}(D^0) = 670 \mu\text{b}$ ,  $Br^{Z \rightarrow ll} \sigma_{\text{incl}}(Z^0) = 75$  pb in excellent agreement with [17] reporting  $Br^{Z \rightarrow ll} \sigma_{\text{incl}}(Z^0) = 76$  pb.

We calculate the  $Zc\bar{c}$  production cross section at the quark level and then convert  $c$ -quarks into  $D^0$  and  $D^+$  mesons with overall probability normalised to 85% (with the rest 15% left for  $D_s$  and  $\Lambda_c$ ). We estimate the yields from the different subprocesses as

$$\sigma(u\bar{u} \rightarrow Zc\bar{c}) = 5 \text{ pb}, \quad (4)$$

$$\sigma(d\bar{d} \rightarrow Zc\bar{c}) = 2.6 \text{ pb}, \quad (5)$$

$$\sigma(gu \rightarrow Zuc\bar{c}) = 11.4 \text{ pb}, \quad (6)$$

$$\sigma(gd \rightarrow Zdc\bar{c}) = 5.2 \text{ pb}, \quad (7)$$

$$\sigma(gg \rightarrow Zc\bar{c}) = 2.5 \text{ pb}. \quad (8)$$

Summing up and multiplying by the quark fragmentation probability and by the  $Z \rightarrow \mu^+ \mu^-$  branching fraction we arrive at  $\sigma^{\text{SPS}}(ZD^0, ZD^+) = 0.85$  pb. This result is consistent with theoretical calculation presented in [16] under the name of ‘MCFM massive’. Adding the DPS contribution in the form (2) gives  $\sigma^{\text{SPS}+\text{DPS}}(ZD^0, ZD^+) = 4.2$  pb, that significantly exceeds the data. After applying the correction factor (3) the agreement becomes rather satisfactory (see Table 1).

The next considered process is the associated production of  $W$  bosons and  $D$  mesons. The production of opposite-sign  $W^\pm D^\mp$  states is dominated by the quark-gluon scattering at  $\mathcal{O}(\alpha_s \alpha)$ . Among the variety of processes contributing to both opposite-sign and same-sign  $WD$  states, the most important ones are the quark-antiquark annihilation at  $\mathcal{O}(\alpha_s^2 \alpha)$  and quark-gluon scattering at  $\mathcal{O}(\alpha_s^3 \alpha)$  (all the processes are listed in Table 2). In addition to that, there present indirect contributions from the production of top-quark pairs  $g + g \rightarrow t + \bar{t}$  and  $q + \bar{q} \rightarrow t + \bar{t}$  followed by a long chain of decays:  $t \rightarrow W^+ b$ ,  $W^+ \rightarrow c\bar{s}$ ,  $b \rightarrow cX$  or  $b \rightarrow c\bar{c}s$  (and the charge conjugated modes). All other possible processes are suppressed by extra powers of coupling constants or by

Double parton scattering contributions				
subprocess	$W^+D^+$	$W^+D^-$	$W^-D^-$	$W^-D^+$
$gg \rightarrow c\bar{c}, u\bar{d} \rightarrow W^+$	$12.3 \pm 4.1$	$12.3 \pm 4.1$	–	–
$gg \rightarrow c\bar{c}, d\bar{u} \rightarrow W^-$	–	–	$8.9 \pm 3.0$	$8.9 \pm 3.0$
Single parton scattering contributions				
subprocess	$W^+D^+$	$W^+D^-$	$W^-D^-$	$W^-D^+$
$g\bar{s}, g\bar{d} \rightarrow W\bar{c}$	–	1.7	–	–
$gs, gd \rightarrow Wc$	–	–	–	2.0
$u\bar{d} \rightarrow Wc\bar{c}$	0.8	0.8	–	–
$d\bar{u} \rightarrow Wc\bar{c}$	–	–	0.4	0.4
$gu \rightarrow Wdc\bar{c}$	1.9	1.9	–	–
$g\bar{d} \rightarrow W\bar{u}c\bar{c}$	0.16	0.16	–	–
$gd \rightarrow Wuc\bar{c}$	–	–	0.8	0.8
$g\bar{u} \rightarrow W\bar{d}c\bar{c}$	–	–	0.14	0.14
$gg \rightarrow t\bar{t} \rightarrow \text{decays}$	0.01	0.01	0.01	0.01
$q\bar{q} \rightarrow t\bar{t} \rightarrow \text{decays}$	0.015	0.02	0.015	0.02

**Table 2:** Predicted  $WD$  production cross sections times the  $W \rightarrow lv$  branching (in pb) integrated over the fiducial region  $p_T(l) > 20$  GeV,  $2 < \eta(l) < 4.5$ ,  $2 < p_T(D) < 12$  GeV,  $2 < \eta(D) < 4$ .

Kobayashi-Maskawa mixing matrix. Subprocesses  $q\bar{q} \rightarrow W^-c\bar{s}$  and  $q\bar{q} \rightarrow W^+s\bar{c}$ , though formally of the same order as  $q\bar{q} \rightarrow Wc\bar{c}$ , are heavily suppressed by the gluon propagator having virtuality of order  $m_W^2$  rather than  $m_{cc}^2$ .

The individual inclusive SPS cross sections  $\sigma(D^\pm)$  and  $\sigma(W^\pm)$  for the LHCb fiducial phase space are  $\sigma_{\text{incl}}(D^\pm) = 190 \mu\text{b}$ ,  $Br^{W \rightarrow lv} \sigma_{\text{incl}}(W^+) = 970$  pb and  $Br^{W \rightarrow lv} \sigma_{\text{incl}}(W^-) = 680$  pb, which is in good agreement with [16] and [18], respectively. Our results for SPS and DPS channels are displayed in Table 2. All DPS contributions are presented there without phase space corrections; they have to be multiplied by a correction factor of 0.48 for  $n = 2$  or 0.38 for  $n = 3$ .

The indirect contributions can be suppressed in experimental analyses using the property that the secondary  $b$ -decay vertex is displaced with respect to the primary interaction vertex. Summing the direct contributions up, we see that the predicted same-sign  $WD$  production rates with and without DPS channels differ by a significant factor. So the forthcoming LHCb data can give conclusive evidence for DPS.

Finally, we present our results on  $WB$  associated production. In contrast with the  $WD$  production, the contribution, analogous to the process  $qg \rightarrow Wc$ , is absent, and the feed-down from top-quark decays now should be regarded as direct contribution. The full list of processes included in the present analysis is presented in Table 3.

With the parameter setting described above, we estimate the inclusive production of  $b$  quarks in the LHCb domain as  $\sigma_{\text{incl}}(b) = \sigma_{\text{incl}}(\bar{b}) = 95 \mu\text{b}$ . Combining this result with results for  $W$ -production we obtain the DPS cross section for  $Wb$ . Table 3 represents our predictions for unconstrained phase space of Eq. (2); they have to be corrected by a factor of 0.45 for  $n = 2$  or 0.36 for  $n = 3$ .

Double parton scattering contributions				
subprocess	$W^+B^+$	$W^+B^-$	$W^-B^-$	$W^-B^+$
$gg \rightarrow b\bar{b}, u\bar{d} \rightarrow W^+$	$5.5 \pm 1.8$	$5.5 \pm 1.8$	–	–
$gg \rightarrow b\bar{b}, d\bar{u} \rightarrow W^-$	–	–	$4.0 \pm 1.3$	$4.0 \pm 1.3$
Single parton scattering contributions				
subprocess	$W^+B^+$	$W^+B^-$	$W^-B^-$	$W^-B^+$
$u\bar{d} \rightarrow Wb\bar{b}$	1.2	1.2	–	–
$d\bar{u} \rightarrow Wb\bar{b}$	–	–	0.5	0.5
$gu \rightarrow Wdb\bar{b}$	2.7	2.7	–	–
$g\bar{d} \rightarrow W\bar{u}b\bar{b}$	0.22	0.22	–	–
$gd \rightarrow Wub\bar{b}$	–	–	1.1	1.1
$g\bar{u} \rightarrow W\bar{d}b\bar{b}$	–	–	0.2	0.2
$gg \rightarrow t\bar{t} \rightarrow WWb\bar{b}$	0.030	0.045	0.030	0.045
$q\bar{q} \rightarrow t\bar{t} \rightarrow WWb\bar{b}$	0.055	0.060	0.055	0.060
$u\bar{d} \rightarrow t\bar{b} \rightarrow Wb\bar{b}$	0.0018	0.0042	0.0018	0.0042
$d\bar{u} \rightarrow b\bar{t} \rightarrow W\bar{b}b$	0.0002	0.0005	0.0002	0.0005

**Table 3:** Predicted  $WB$  production cross sections times the  $W \rightarrow l\nu$  branching (in pb) integrated over the fiducial region  $p_T(l) > 20$  GeV,  $2 < \eta(l) < 4.5$ ,  $2 < \eta(B) < 4.5$ . Here  $B^+$  and  $B^-$  denote the sum of  $B^+$  and  $B^0$  and the sum of  $B^-$  and  $\bar{B}^0$  mesons, respectively.

In conclusion, the correction factor  $(1 - x_1 - x_2)^n$ , allowing to take into account effects of the limited partonic phase space, gives significant suppression (to a factor of 2) of the  $W/Z + D/B$  DPS production cross section; the production of same-sign  $W^\pm D^\pm$  states in the forward region is dominated by the DPS mechanism, so this process can be recommended as a DPS indicator; LHCb kinematics opens doors for a still new indicative process, which is the beauty-associated production of gauge bosons  $W$ .

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