Analyses of LHCb data from Run I of the LHC have led to a range of new results relating to spectroscopy including the following: the first observation of the decay $D_{s2}^+(2573)\rightarrow D^\pm K^0_s$ and a measurement of its branching fraction; a Dalitz plot model of $D^0 \rightarrow K^0_S K^\pm \pi^\mp$ decays; the discovery of pentaquarks in $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays and a model-independent confirmation; and an upper limit on the production of the claimed $X(5568)^\pm$ tetraquark within the LHCb acceptance.
1. $D_s^+$ spectroscopy

Heavy meson spectroscopy provides essential tests used to refine models of quantum chromodynamics. Recently, such tests have been provided by studies of the $D_{s1}^+(2700)^+, D_{s1}^+(2860)^+$, $D_{s3}^+(2860)^+$ and $D_{sJ}^+(3040)^+$ mesons [1, 2, 3, 4, 5, 6]. The former three may be interpreted as the natural spin-parity (i.e. $J^P = 0^+, 1^+, 2^+, \ldots$) 2S and 1D states of the $D_s^+$ system while the latter has unnatural spin-parity (i.e. $J^P = 0^-, 1^+, 2^-, \ldots$). No mesons that are consistent with being the three unnatural states in the 2S and 1D levels have yet been observed. Candidates for these states should decay to the $D^+K^0$ final state.

An inclusive study of $pp \to D^{*\pm}K^0_sX$ and $D^{*0}K^{\pm}X$ decays was performed at LHCb [7]. $D^{*\pm}$ candidates were reconstructed from the decay chains $D^{*\pm} \to D^0\pi^\pm$, $D^0 \to K^-\pi^+$, $K^-\pi^+\pi^+\pi^-$, and $D^{*0}$ candidates were reconstructed from the decay chain $D^{*0} \to D^0\pi^0$, $D^0 \to K^-\pi^+$. Fits to the $D^{*\pm}K^0_s$, $D^{*0}K^0_s$, $D^{*\pm} \to D^0\pi^\pm$, $D^0 \to K^-\pi^+$ dataset are shown in Fig. 1, where candidates have been partitioned into two subsets that enhance the natural (NP) and unnatural (UP) contributions, respectively. Clear contributions are seen corresponding to the $D_{s1}^+(2536)^+, D_{s2}^+(2573)^+, D_{s1}^+(2700)^+$ and $D_{s3}^+(2860)^+$ resonances, and some evidence is seen for the $D_{sJ}^+(3040)^+$ state with a significance of 2.4$\sigma$. This was the first observation of the decay $D_{s2}^+(2573)^+ \to D^{*+}K^0_s$ and the relative branching fraction was measured to be

$$\frac{\mathcal{B}(D_{s2}^+(2573)^+ \to D^{*+}K^0_s)}{\mathcal{B}(D_{s3}^+(2573)^+ \to D^{*+}K^0_s)} = 0.044 \pm 0.005 \text{ (stat.)} \pm 0.011 \text{ (syst.)}.$$  

The helicity angle $\theta_H$, defined as the angle between the $K^0_s$ meson and the pion from the $D^{*\pm}$ decay in the rest frame of the $D^{*\pm}K^0_s$ system, yields information on the spin-parity of each resonance. Specifically, the angular distribution is expected to follow a $\sin^2 \theta_H$ distribution for an NP (UP) resonance. Fig. 2 shows the $\theta_H$ distributions in the regions of the $D_{s1}^+(2700)^+$, $D_{s3}^+(2860)^+$ and $D_{sJ}^+(3040)^+$ resonances which are consistent with previous spin-parity assignments. The distribution in the $D_{s3}^+(2860)^+$ region is also consistent with a small UP contribution in this region.

**Figure 1:** Distributions of the $D^{*+}K^0_s$ invariant mass for the $D^0 \to K^-\pi^+$ sample with (a) $|\cos \theta_H| < 0.5$ and (b) $> 0.5$. These requirements enhance NP and UP contributions, respectively. The solid red line describes the full fitting function, the dashed line shows the background, and the dotted lines show individual resonant contributions. The insets show the same mass distributions with the backgrounds subtracted.
2. Dalitz plot analysis of $D^0 \to K_S^0 K^\pm \pi^\mp$ decays

A Dalitz plot analysis of $D^0$ and $\bar{D}^0$ decays to the $K_S^0 K^\pm \pi^\mp$ final states can be used to study the resonant structure and CP violation present in these decays. CP violation as a function of position in phase space is an important input to measurements of the CKM angle $\gamma$, while the resonant structure provides a probe of light-flavour meson spectroscopy. An analysis of these decays was performed at LHCb using the charge of the slow pion from the decay $D^{\pm} \to D^0 \pi_\text{slow}$ to tag the initial flavour of the decaying meson. The amplitude model describing each Dalitz plot is constructed using the isobar formalism

$$\mathcal{M}_{K^0_S K^\pm \pi^\mp}(m_{K^0_S K^\pm \pi^\mp}) = \sum_R a_{R\theta} \mathcal{M}_R(m_{K^0_S K^\pm \pi^\mp})$$

where $\mathcal{M}_R$ describes the resonant or nonresonant contribution, $R$, and $a_{R\theta}$ is a complex coefficient determined from the fit. Projections of the fits to both Dalitz plots are shown in Fig. 3. The model significantly favours the inclusion of percent-level contributions from the $\rho(1450)^\pm$ and $\rho(1700)^\pm$ resonances, which were previously observed in Ref [9] but are not well established.

Figure 2: Distributions of the helicity angle, $\theta_H$, for data in the (a) $D^{*+}_{s3}(2700)^+$, (b) $D^{*+}_{s3}(2860)^+$ and (c) $D_{sJ}(3040)^+$ regions with backgrounds subtracted. The angular fit to each distribution is shown as a solid red line.

Figure 3: Invariant mass projections of the (top) $K_S^0 K^- \pi^+$ and (bottom) $K_S^0 K^+ \pi^-$ Dalitz plots: (left) $m(K_S^0 K^-)$, (centre) $m(K_S^0 \pi^+)$ and (right) $m(K^+ \pi^-)$. The fit components are as described in the legends.
The fit results are consistent with CP conservation, with a p-value of 0.54. The branching ratio was measured across the full phase space and also in the region of the $K^*(892)^\pm$ resonance
\[
\frac{\mathcal{B}(D^0 \to K^0_s K^+ \pi^-)}{\mathcal{B}(D^0 \to K^0_s K^- \pi^+)} = 0.655 \pm 0.004 \text{(stat.)} \pm 0.006 \text{(syst.)},
\]
\[
\frac{\mathcal{B}(D^0 \to K^0_s K^-)}{\mathcal{B}(D^0 \to K^0_s K^+)} = 0.370 \pm 0.003 \text{(stat.)} \pm 0.012 \text{(syst.)},
\]
and the corresponding coherence factors are measured to be
\[
R_{K^0_s K \pi} = 0.573 \pm 0.007 \pm 0.019, \quad R_{K^- K} = 0.831 \pm 0.004 \pm 0.010.
\]

3. Pentaquark contributions in $\Lambda_b^0 \to J/\psi pK^-$ decays

An LHCb study of $\Lambda_b^0 \to J/\psi pK^-$ decays led to the first observation of two new resonant states, labelled $P_c(4450)^+$ and $P_c(4380)^+$, which decay to the $J/\psi p$ final state and are consistent with being pentaquarks. Using a 6D amplitude analysis, both pentaquarks were found to be necessary to successfully fit the data with significances in excess of 9$\sigma$ [10]. In addition to these exotic contributions, the three-body decay involves many contributions from resonances in $m(pK^-)$. As the spectrum of these $pK^-$ states is poorly understood (see Fig. 4(a)), a 2D model-independent study has now been performed to test the hypothesis that structures in the $pK^-$ system could fake the observed pentaquark signals [11]. The analysis is performed in bins in $m(pK^-)$ with the angular distribution in each bin described by a sum of Legendre polynomials,
\[
dN/d\cos \theta_{\Lambda^*} = \sum_{l=0}^{l_{\text{max}}} \langle P_l^U \rangle P_l(\cos \theta_{\Lambda^*}),
\]
where $N$ is the efficiency-corrected and background-subtracted yield, $\theta_{\Lambda^*}$ is the angle between the proton and the $J/\psi$ meson in the rest frame of the $pK^-$ system, $P_l$ is the $l$th Legendre polynomial, $l_{\text{max}}$ is the highest-order term used in the summation and $\langle P_l^U \rangle$ is the Legendre moment of rank $l$,
\[
\langle P_l^U \rangle = \int_{-1}^{+1} d\cos \theta_{\Lambda^*} \, P_l(\cos \theta_{\Lambda^*}) \, dN/d\cos \theta_{\Lambda^*}.
\]

As a resonance of spin $J$ in the $pK^-$ system may only contribute to moments up to $2J$ then, in the absence of exotic states, the angular distribution should remain well described when the sum over $l$ is truncated. Conversely, exotic contributions in either the $J/\psi p$ or $J/\psi K^-$ system would introduce non-zero contributions to higher moments. The moments expected within each mass bin, and hence the values of $l_{\text{max}}$, were determined based on theoretical predictions and observed resonances as shown in Fig. 4(a).

To test for exotic contributions, a likelihood ratio is constructed between a null hypothesis in which only contributions up to $l_{\text{max}}$ were included and an alternative hypothesis with higher moments also included. As shown in Fig. 4(b), the likelihood ratio determined from data is significantly separated from the value determined from simulated data containing only $pK^-$ contributions and consistent with the value from simulated data containing two pentaquark resonances. The $m(J/\psi p)$ distribution of data is shown in Fig. 4(c) with the results from both hypotheses superimposed.
4. $B_s^0\pi^\pm$ spectroscopy

The D0 collaboration has recently announced evidence for a new tetraquark, labelled $X(5568)^\pm$, decaying to the $B_s^0\pi^\pm$ final state [12]. Within the D0 acceptance, the production rate of this state was measured relative to the total $B_s^0$ production rate to be $\rho_s^{D0} = (8.6 \pm 1.9 \pm 1.4) \%$. An LHCb study was performed to search for this state and measure its production within the LHCb acceptance [13]. Large clean samples of $B_s^0$ candidates were reconstructed from the $J/\psi \phi$ and $D_{sJ}^- \pi^+$ final states and combined with pion candidates. Fig. 5 shows the distribution of $m(B_s^0\pi^\pm)$ compared to the signal that would be expected for $\rho_s^{LHCb} = 8.6 \%$. The study found no evidence for the claimed state. Within the LHCb acceptance, limits are set on the production rate of 0.9 % (1.0 %) at the 90 % (95 %) confidence level for $B_s^0$ mesons with $p_T > 5\, GeV/c$ and 1.6 % (1.8 %) for mesons with $p_T > 10\, GeV/c$.

![Figure 4](image1.png)

**Figure 4:** (a) Masses of (green) measured and (black) predicted $\Lambda^*$ states. The red line shows $l_{\text{max}}$ as a function of mass and the blue lines show the kinematic limits of $m(pK^-)$ in the three-body decay. (b) The difference in log likelihood determined from (red hatched) model-independent pseudoexperiments and (as labelled) various amplitude models. (c) The distribution of data in $m(J/\psi p)$ with the results from (blue) the null hypothesis and (black dashed) the alternative hypothesis superimposed.

![Figure 5](image2.png)

**Figure 5:** Distribution of $m(B_s^0\pi^\pm)$ with $p_T(B_s^0) > 10\, GeV/c$. A hypothetical signal component corresponding to $\rho_s^{LHCb} = 8.6 \%$ is superimposed.

5. Summary

Analyses of LHCb data from Run I of the LHC continue to produce new meson spectroscopy results and drive the search for new exotic states [14, 15, 16]. With Run II of the LHC ongoing, more exciting results are expected over the next few years.
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References


