Modeling GeV to very high energy emission from long GRBs

Jagdish C. Joshi∗
University of Johannesburg
E-mail: jjagdish@uj.ac.za

Soebur Razzaque
University of Johannesburg
E-mail: srazzaque@uj.ac.za

Gamma-ray bursts (GRBs) are energetic, transient explosions, which indicate either the death of a massive star ($\geq 25M_\odot$) or the merger of two compact object. In the current understanding, collapsar based GRBs stay active for a long duration ($T_{90} > 2s$), and merger based GRBs last for a very short duration ($T_{90} < 2s$), $T_{90}$ is the time over which gamma-ray burst emits 90 % of its total measured fluence. A clear understanding of GRB emission can reveal the nature of the central source and the composition of the relativistic jet. Fermi-LAT observations of GRBs have detected a significant power-law component in the energy range MeV to tens of GeV, in short as well as in long GRBs. The explanation of its origin is still not understood. In this work we have discussed a plausible origin of this component, in the case for long GRBs.

4th Annual Conference on High Energy Astrophysics in Southern Africa
25-27 August, 2016
Cape Town, South Africa

∗Speaker.
1. Introduction

The emission from a GRB in the early time, for the first tens of seconds, is known as ‘Prompt-emission’ while the late emission, which remains active after the prompt emission is known as ‘Afterglow emission’. The prompt emission dominates in the gamma-rays (keV-MeV-GeV), while the afterglow emission mainly occurs in X-ray, UV, optical, infrared, radio wavelengths and possibly in gamma-rays. The study of prompt and afterglow emission in GRBs reveals the nature of the central source and the composition of the relativistic jet [1, 2]. These explosions can be detected in thermal as well as in non-thermal radiation.

The non-thermal emission from GRBs, which is dominant in MeV energy, can be modelled using the band function [3] and in some cases with an addition of Planck type thermal component [4, 5]. A hard non-thermal, power-law component appears in GeV energy band [6] in some of the GRBs.

One of the most famous model for explaining the observations of GRBs is the Fireball model. This model was developed by Paczynski [7], Goodman [8], Shemi and Piran [9], Rees and Meszaros [10–12]. The radiation dominated outflow from GRBs leads to a relativistic flow due to radiation pressure. In the expansion stage, the physical processes in GRBs results in a mixed composition, (electron, positron, protons and heavy nuclei). In the case of long GRBs the jet composition may also include heavy nuclei which are absent in the case of short gamma-ray bursts.

In this work, we have investigated the case of three long GRBs namely GRB090902B (redshift z=1.82 [13]), GRB090926A (redshift z=2.11 [14]) and GRB 130427A (redshift z=0.34 [6]), in which a power-law component has a photon distribution been observed by Fermi-LAT observations. In case of GRB130427A the power-law has a cutoff- at 70 GeV, while for GRB090902B at 11.16 GeV and for GRB090926A it occurs at 1.4 GeV. The case of GRB 130427A has also been discussed in [15] using the photo-disintegration model [16–19].

2. Models of gamma-ray production in GRBs

The emission of gamma-rays from GRBs can originate from thermal as well as non-thermal processes. In this section we have discussed these processes in detail.

2.1 Photospheric models

The injection of huge luminosities from GRBs led to early theoretical investigations of thermal emission, where the emission dominated in hard X-rays up to gamma-rays [20, 21]. The physical scenario can be mapped to the fireball model [20–24], where the production of thermal energy in the jet occurs via the dissipation of particle and magnetic energy, between the explosion centre and the photosphere. The photospheric emission [25], has been used to account for the X-ray emission observed in BATSE [26] bursts. In some of the GRBs the prompt [4] and afterglow emission [27] has been modelled by considering the thermalization processes at the source. In particular the photospheric emission efficiency can dominate in the long GRBs [28].

If the central source injects the radiation at a radius \( r_0 \) of \( 10^7 \) cm, with a luminosity \( L \sim 10^{52} \text{erg s}^{-1} \), then the temperature of the source, if it is in thermal equilibrium can be calcu-
lated by the relation $L = 4\pi r_0^2 \sigma T^4$, where $\sigma$ is the Stefan-Boltzmann constant with a value $5.67 \times 10^{-5}\text{erg cm}^{-2}\text{s}^{-1}\text{K}^{-4}$. The thermal emission for the above parameters will peak at 1.7 MeV.

### 2.2 Lepto-hadronic models

The relativistic emission from the GRB fireball leads to the formation of GRB jets. The injected total energy into the GRB jet is distributed into magnetic, leptonic (electrons and positrons) and hadronic (protons and heavy nuclei) components. This distribution of energy leads to a broad, multi-wavelength spectrum that is detected at earth. In general the spectrum at earth, with normalization $A$, maximum flux at break energy $E_0$, energy spectrum index before $E_0$, $\alpha$, and after $E_0$, $\beta$, can be fitted empirically by the band function

$$n(E) = \begin{cases} A\left(\frac{E}{100\text{ keV}}\right)^\alpha \exp\left(-\frac{E}{E_0}\right), & (\alpha - \beta)E_0 \geq E, \\ A\left(\frac{E}{100\text{ keV}}\right)^{\alpha - \beta} \exp\left(\beta - \alpha\right)\left(\frac{E}{100\text{ keV}}\right)^\beta, & (\alpha - \beta)E_0 < E \end{cases}$$

In general the spectral index distribution varies as, $-1.5 < \alpha < 0$, $\beta_{av} \simeq -2$, while the peak energy can have a range of keV to MeV with an average around $\simeq 200$ keV [30]. The band function in general can be used to model the MeV non-thermal radiation, which is believed to be produced by the synchrotron emission of relativistic electrons. The explanation of prompt emission due to leptonic synchrotron process has been considered in the literature [30, 31]. In this process the relativistic electrons cool very fast by emitting radiation in the jet magnetic field, so that most of their energy can be channeled to the emitted radiation [32].

Hadronic models for GRBs are mainly used if the observed spectrum from GRBs has more components than the usual band spectrum and the inverse Compton emission cannot explain this deviation at higher energy [33]. In case of GRB 080916C, 100 MeV-GeV emission can be explained by the proton synchrotron model [34] and the MeV to 100 GeV radiation from GRB 130427A can be explained by the photo-disintegration of heavy nuclei due to the low energy photons available in the jet of GRB [15].

### 3. Photo-disintegration of Heavy nuclei in long GRBs

In this process, an energetic nuclei, in the frame of GRB jets interact with the isotropic radiation field. During the interaction of the heavy nuclei with the radiation field, the heavy nuclei excites to a higher energy state. The de-excitation produces daughter nuclei, secondary nucleons (protons/neutrons) and gamma-ray photons, as shown in equation (3.1),

$$A + \gamma \rightarrow A^* \rightarrow (A - 1) + \gamma + n/p$$

We follow the same notation for our calculation as discussed in [15]. The notation for the frame of references are, (i) The comoving GRB jet frame or wind rest frame is denoted with superscript ‘$\prime$’, (ii) the lab frame or GRB source frame is denoted with superscript ‘$\ast$’, (iii) the rest-frame of the nuclei is denoted with superscript ‘$\prime\prime$’, and (iv) the observer frame with no superscript. The energies in the observer frame, lab frame and comoving jet frame are related by the Lorentz boost factor $\Gamma$ of the bulk GRB outflow and redshift $z$ by the relation $E_\gamma = E_{\gamma\prime}/(1+z) = \Gamma E_{\gamma\ast}/(1+z)$. 

2

---

**High energy emission from long GRBs**

Jagdish C. Joshi
The acceleration of atomic nuclei ($Z$), in the magnetic field of the GRB can be calculated using [35],

$$t'_{\text{acc}} = \eta \frac{2\pi E'_A}{ZeB'c}$$

$$\approx 2 \times 10^{-5} \left( \frac{\eta}{10} \right) \left( \frac{Z}{26} \right)^{-1} \left( \frac{B'}{27.2 \text{ kG}} \right)^{-1} \left( \frac{E'_A}{\text{TeV}} \right)^s$$  \hspace{1cm} (3.2)

where $E'_A$ is the energy of the cosmic ray nuclei and $\eta = 10$ is a fiducial value for the number of gyroradius required for acceleration. During the acceleration process, due to their charge heavy nuclei will cool down due to synchrotron radiation [35],

$$t'_{\text{syn}} = \frac{6\pi m_p \gamma^3}{\sigma_T m_e^2 E'_A B'_2} \left( \frac{A}{Z} \right)^4$$

$$= 5.7 \times 10^6 \left( \frac{B'}{130 \text{ kG}} \right)^{-2} \left( \frac{E'_A}{\text{TeV}} \right)^{-1} \left( \frac{A}{56} \right)^4 \left( \frac{Z}{26} \right)^{-4} \text{s}$$  \hspace{1cm} (3.3)

This is too long to be significant in the energy range we are interested. The dynamic timescale of the jet flow at the internal shock, with dissipation radius $R_{in}$ is calculated using,

$$t'_{\text{dyn}} = \frac{R_{in}}{\gamma c} = 0.7 \left( \frac{R_{in}}{2 \times 10^{13} \text{ cm}} \right) \left( \frac{\Gamma}{10^3} \right)^{-1} \text{s}$$  \hspace{1cm} (3.4)

The interaction of heavy nuclei with low energy photons in the GRB jet can be estimated using the observed differential photon flux at earth, $f_\gamma(e)$ in units of $(\text{MeV}^{-1}\text{s}^{-1}\text{cm}^{-2})$ [36],

$$n'_\gamma(e') = \frac{2d_L^2}{R_{in}^2 c f_\gamma} \left( \frac{\Gamma e'}{1+z} \right)$$  \hspace{1cm} (3.5)

where $R_{in}$ is the internal shock radius and $d_L$ is the luminosity distance to the source and $n'_\gamma(e')$ is the photon density in the comoving frame. The photo-disintegration time scale of heavy nuclei, calculated using the photon density in the jet frame as defined in 3.5, is given by,

$$t^{-1}_A(\gamma'_A) = \frac{c}{2\gamma'_A} \int_{\epsilon''_A}^\infty \epsilon''_A \sigma_A(\epsilon''_A) d\epsilon''_A \int_{\epsilon''_A/2\gamma'_A}^\infty \frac{n'_\gamma(e')}{e'^2} d\epsilon'$$  \hspace{1cm} (3.6)

Here $\gamma'_A = E'_A/m_Ac^2$ is the boost factor of the energetic nuclei, $\epsilon''_A = \gamma'_A \epsilon'(1-\beta_A \cos \theta)$ is the photon energy in the rest frame of the nuclei with an angle $\theta$ between their velocity vectors, $\epsilon''_A$ is the threshold photon energy for the nuclei excitation and $\sigma_A(\epsilon''_A)$ is the photo-disintegration cross-section and for a relativistic nuclei with speed $u$, $\beta = \frac{u}{c}$. For more details, see [15]. We calculated the time scales for Iron and Oxygen nuclei for GRB130427A, GRB090926A, GRB090902B as shown in figure 1, 2, 3 respectively. The $p-\gamma$ interaction time scale can be calculated using the above formula using a mass number A=1 and corresponding interaction cross-section values. All these plots indicate the efficiency of photo-disintegration of heavy nuclei in the jet of these GRBs.
4. GeV gamma-ray flux at earth

The photo-disintegrated gamma-ray flux at earth can be calculated using the formalism given in [15]. In this formalism, heavy nuclei are disintegrated by low energy target photons. The emitted photons have a energy of approximately 1 MeV in the rest frame of nuclei, and further their energy is boosted by the Lorentz factor $\Gamma$ of the GRB jet. These photons will escape the fireball from the optically thin regions. We have followed the same formalism with similar notations. The observed gamma-ray flux at earth for GRB130427A, GRB090926A, GRB090902B are shown in figures 4, 5, 6 respectively, with an effective attenuation due to optical depth effects.
The Fe- nuclei luminosity to explain these gamma-ray fluxes at earth for GRB 130427A is approximately $10^{53} \text{ erg s}^{-1}$, this is very similar to the luminosity available in the radiation field for this GRB. In the case of GRB090926A and GRB090902B the required luminosity budget is approximately $10^{55} \text{ erg s}^{-1}$, and this is 100 times higher than the radiation field luminosity budget for these GRBs. The luminosity requirement favours the photo-disintegration model for GRB130427A, but other emission mechanism may be in place for the other two GRBs discussed here.

5. Summary and Conclusion

The observation of GeV gamma-rays from long GRB is very important to understand the dynamics of heavy nuclei composition in GRB jets, if present, in particular because they can produce the power-law component observed in case of long GRBs discussed above. In the case of GRB 130427A, photo-disintegration model can explain the origin of this power-law component with a plausible luminosity budget for this source. We tried the same physical scenario for GRB090926A and GRB090902B and found that only a small portion of the power-law component can be reproduced using photo-disintegration model, but it demands a challenging energy budget.

References


High energy emission from long GRBs

Jagdish C. Joshi


