

CPV in beauty decays with LHCb

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During 2011 and 2012, pp collision data corresponding to integrated luminosities of 1 fb^{-1} at a centre-of-mass energy of 7 TeV and 2 fb^{-1} at 8 TeV have been collected with the LHCb detector. This dataset has allowed LHCb to measure with unprecedented precision observables relating to the CKM unitary triangles. In these proceedings I describe measurements sensitive to γ , the least well constrained unitary triangle angle.

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1. Introduction

In the Standard Model of particle physics (SM) the weak force is maximally violating CP conservation. A single irreducible phase in the Cabibbo-Kobayashi-Maskawa (CKM) matrix [1, 2] describes CP violation in the quark-mixing sector. The unitary CKM matrix relates the mass eigenstates with the eigenstates to the weak force of the three generations of down-type quarks. Its unitarity results in certain conditions, which can be expressed as closed triangles in the complex plane. The triangle that is usually referred to as the CKM triangle fulfils the condition

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0.$$

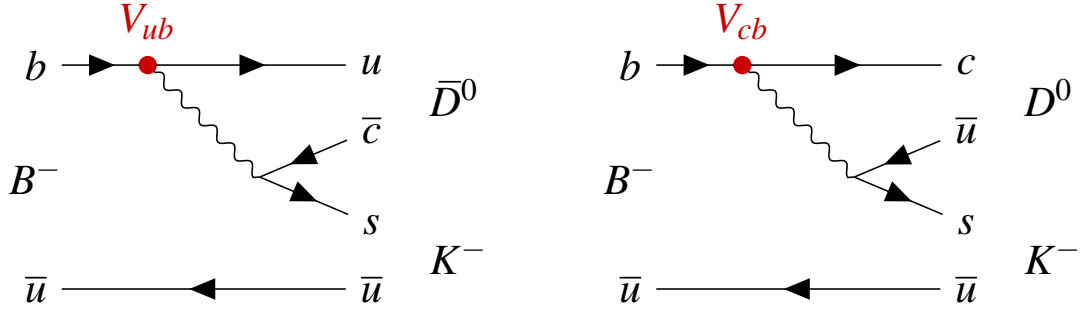
Precision measurements of the side lengths and angles of this triangle provide insight into the nature of CP violation. The least well known angle is $\gamma \equiv \arg[-(V_{ud}V_{ub}^*)/(V_{cd}V_{cb}^*)]$. This angle is unique in that it can be determined from tree-level only processes. Comparisons between direct measurements of γ and constraints coming from global fits, which include loop diagrams as well, offer a good opportunity to test the SM. To achieve this goal it is mandatory to improve the precision on tree-level measurements of γ . I present here recent measurements of γ using the full Run I data sample corresponding to an integrated luminosity of 3 fb^{-1} of pp collisions.

2. LHCb detector

The LHCb detector [3, 4] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b - or c -quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the pp interaction region, a large-area silicon-strip detector located upstream of a dipole magnet, and three stations of silicon-strip detectors and straw drift tubes placed downstream of the magnet. Depending on the detector response two different type of $K_S^0 \rightarrow \pi^+\pi^-$ decays are considered: the first involving K_S^0 mesons that decay early enough for the daughter pions to be reconstructed in the vertex detector; and the second consisting of K_S^0 candidates that decay later such that track segments of the pions cannot be formed in the vertex detector. These categories are referred to as *long* and *downstream*, respectively. The long category has better mass, momentum and vertex resolution than the downstream category. Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors. Photon, electron, and hadron candidates are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter, and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers. The online event selection system (trigger) [5] consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage.

3. Concept of tree-level γ measurements

It is possible to measure γ relying only on tree-level Feynman diagrams. This is based on the interference between $b \rightarrow c$ and $b \rightarrow u$ transitions, of which one such process is the decay $B^\pm \rightarrow DK^\pm$. As can be seen in Fig. 1, the daughter D meson can be both a D^0 and a \bar{D}^0 meson.

Figure 1: Feynman diagrams for $B^\pm \rightarrow DK^\pm$ decays.

37 The two decay amplitudes $A(B^- \rightarrow D^0 K^-)$ and $A(B^- \rightarrow \bar{D}^0 K^-)$ differ by a factor $r_B e^{i(\delta_B - \gamma)}$,
 38 where r_B is the magnitude of the ratio of the decay amplitudes, and δ_B a strong phase difference.
 39 The sensitivity on γ depends on the size of r_B , as it represents the amount of interference. When
 40 changing the flavour of the decaying B meson, γ enters the equations with the opposite sign. Instead
 41 of directly fitting for γ the parametrizations

$$\begin{aligned} x_\pm &= r_B \cos(\delta_B \pm \gamma) \\ y_\pm &= r_B \sin(\delta_B \pm \gamma) \end{aligned} \quad (3.1)$$

42 are often used, as they are more robust, especially when the statistics is small or the results are
 43 close to physics boundaries. The subsequent D decay can contain amplitude and phase differences
 44 as well, which requires input from charm decays. Depending on the D final state three methods are
 45 distinguished: in the ADS method [6] CP eigenstates like $D \rightarrow K\pi$ are used, in the GLW method [7,8]
 46 CP -even D decays like $D \rightarrow K^+ K^-$ or $D \rightarrow \pi^+ \pi^-$, and in the GGSZ method [9] multi-body D
 47 decays, which require the analysis of the corresponding Dalitz plot.

48 4. Measurement of the CKM angle γ using $B^0 \rightarrow DK^{*0}$ [10,11]

49 In the measurement of γ from studies of $B^0 \rightarrow DK^{*0}$ decays the flavour of the decaying B
 50 meson can be inferred from the charges of the decay products of the K^{*0} meson, as the decay of
 51 the K^{*0} is flavour specific. The D meson can be reconstructed in the $D \rightarrow K_s^0 \pi^+ \pi^-$ final state.
 52 This requires an analysis of the Dalitz plot of the D phase space. The amplitude of the D^0 and
 53 the \bar{D}^0 decay can be assumed to be the same but there is a strong phase difference δ_D between the
 54 two decay amplitudes, which differs throughout the phase space. The strong phase can either be
 55 described by a specific amplitude model [10] or the results of a measurement of δ_D in bins of the
 56 Dalitz plot can be used [11].

57 Model-dependent approach [10]

58 Certain mass window requirements on the K_s^0 , K^{*0} and D candidates are applied. A boosted
 59 decision tree (BDT) [12,13] is trained to improve the signal purity. To disentangle signal from back-
 60 ground a fit to the invariant DK^* mass is performed. Apart from the signal, which is parametrized
 61 with the sum of two Crystal Ball functions [14], components for $B_s^0 \rightarrow DK^{*0}$ decays, combinatorial

62 background, partially reconstructed $B_{(s)}^0 \rightarrow D^* \bar{K}^{*0}$ decays, and misidentified $B^0 \rightarrow D\rho^0$ decays,
 63 are included in the fit model (see Fig. 2). The mass fit yields 89 ± 11 $B^0 \rightarrow DK^{*0}$ candidates in a
 64 ± 25 MeV/ c^2 mass window around the B^0 mass. In this mass window the CP fit is performed.

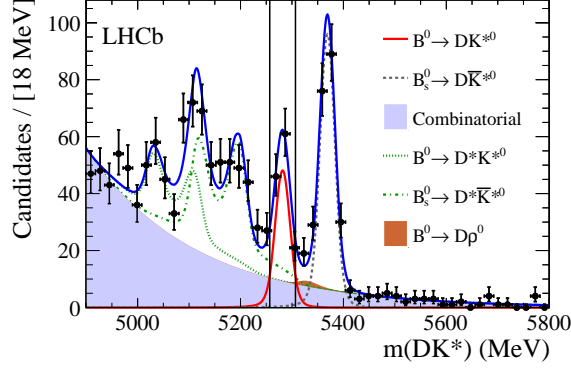


Figure 2: Invariant mass distribution for $B^0 \rightarrow DK^{*0}$ long and downstream candidates.

65 The efficiencies in the Dalitz plot are determined using simulations. The decay rates of B^0 and
 66 \bar{B}^0 can be expressed as

$$\begin{aligned} d\Gamma(B^0 \rightarrow DK^{*0}) &\propto |A_D|^2 + r_{B^0}^2 |\bar{A}_D|^2 + 2\kappa \text{Re}(A_D^* \bar{A}_D(x_+ + iy_+)), \\ d\Gamma(\bar{B}^0 \rightarrow D\bar{K}^{*0}) &\propto |A_D|^2 + r_{\bar{B}^0}^2 |\bar{A}_D|^2 + 2\kappa \text{Re}(A_D^* \bar{A}_D(x_- + iy_-)), \end{aligned} \quad (4.1)$$

67 where the amplitude model developed by BaBar [15] is applied for A_D and \bar{A}_D and the coherence
 68 factor κ is taken from the $B^0 \rightarrow DK^+ \pi^-$ amplitude analysis [16]. The CP parameters are measured
 69 to be

$$\begin{aligned} x_+ &= 0.05 \pm 0.24 \pm 0.04 \pm 0.01, \\ x_- &= -0.15 \pm 0.14 \pm 0.03 \pm 0.01, \\ y_+ &= -0.65_{-0.23}^{+0.24} \pm 0.08 \pm 0.01, \\ y_- &= 0.25 \pm 0.15 \pm 0.06 \pm 0.01, \end{aligned}$$

70 where the first uncertainty is statistical, the second systematic and the third covers the uncertain-
 71 ties introduced by the specific amplitude model, which are currently negligible compared to the
 72 other uncertainties. The largest systematic uncertainties arise from the invariant mass fit and the
 73 description of non- D background contributions. The values for x_{\pm} and y_{\pm} are transferred to

$$\gamma = (80_{-22}^{+21})^\circ, \quad r_B = 0.39 \pm 0.13, \quad \delta_B = (197_{-20}^{+24})^\circ.$$

74 Model-independent approach [11]

75 In the model-independent approach a very similar selection strategy is applied consisting of
 76 a rather loose preselection followed by a boosted decision tree and some particle identification
 77 requirements. The statistics is increased by reconstructing as well $D \rightarrow K_S^0 K^+ K^-$ decays. A si-
 78 multaneous fit to the invariant mass distribution of both final states is performed in the range

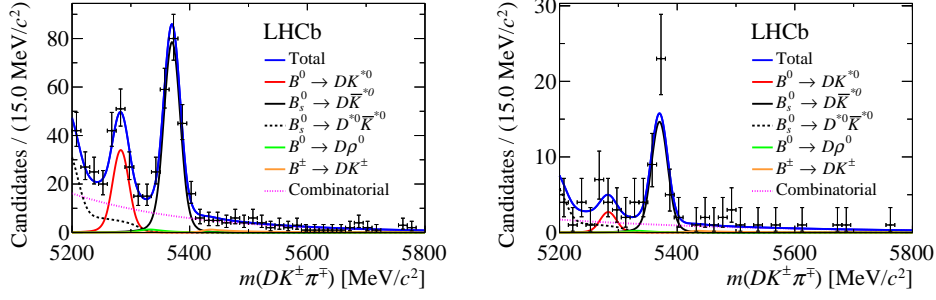


Figure 3: Invariant mass distributions of $B^0 \rightarrow DK^{*0}$ candidates with (left) $D \rightarrow K_S^0 \pi^+ \pi^-$ and (right) $D \rightarrow K_S^0 K^+ K^-$. The fit results, including the signal and background components, are superimposed.

79 5200–5800 MeV/c^2 . The lower mass boundary is higher than in the previously described model-
 80 dependent approach, which allows to neglect a component for $B^0 \rightarrow D^{*0} K^{*0}$ decays. All other
 81 components are the same as before. The resulting mass distributions are shown in Fig. 3.

82 The Dalitz plot shown in Fig. 4 is symmetrically binned into two times eight and two times
 83 two bins for the $D \rightarrow K_S^0 \pi^+ \pi^-$ and $D \rightarrow K_S^0 K^+ K^-$ final states, respectively. The expected number
 84 of candidates in bin i is given by

$$N_i(B^0) = n_{B^0} \left[F_{-i} + (x_+^2 + y_+^2) F_i + 2\kappa \sqrt{F_i F_{-i}} (x_+ c_i - y_+ s_i) \right],$$

$$N_i(\bar{B}^0) = n_{\bar{B}^0} \left[F_i + (x_-^2 + y_-^2) F_{-i} + 2\kappa \sqrt{F_i F_{-i}} (x_- c_i + y_- s_i) \right],$$

85 where F_i , the efficiency-corrected fraction of $D \rightarrow K_S^0 h^+ h^-$ candidates in bin i , is determined using
 86 $B^0 \rightarrow D^{*-} \mu^+ \nu_\mu$ decays with $D^{*-} \rightarrow \bar{D}^0 \pi^-$, and the values for $c_i = \cos \delta_D(i)$ and $s_i = \sin \delta_D(i)$ are
 87 taken from a CLEO measurement using quantum-correlated $\psi(3770) \rightarrow D^0 \bar{D}^0$ decays [17].

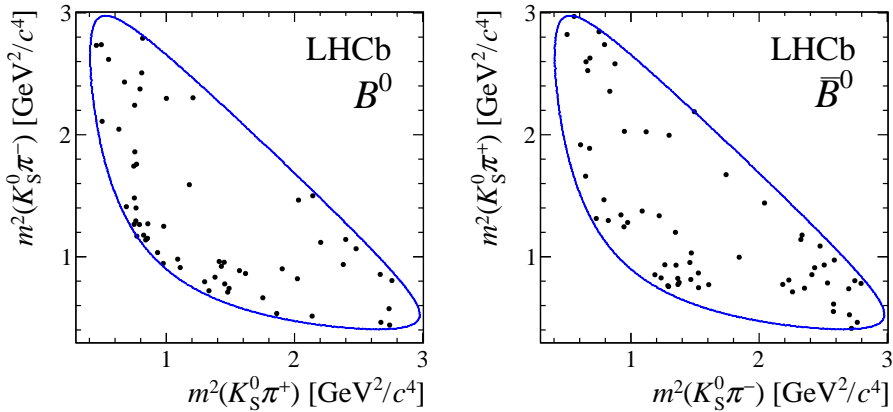


Figure 4: Dalitz plots of candidates in the signal region for $D \rightarrow K_S^0 \pi^+ \pi^-$ decays from (left) $B^0 \rightarrow DK^{*0}$ and (right) $\bar{B}^0 \rightarrow D\bar{K}^{*0}$ decays. The solid blue line indicates the kinematic boundary.

88 The results of the CP parameters

$$\begin{aligned} x_+ &= 0.05 \pm 0.35(\text{stat}) \pm 0.02(\text{syst}), \\ x_- &= -0.31 \pm 0.20(\text{stat}) \pm 0.04(\text{syst}), \\ y_+ &= -0.81 \pm 0.28(\text{stat}) \pm 0.06(\text{syst}), \\ y_- &= 0.31 \pm 0.21(\text{stat}) \pm 0.05(\text{syst}), \end{aligned}$$

89 are very similar to the ones of the model-dependent approach but slightly less precise. The latter
90 changes when translating the values to γ because a higher value for r_B is measured:

$$\gamma = (71 \pm 20)^\circ, \quad r_B = 0.56 \pm 0.17, \quad \delta_B = (204_{-20}^{+21})^\circ.$$

91 A direct comparison between the model-dependent and the model-independent approach is given
92 in Fig. 5, where the x - y -plane is depicted.

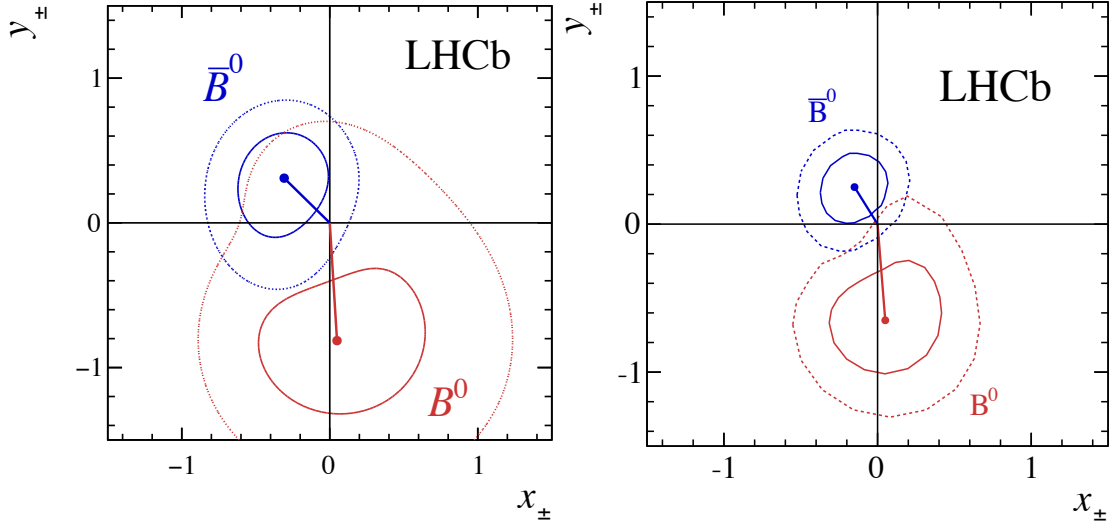


Figure 5: Confidence levels at (solid) 68.3 % and (dotted) 95.5 % for (red, light) (x_+, y_+) and (blue, dark) (x_-, y_-) as measured in $B^0 \rightarrow DK^{*0}$ decays (statistical uncertainties only) for (left) the model-independent analysis [11] and (right) the model-dependent approach [10]. The points represent the best fit values.

93 5. Constraints on the unitarity triangle angle γ from Dalitz plot analysis of 94 $B^0 \rightarrow DK^+ \pi^-$ decays [16]

95 Candidate $B^0 \rightarrow DK^+ \pi^-$ decays are selected with the D meson decaying into the $K^+ \pi^-$, $K^+ K^-$
96 or $\pi^+ \pi^-$ final state. After some loose requirements and vetoes to remove exclusive backgrounds,
97 neural networks (NNs), one for each D decay mode, are trained to separate the signal from the
98 remaining background. The networks make use of input variables that describe the corresponding
99 decay topology. Loose requirements are applied on the NNs. The resulting samples are divided
100 into five bins, which have a similar number of signal decays. A simultaneous mass fit is performed

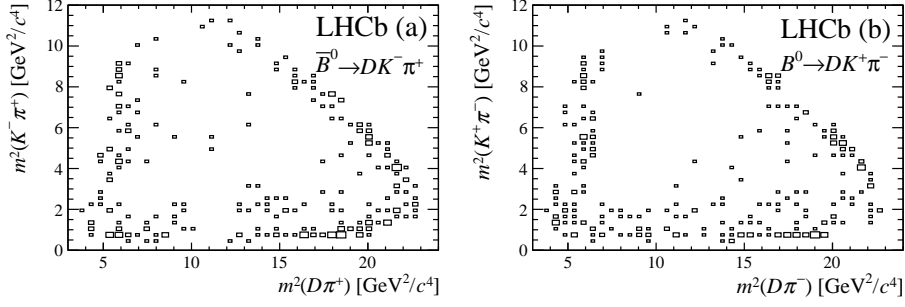


Figure 6: Dalitz plots for candidates in the B candidate mass signal region in the $D \rightarrow K^+ K^-$ and $D \rightarrow \pi^+ \pi^-$ samples for (a) \bar{B}^0 and (b) B^0 candidates. Background has not been subtracted, and therefore some contribution from $\bar{B}_s^0 \rightarrow D^{*0} K^+ \pi^-$ decays is expected at low $m(DK^+)$ (*i.e.* along the top right diagonal).

101 in the five bins and the results are statistically combined. For the analysis of the Dalitz plot, which
 102 is shown in Fig. 6, only the candidates in the 2.5σ window around the B^0 peak are used. The decay
 103 amplitude is parametrized with the isobar model:

$$A(m^2(D\pi^-), m^2(K^+\pi^-)) = \sum_{j=1}^N c_j F_j(m^2(D\pi^-), m^2(K^+\pi^-)).$$

104 The functions F_j describe the resonant dynamics considering line shape, angular distributions and
 105 barrier factors as a function of the phase space $(m^2(D\pi^-), m^2(K^+\pi^-))$. The parametrization of
 106 the $D\pi$ system takes into account contributions from $D_0^*(2400)^-$, $D_2^*(2460)^-$, and $D\pi^-$ S- and
 107 P-waves. The masses and widths of the resonances in the $D\pi$ system are constrained. In the $K\pi$
 108 system the masses and widths of the resonances $K^*(892)^0$, $K^*(1410)^0$, and $K_2^*(1430)^0$ are fixed.
 109 Additionally, a $K^+\pi^-$ S-wave component is considered. Only for the complex coefficient c_j of
 110 the $K^*(892)^0$ contribution CP violation is allowed in the fit. The fit results for x_{\pm} and y_{\pm} show no
 111 significant CP violation. Neither a non-zero value for r_B can be established nor any value for γ can
 112 be excluded at 95 % confidence level.

113 6. Measurement of CP observables in $B^{\pm} \rightarrow DK^{\pm}$ and $B^{\pm} \rightarrow D\pi^{\pm}$ with two- and 114 four-body D decays [18]

115 When reconstructing the D mesons of $B^{\pm} \rightarrow Dh^{\pm}$ decays ($h = K^{\pm}$ or π^{\pm}) in the $K^+\pi^-$ or in
 116 the $K^+\pi^-\pi^+\pi^-$ final state, large interference between the $B^- \rightarrow D^0 h^-$ and the $B^- \rightarrow \bar{D}^0 h^-$ decay
 117 rates occurs. The reason is that both amplitudes are the combination of a Cabibbo-favoured and a
 118 Cabibbo-suppressed decay (ADS method). The decay rate is given by

$$\Gamma(B^{\pm} \rightarrow f_D h^{\pm}) \propto (r_D^f)^2 + r_B^2 + 2r_B r_D^f \kappa_D^f \cos(\delta_B + \delta_D^f \pm \gamma), \quad (6.1)$$

119 where r_D^f and r_B are the ratio of the suppressed and favoured amplitudes of the D and B decays,
 120 respectively. For the two-body final state the coherence factor κ_D^f is unity while for the four-body
 121 final state it has been measured to be $\kappa_D^{K^3\pi} = 0.32^{+0.12}_{-0.08}$ [19]. One of the observables that are

122 determined in this analysis is the charge asymmetry

$$A \equiv \frac{\Gamma(B^- \rightarrow f_D h^-) - \Gamma(B^+ \rightarrow \bar{f}_D h^+)}{\Gamma(B^- \rightarrow f_D h^-) + \Gamma(B^+ \rightarrow \bar{f}_D h^+)}, \quad (6.2)$$

123 which can be directly calculated from the efficiency-corrected B^- and B^+ yields. Although the
124 samples with bachelor pions are clearly larger and thus have smaller statistical uncertainties than
125 the ones with bachelor kaons, the most significant asymmetry, in fact even the first observation of
126 CP violation with a single $B \rightarrow Dh$ mode, is achieved in $B \rightarrow DK$ with $D \rightarrow K\pi$:

$$A_{\text{ADS}(K)}^{\pi K} = -0.403 \pm 0.056(\text{stat}) \pm 0.011(\text{syst}).$$

127 A fit to the invariant mass distributions of selected $B \rightarrow DK$ decays is shown in Fig. 7.

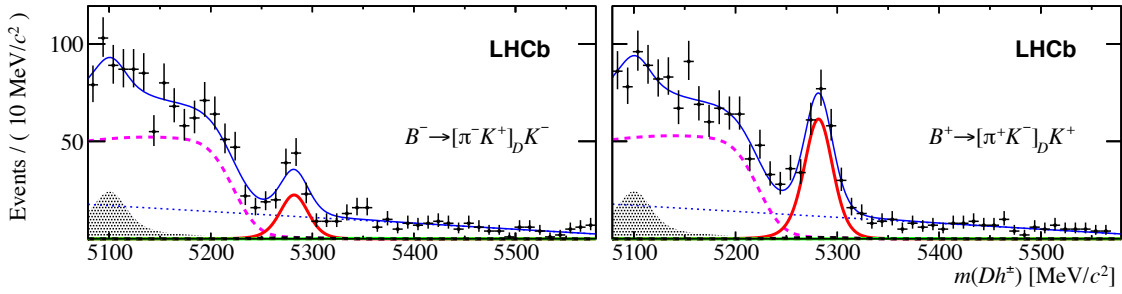


Figure 7: Invariant mass distributions of selected $B \rightarrow DK$ decays, separated by charge. The dashed pink line left of the signal peak (red, thick) shows partially reconstructed $B_s^0 \rightarrow DK^- \pi^+$ decays, where the bachelor pion is missed.

128 Another approach is to reconstruct D final states that are CP eigenstates (GLW method). In
129 this case, the decay rates simplify to

$$\Gamma(B^{\mp} \rightarrow f_D h^{\mp}) \propto 1 + r_B^2 + 2r_B(2F_+ - 1) \cos(\delta_B \mp \gamma), \quad (6.3)$$

130 as r_D is unity and δ_D is zero. While the two-body final states $\pi^+ \pi^-$ and $K^+ K^-$ are totally CP -
131 even ($F_+ = 1$), the fraction of the CP -even component in the four-body D final state $\pi^+ \pi^- \pi^+ \pi^-$ is
132 determined to be $F_+^{4\pi} = 0.737 \pm 0.028$ [20]. For the first time CP asymmetries with this four-body
133 D final state are determined, among others the charge asymmetry:

$$A_{\text{GLW}(K)}^{\pi\pi\pi\pi} = 0.100 \pm 0.034(\text{stat}) \pm 0.018(\text{syst}).$$

134 7. Measurement of the CKM angle γ from a combination of $B \rightarrow DK$ analyses [21]

135 The tree-level measurements of the CKM angle γ from $B \rightarrow DK$ decays are combined. The
136 combination comprises results from $B^\pm \rightarrow DK^\pm$, $B^0 \rightarrow DK^{*0}$, $B^+ \rightarrow DK^+ \pi^+ \pi^-$, and $B_s^0 \rightarrow D_s^\pm K^\pm$
137 decays and follows a frequentist treatment. To obtain the best precision, the hadronic parameters
138 are also considered in the combination. The average value $\gamma = (70.9_{-8.5}^{+7.1})^\circ$ is the most precise
139 single-experiment measurement to date. The shapes of the 1 - CL curves, split by the method, are
140 shown in Fig. 8.

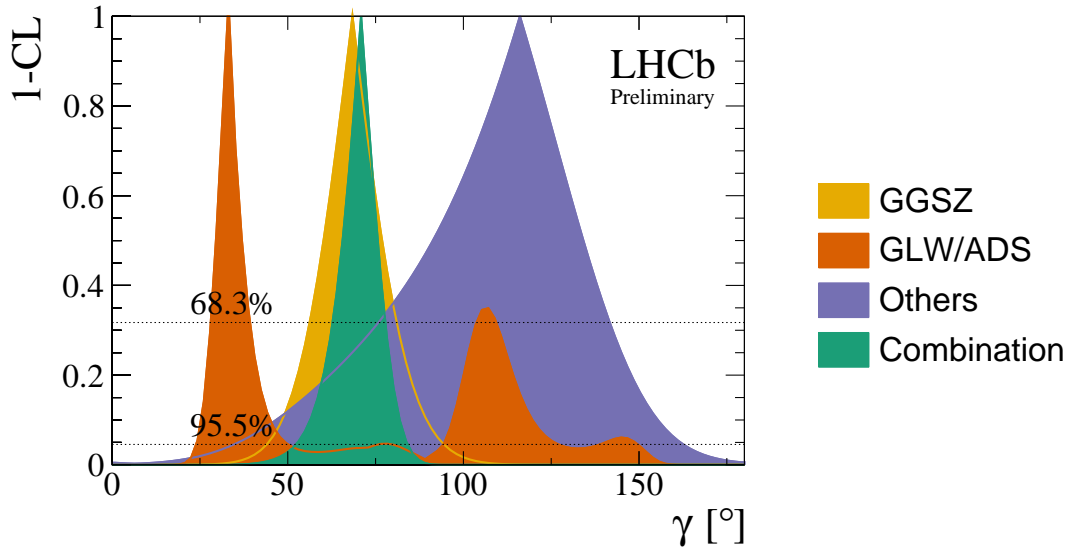


Figure 8: $1 - \text{CL}$ curves for the combination of the γ measurements and the contributions from the individual methods.

141 8. Conclusion

142 With the world's largest sample of B -hadrons LHCb has performed many promising mea-
 143 surements of γ . Using the GGSZ method $B^0 \rightarrow DK^{*0}$ decays have been analysed with a model-
 144 dependent and a model-independent approach. The ADS and the GLW method have been applied
 145 to measure the asymmetries in $B \rightarrow Dh$ decays using two- and four-body final states. All $B \rightarrow DK$
 146 modes are combined into an average value of $\gamma = (70.9_{-8.5}^{+7.1})^\circ$, which represents the most precise
 147 measurement from a single experiment. This result will even be improved once the $B \rightarrow D\pi$ modes
 148 are included as well.

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