# The $X$ (3872) and the search for its bottomonium counterpart at the LHC 

K. Toms*<br>University of New Mexico, USA<br>E-mail: ktoms@cern.ch

We present results on $X$ (3872) particle studies at three LHC experiments: ATLAS, CMS, and LHCb. Production cross section measurements are reported, as well as determination of the $X(3872)$ quantum numbers. The search of the $X(3872)$ bottomonium counterpart is also described.

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## 1. Introduction

The $X(3872)$ particle was first discovered by the Belle experiment in 2003 in the transition $B^{ \pm} \rightarrow$ $K^{ \pm} X\left(\rightarrow J / \psi \pi^{+} \pi^{-}\right)$[1] and soon was confirmed by many experiments [2]. The $X(3872)$ state is narrow, with mass close to the $D^{0} \bar{D}^{0 *}$ threshold and decays to the $\rho^{0} J / \psi$ and $\omega J / \psi$ final states with comparable branching fractions, thus violating isospin symmetry, so it cannot be a simple $c \bar{c}$ state. The nature of the state remains unclear, and there are many theoretical developments that suggest different models to describe the $X(3872)$ structure, see for example [3]. Heavy quark symmetry implies the existence of a hidden-beauty partner, $X_{b}$, which should be produced in $p p$ collisions.

In this paper we present the results by three LHC [4] experiments: ATLAS [5], CMS [6], and LHCb [7], related to the studies of $X(3872)$ properties and search for its bottomonium counterpart.

## 2. Search for $X_{b}$ at ATLAS and CMS

The decay $X_{b} \rightarrow \pi^{+} \pi^{-} \Upsilon(1 S)\left(\rightarrow \mu^{+} \mu^{-}\right)$may serve as a decay mode analogous to that in which the $X(3872)$ was discovered. CMS reported results on a search for this decay, finding no evidence for narrow states in the $10.06-10.31 \mathrm{GeV}$ and $10.40-10.99 \mathrm{GeV}$ mass ranges [8]. Upper limits on the product of cross section and branching fraction at values between $0.9 \%$ and $5.4 \%$ of the $\Upsilon(2 S)$ rate were set. The resulting plot is shown in Figure 1 right. ATLAS has performed a similar search [9] with results shown in Figure 1 left, and no evidence for new narrow states with masses in the range $10.05-10.31 \mathrm{GeV}$ and $10.40-11.00 \mathrm{GeV}$ was found. Separate fits to the $\Upsilon\left(1^{3} D_{J}\right)$ triplet, $\Upsilon(10860)$, and $\Upsilon(11020)$ also reveal no significant signals.


Figure 1: Left: Observed $95 \% \mathrm{CL}_{S}$ upper limits (solid line) on the relative production rate $R=(\sigma B) /(\sigma B)_{2 S}$ of a hypothetical $X_{b}$ parent state decaying isotropically to $\pi^{+} \pi^{-} \Upsilon(1 S)$, as a function of mass. The median expectation (dashed) and the corresponding $\pm 1 \sigma$ and $\pm 2 \sigma$ bands (green and yellow respectively) are also shown. The bar on the right shows typical shifts under alternative $X_{b}$ spin-alignment scenarios, relative to the isotropic ("FLAT") case shown with the solid points [9]. Right: Upper limits at the $95 \%$ confidence level on $R$, the production cross section for the $X_{b}$ times its branching fraction to $\Upsilon(1 S) \pi^{+} \pi^{-}$relative to the $\Upsilon(2 S)$, as a function of the $X_{b}$ mass. The solid curve shows the observed limits, while the dashed curve represents the expected limits in the absence of a signal, with the two shaded regions giving the $\pm 1$ and $\pm 2$ standard deviation uncertainties on the expected limits. The measured value for the analogous $X(3872)$ to $\psi(2 S)$ ratio of $6.56 \%$ is shown by the dotted line [8].

## 3. Production measurement of $\psi(2 S)$ and $X(3872)$ at ATLAS and CMS

A cross-section measurement of promptly produced $X$ (3872) was performed by CMS [10] at $\sqrt{s}=7$ TeV as a function of transverse momentum $p_{\mathrm{T}}$. It was done in a kinematic range in which the $X(3872)$ had $\left(10<p_{\mathrm{T}}<50\right) \mathrm{GeV}$ and rapidity $|y|<1.2$. The ratio of the $X(3872)$ and $\psi(2 S)$ cross sections times their branching fractions into $J / \psi \pi^{+} \pi^{-}$was measured as a function of $p_{\mathrm{T}}$. It has been shown that the nonrelativistic QCD (NRQCD) prediction [11] for prompt $X$ (3872) production, assuming a $D^{0} \bar{D}^{* 0}$ molecule, is too high, although the shape of the $p_{\mathrm{T}}$ dependence was described fairly well. A later interpretation of
the $X(3872)$ as a mixed $\chi_{c 1}(2 P)-D^{0} \bar{D}^{* 0}$ state, where the $X(3872)$ is produced predominantly through its $\chi_{c 1}(2 P)$ component, was adopted in conjunction with the next-to-leading-order (NLO) NRQCD model and fitted to CMS data, showing a good agreement [12]. ATLAS has performed a similar study at $\sqrt{s}=8 \mathrm{TeV}$ [13] with the $J / \psi \pi^{+} \pi^{-}$candidates having $\left(10<p_{\mathrm{T}}<70\right) \mathrm{GeV}$ and $|y|<0.75$. Two models of the lifetime dependence of the non-prompt production are considered: a model with a single effective lifetime, and an alternative model with two distinctly different effective lifetimes. The two models give compatible results for the prompt and non-prompt differential cross sections of the $\psi(2 S)$ and $X(3872)$. For the single-lifetime model, assuming that non-prompt $\psi(2 S)$ and $X(3872)$ originate from the same mix of parent $b$-hadrons, the following result is obtained for the ratio of the branching fractions:

$$
R_{B}^{1 \mathrm{~L}}=\frac{\mathscr{B}(B \rightarrow X(3872)+\text { any }) \mathscr{B}\left(X(3872) \rightarrow J / \psi \pi^{+} \pi^{-}\right)}{\mathscr{B}(B \rightarrow \psi(2 S)+\text { any }) \mathscr{B}\left(\psi(2 S) \rightarrow J / \psi \pi^{+} \pi^{-}\right)}=(3.95 \pm 0.32(\text { stat }) \pm 0.08(\text { sys })) \times 10^{-2},
$$

[13]. In the two-lifetime model, the two lifetimes are fixed to expected values for $X(3872)$ originating from the decays of the $B_{c}$ and from long-lived $b$-hadrons, respectively, with their relative weight determined from the fits to the data. The ratio of the branching fractions $R_{B}$ is determined from the long-lived component alone:

$$
R_{B}^{2 \mathrm{~L}}=\frac{\mathscr{B}(B \rightarrow X(3872)+\text { any }) \mathscr{B}\left(X(3872) \rightarrow J / \psi \pi^{+} \pi^{-}\right)}{\mathscr{B}(B \rightarrow \psi(2 S)+\text { any }) \mathscr{B}\left(\psi(2 S) \rightarrow J / \psi \pi^{+} \pi^{-}\right)}=(3.57 \pm 0.33(\text { stat }) \pm 0.11(\text { sys })) \times 10^{-2},
$$

[13]. In the two-lifetime model, the fraction of the short-lived non-prompt component in $X$ (3872) production, for $p_{\mathrm{T}}>10 \mathrm{GeV}$, is found to be

$$
\begin{equation*}
\frac{\sigma\left(p p \rightarrow B_{c}+\text { any }\right) \mathscr{B}\left(B_{c} \rightarrow X(3872)+\text { any }\right)}{\sigma(p p \rightarrow \text { non-prompt } X(3872)+\text { any })}=(25 \pm 13(\text { stat }) \pm 2(\text { sys }) \pm 5(\text { spin })) \% \tag{3.1}
\end{equation*}
$$

[13]. The measured differential cross section for non-prompt production of the $X(3872)$ is shown in Figure 2 (right). This is compared to a calculation based on the FONLL model prediction for $\psi(2 S)$, recalculated for the $X(3872)$ using a kinematic template [13] for the non-prompt $X(3872) / \psi(2 S)$ ratio and the effective value of the product of the branching fractions $\mathscr{B}(B \rightarrow X(3872)) \mathscr{B}\left(X(3872) \rightarrow J / \psi \pi^{+} \pi^{-}\right)=(1.9 \pm 0.8) \times 10^{-4}$ estimated in Ref. 3.1 based on Tevatron data [15]. This calculation overestimates the data by a factor increasing with $p_{\mathrm{T}}$ from about four to about eight over the $p_{\mathrm{T}}$ range of this measurement. The non-prompt fractions of $\psi(2 S)$ and $X(3872)$ production are shown in Figure 3. The non-prompt fraction of $X(3872)$ shows no sizeable dependence on $p_{\mathrm{T}}$. This measurement agrees within uncertainties with the CMS result obtained at $\sqrt{s}=7 \mathrm{TeV}$ [10].


Figure 2: Measured cross section times branching fractions as a function of $p_{\mathrm{T}}$ for (left) prompt $X$ (3872) in the ATLAS experiment [13] compared to NLO NRQCD predictions with the $X(3872)$ modelled as a mixture of $\chi_{c 1}(2 P)$ and a $D^{0} \bar{D}^{* 0}$ molecular state [12], and (right) non-prompt $X$ (3872) compared to the FONLL [14] model prediction. Bottom plots on both left and right show theory to data ratio.


Figure 3: Measured non-prompt fractions for (left) $\psi(2 S)$ and (right) $X(3872)$ production in the ATLAS experiment [13], compared to CMS results [10] at $\sqrt{s}=7 \mathrm{TeV}$. The blue circles are the results reported by ATLAS, while the green squares show CMS results [10, 16].

## 4. Determination of the $X(3872)$ quantum numbers at $\mathbf{L H C b}$

Early constraints on the $X(3872)$ quantum numbers were set by CDF [17] and have restricted the options to $1^{++}$and $2^{-+}$. LHCb's 2013 full angular analysis [18] settled on $1^{++}$, but that analysis assumed that the lowest orbital angular momentum process dominated the decay. A new analysis [19] described below removed that assumption. The analysis uses $3 \mathrm{fb}^{-1}$ of $\sqrt{s}=7 \mathrm{TeV}$ and $\sqrt{s}=8 \mathrm{TeV}$ data.

The $X(3872)$ signal is sought in the decay $B^{+} \rightarrow X(3872) K^{+}$with $X(3872) \rightarrow \rho^{0} J / \psi, \rho^{0} \rightarrow \pi^{+} \pi^{-}$, and $J / \psi \rightarrow \mu^{+} \mu^{-}$. The fit yields $1011 \pm 38$ signal events over a background of $1468 \pm 44$ in the $\Delta \mathrm{M}$ range of (725-825) MeV. The $X$ (3872) mass resolution is 2.8 MeV . The signal purity is $80 \%$ within 2.5 standard deviations around the peak.

Angular correlations in the $B^{+}$decay chain are analyzed using an unbinned maximum-likelihood fit to determine the $X(3872)$ quantum numbers and orbital angular momentum. The probability density function $(\mathscr{P})$ for each $J^{P C}$ hypothesis, $J_{X}$, is defined in the five-dimensional angular space $\Omega \equiv$ $\left(\cos \theta_{X}, \cos \theta_{\rho}, \Delta \phi_{X, \rho}, \cos \theta_{J / \psi}, \Delta \phi_{X, J / \psi}\right)$, where $\theta_{X}, \theta_{\rho}$ and $\theta_{J / \psi}$ are the helicity angles in the $X(3872), \rho^{0}$ and $J / \psi$ decays, respectively, and $\Delta \phi_{X, \rho}$ and $\Delta \phi_{X, J / \psi}$ are the angles between the decay planes of the $X(3872)$ particle and its decay products. The quantity $\mathscr{P}$ is the normalized product of the expected decay matrix element $(\mathscr{M})$ squared and the reconstruction efficiency $(\varepsilon), \mathscr{P}\left(\Omega \mid J_{X}\right)=\left|\mathscr{M}\left(\Omega \mid J_{X}\right)\right|^{2} \varepsilon(\Omega) / I\left(J_{X}\right)$, where $I\left(J_{X}\right)=\int\left|\mathscr{M}\left(\Omega \mid J_{X}\right)\right|^{2} \varepsilon(\Omega) d \Omega$. The efficiency is averaged over the $\pi^{+} \pi^{-}$mass of the $X(3872) \rightarrow \rho^{0} J / \psi$, $\rho^{0} \rightarrow \pi^{+} \pi^{-}$decay. The lineshape of the $\rho^{0}$ resonance can change slightly depending on the $X(3872)$ spin hypothesis. The effect on $\varepsilon(\Omega)$ is very small and is neglected. The angular correlations are obtained using the helicity formalism,

$$
\begin{aligned}
\left|\mathscr{M}\left(\Omega \mid J_{X}\right)\right|^{2}=\sum_{\Delta \lambda_{\mu}=-1,+1} \mid & \sum_{\lambda_{J / \psi}, \lambda_{\rho}=-1,0,+1} A_{\lambda_{J / \psi}, \lambda_{\rho}} D_{0, \lambda_{J / \psi}-\lambda_{\rho}}^{J_{X}}\left(0, \theta_{X}, 0\right)^{*} \\
& \left.D_{\lambda_{\rho}, 0}^{1}\left(\Delta \phi_{X, \rho}, \theta_{\rho}, 0\right)^{*} D_{\lambda_{J / \psi}, \Delta \lambda_{\mu}}^{1}\left(\Delta \phi_{X, J / \psi}, \theta_{J / \psi}, 0\right)^{*}\right|^{2}
\end{aligned}
$$

where the $\lambda$ 's are particle helicities, $\Delta \lambda_{\mu}=\lambda_{\mu^{+}}-\lambda_{\mu^{-}}$, and the $D_{\lambda_{1}, \lambda_{2}}^{J}$ are Wigner functions. The helicity couplings, $A_{\lambda_{J / \psi}, \lambda_{\rho}}$, are expressed in terms of the $L S$ couplings, $B_{L S}$, through Clebsch-Gordan coefficients, where $L$ is the orbital angular momentum between the $\rho^{0}$ and the $J / \psi$ mesons, and $S$ is the sum of their spins. The possible values of $L$ are constrained by parity conservation, $P_{X}=P_{J / \psi} P_{\rho}(-1)^{L}=(-1)^{L}$. In this analysis all $L$ values are allowed. Values of $J_{X}$ up to four are analyzed. Since the orbital angular momentum in the $B^{+}$decay equals $J_{X}$, high values are suppressed by the angular momentum barrier. The set of possible complex $B_{L S}$ amplitudes, which are free parameters in the fit, is denoted as $\alpha$. The function to be minimized is $-2 \ln \mathscr{L}\left(J_{X}, \alpha\right) \equiv-s_{w} 2 \sum_{i=1}^{N_{\text {data }}} w_{i} \ln \mathscr{P}\left(\Omega_{i} \mid J_{X}, \alpha\right)$, where $\mathscr{L}\left(J_{X}, \alpha\right)$ is the unbinned likelihood and $N_{\text {data }}$ is the number of selected candidates. The background is subtracted using the $s P l o t$ technique [20]
by assigning a weight, $w_{i}$, to each candidate based on its $\Delta M$ value. No correlations between $\Delta M$ and $\Omega$ are observed. Prompt production of $X(3872)$ in $p p$ collisions gives negligible contribution to the selected sample. Statistical fluctuations in the background subtraction are taken into account in the log-likelihood value via a constant scaling factor, $s_{w}=\sum_{i=1}^{N_{\text {data }}} w_{i} / \sum_{i=1}^{N_{\text {data }}} w_{i}{ }^{2}$. The $1^{++}$hypothesis gives the highest likelihood value. Projections of the data and of the fit $\mathscr{P}$ onto individual angles show good consistency with the $1^{++}$assignment as is illustrated in Fig. 4 left. Inconsistency with the other assignments is apparent when correlations between various angles are examined. For example, the data projection onto $\cos \theta_{X}$ is consistent only with the $1^{++}$fit projection after requiring $\left|\cos \theta_{\rho}\right|>0.6$ (see Fig. 4 right), while inconsistency with the other quantum number assignments is less clear without the $\cos \theta_{\rho}$ requirement.

In summary, the analysis confirms that the eigenvalues of total angular momentum, parity, and chargeconjugation of the $X(3872)$ state are $1^{++}$. These quantum numbers are consistent with those predicted by the molecular or tetraquark models and with the $\chi_{c 1}\left(2^{3} \mathrm{P}_{1}\right)$ charmonium state [21], possibly mixed with a molecule [22]. Other charmonium states are excluded. No significant D-wave fraction is found, with an upper limit of $4 \%$ at $95 \%$ C.L. The $S$-wave dominance is expected in the charmonium or tetraquark models, in which the $X(3872)$ state has a compact size. An extended size, as that predicted by the molecular model, implies more favorable conditions for the D wave. However, conclusive discrimination among models is difficult because quantitative predictions are not available.


Figure 4: Left: Background-subtracted distributions of all angles for the data (points with error bars) and for the $1^{++}$fit projections (solid histograms). Right: Background-subtracted distribution of $\cos \theta_{X}$ for candidates with $\left|\cos \theta_{\rho}\right|>0.6$ for the data (points with error bars) compared to the expected distributions for various $X(3872) J^{P C}$ assignments (solid histograms) with the $B_{L S}$ amplitudes obtained by the fit to the data in the five-dimensional angular space. The fit displays are normalized to the observed number of signal events in the full angular phase space.

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[^0]:    *Speaker.
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