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Initial state correlations.

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We point out that Bose enhancement in a hadronic wave function generically leads to correlations between produced particles. We illustrate this general phenomenon by considering particle production within the Color Glass Condensate framework. We show that the Bose enhancement of gluons in the projectile leads to azimuthal collimation of long range rapidity correlations of the produced particles, the so-called ridge correlations.

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1. Introduction

The classic QCD analyses of hadronic structure in high energy scattering experiments are based on collinear factorization picture. Although this approach is very useful to describe perturbative processes, the hadronic structure is much richer than implied in simple collinear picture. The hadrons in the wave function are certainly correlated. These correlations are not important for inclusive reactions like DIS, where only the total number of partons in the wave function matters, or even in semi inclusive DIS which probes the average distribution of partons in the transverse plane - TMD's.

It is however clearly very interesting to understand the details of the correlated structure of hadronic wave function. It must be observable in less inclusive experiments, which for example measure correlations between produced particles.

The purpose of this contribution is to discuss one very particular type of correlations within a very specific framework. Namely we will deal with Bose-Einstein correlations between gluons in a high energy proton wave function[1]. The approximation we use is the so called Color Glass Condensate (CGC) approximation to a high energy hadronic wave function.

The practical motivation comes from an attempt to understand the so called ridge correlations in particle production observed in p-p and p-Pb collisions at LHC.

The ridge structure observed in high multiplicity p-p [2] and p-Pb [3] collisions at the Large Hadron Collider (LHC) triggered an intense activity aimed at understanding the possible physical origin of correlations between emitted particles. Two basic ideas have been put forward in this context (see others in [4]).

According to one idea, the origin of the correlations is the same as in similar ridge correlations observed earlier in heavy ion collisions at the Relativistic Heavy Ion Collider [5] and the LHC [6]. Namely, the angular collimation is due to flow effects in the final state [7]. The qualitative features of the high multiplicity p-p and p-Pb data, including the dependence on masses of produced particles, are well described by the hydrodynamic-based models. It is nevertheless challenging to explain how the spatially small system produced in the final state in p-p collisions can sustain the collective behavior necessary for local equilibration.

The second suggestion is that the final state correlations carry the imprint of the partonic correlations that exist in the initial state. Three different variants of such initial state effects have been discussed in the literature: local anisotropy of target fields [8], spatial variation of partonic density [9] and finally the "glasma graph" contributions to particle production [10] within the Color Glass Condensate (CGC) approach to high-energy hadronic scattering. While the physical origin of the first two effects is quite clear, the physics behind glasma graphs has not been elucidated in the literature. On the other hand, numerical calculations based on the glasma graph approach have been very successful in reproducing the systematics of ridge correlations [11]. It is therefore important to understand the physics that underlies these numerical results.

The purpose of this Letter is to point out that there exists a general quantum mechanical mechanism that leads to positive correlations of emitted particles with similar quantum numbers. It is operative when the wave function of an incoming hadron is dominated by bosons (gluons), and is due to Bose enhancement in this wave function. In the next section, after recalling the basic derivation, we will show that this is precisely the physical mechanism that underlies the glasma graph calculation of hadron production in p-p and p-A collisions. The mechanism itself is however more general, has been widely used for identical mesons in heavy-ion collisions, see e.g. [12]. Analogously, for fermions in the initial state one expects the opposite effect, namely Pauli blocking. In the final section, after discussing our results, we briefly address the question of which final state observables could be sensitive to the initial state Pauli blocking.

To avoid confusion, we stress that by Bose enhancement we do not mean the Hanbury-Brown-Twiss (HBT) correlations between emitted particles, which arise due to emission from a large source comprised of many incoherent emitters. We rather mean the effect of Bose statistics that enhances the probability to find two identical bosons with the same transverse momentum *in the incoming projectile wave function before the collision*. Although this initial state enhancement is for two incoming bosons with identical transverse momentum, the momenta of the two are modified differently by the interaction with the target. Thus after scattering the two bosons emerge in the final state with different momenta. The correlation between the directions of the two momenta is nevertheless preserved in some range of kinematics, see later.

2. Gluon production and Bose enhancement

2.1 Basics of Bose enhancement

The prototypical textbook calculation of Bose enhancement proceeds as follows [13]. Consider a state with fixed occupation numbers of *N* species of bosons at different momenta, $|\{n^i(p)\}\rangle \equiv \prod_{i,p} \frac{1}{\sqrt{n^i(p)!}} (a_i^{\dagger}(p)/\sqrt{V})^{n^i(p)} |0\rangle$, i = 1, ..., N, with a finite volume *V* and periodic boundary conditions so that momenta are discrete. The state is translationally invariant with mean particle density

$$n \equiv \langle \{n^{i}(p)\} | a^{\dagger i}(x) a^{i}(x) | \{n^{i}(p)\} \rangle = \sum_{i,p} n^{i}(p).$$
(2.1)

Hereafter we take $\sum_{p} \approx \int d^{3}p/(2\pi)^{3}$. The 2-particle correlator in coordinate space is

$$D(x,y) \equiv \langle \{n(p)\} | a^{\dagger i}(x) a^{\dagger j}(y) a^{i}(x) a^{j}(y) | \{n(p)\} \rangle.$$

$$(2.2)$$

This is calculated by going to momentum space, where the operator averages are simple:

$$\langle \{n(p)\} | a^{\dagger i}(p) a^{\dagger j}(q) a^{i}(l) a^{j}(m) | \{n(p)\} \rangle$$

$$= \langle \{n(p)\} | \delta(p-l) \delta(q-m) a^{\dagger i}(p) a^{i}(p) a^{\dagger j}(q) a^{j}(q)$$

$$+ \delta(p-m) \delta(q-l) a^{\dagger i}(p) a^{j}(p) a^{\dagger j}(q) a^{i}(q) | \{n(p)\} \rangle$$

$$\approx \delta(p-l) \delta(q-m) \sum_{i} n^{i}(p) \sum_{j} n^{j}(q)$$

$$+ \delta(p-m) \delta(q-l) \sum_{i} n^{i}(p) n^{i}(q),$$

$$(2.3)$$

where we have neglected the terms where all momenta are equal, which are suppressed by a phase space factor. Using this, the result for D(x, y) reads

$$D(x,y) = n^{2} + \sum_{i} \left| \int \frac{d^{3}p}{(2\pi)^{3}} e^{ip(x-y)} n^{i}(p) \right|^{2}.$$
 (2.4)

The last term expresses the Bose enhancement. It vanishes when the points are very far away, and gives $\mathcal{O}(1/N)$ enhancement when the points coincide. The $\mathcal{O}(1/N)$ suppression of the second term relative to the first one is due to the fact that the second term contains a single sum over the species index. The physics is that only bosons of the same species are correlated with each other. Technically the origin of this additional contribution is the "wrong contraction" term in eq. (2.3).

The Bose enhancement is a generic phenomenon, and is not tied specifically to the state with fixed number of particles. An overwhelming majority of pure states or quantum density matrices exhibit Bose enhancement at some degree. There is however one type of states that do not exhibit such behavior, notably classical-like coherent states. Consider a coherent state

$$|b(x)\rangle \equiv \exp\{i\int d^3x \, b^i(x)(a^i(x) + a^{\dagger i}(x))\} \,|0\rangle.$$
(2.5)

A trivial calculation in this state gives

$$\langle b(x)|a^{\dagger i}(x)a^{i}(x)|b(x)\rangle = b^{i}(x)b^{i}(x),$$

$$\langle b(x)|a^{\dagger i}(x)a^{\dagger j}(y)a^{i}(x)a^{j}(y)|b(x)\rangle = b^{i}(x)b^{i}(x)b^{j}(y)b^{j}(y),$$

$$(2.6)$$

so D(x,y) = n(x)n(y). Thus, in order to exhibit Bose enhancement, a state has to be nonclassical.

2.2 Gluon production via glasma graphs

As stated above, we want to demonstrate that the angular collimation arising from the glasma graph calculation owes its existence to the Bose enhancement in the projectile wave function. Following [11, 14], we consider the calculation of inclusive two particle production and assume local parton-hadron duality, namely that at a given momentum the number of produced hadrons is proportional to the number of produced gluons.

The graphs that contribute to this observable can be conveniently represented in terms of averages of gluon creation and annihilation operators in the incoming projectile wave function (see supplementary material and [14]). They come in three varieties, see fig. 1. Type A graphs give the contribution whereby two gluons from the incoming projectile wave function scatter independently on the target. The incoming gluons have transverse momenta k_1 and k_2 respectively. While propagating through the target the first particle picks up transverse momentum $p - k_1$ and the second particle picks up transverse momentum $q - k_2$, so that the outgoing particles have momenta p and q. Type B and C graphs from the projectile point of view are "interference graphs", in the sense that the final state gluon with momentum p comes from the projectile gluons with different momenta in the amplitude and complex conjugate amplitude.

Type B and C diagrams contain leading contributions that can be reinterpreted as Type A but with gluons originating from the target rather than from the projectile, and additionally subleading contributions, including those that lead to HBT correlations [15]. Therefore, in the following we will only discuss those of Type A, keeping in mind this complementary interpretation of the leading pieces of Type B and C.

The Type A contribution to double inclusive gluon production can be written as

$$C \int_{k_1,k_2} \langle in|a_a^{\dagger i}(k_1)a_b^{\dagger j}(k_2)a_a^k(k_1)a_b^l(k_2)|in\rangle$$
(2.7)

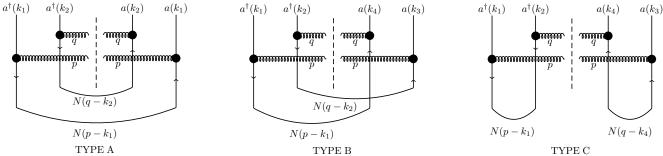


Figure 1: Glasma graphs for two gluon inclusive production before averaging over the projectile color charge density ρ . Black blobs denote vertices which involve two momenta, e.g. $\delta^{ij} - p^i k_1^j / p^2$, and dashed lines the cuts. For details see the text.

$$\times \left[\delta^{ik} - \frac{k_1^i k_1^k}{p^2}\right] \left[\delta^{jl} - \frac{k_2^j k_2^l}{q^2}\right] N(p-k_1) N(q-k_2),$$

where $|in\rangle$ is the wave function of the incoming projectile, *C* is a constant, N(p-k) is the probability that the incoming gluon with transverse momentum *k* acquires transverse momentum *p* after scattering and, hereafter, we use the notation $\int_k \equiv \int \frac{d^2k}{(2\pi)^2}$. This scattering probability is of course determined by the distribution of target fields (within the glasma graph calculation, the scattering of the two gluons is independent). We have also assumed that the target wave function is translationally invariant, so that the momentum transfer is the same to the gluon in the amplitude and complex conjugate amplitude. The last assumption does not allow one to discuss the correlation mechanisms proposed in [8, 9] within this framework.

Also note that we have not indicated the rapidity variable on the gluon creation and annihilation operators. Within the glasma graph calculation the gluon production is rapidity independent. Rapidity dependence becomes significant only when the rapidity difference between the observed hadrons becomes large, $\Delta \eta \sim 1/\alpha_s$. The origin of this independence is that the CGC hadronic wave function is approximately boost-invariant. In fact, only the rapidity independent mode of the gluon field is large in the wave function of the fast hadron, and only the creation operators of this one rapidity mode are relevant to the discussion of correlations.

Thus, the creation and annihilation operators entering the above equation are the original gluon operators integrated over rapidity,

$$a_{a}^{i}(k) \equiv \frac{1}{\sqrt{Y}} \int_{|\eta < Y/2|} \frac{d\eta}{2\pi} a_{a}^{i}(\eta, k).$$
(2.8)

Here the rapidity interval Y/2 is arbitrary, but large enough to contain the rapidities of both observed gluons. The operators defined this way satisfy the standard commutation relations in the transverse momentum space:

$$[a_a^i(k), a_b^{\dagger j}(p)] = (2\pi)^2 \delta_{ab} \delta^{ij} \delta^{(2)}(k-p).$$
(2.9)

The integral over momenta k_1, k_2 in eq. (2.8) contains a contribution from the region $k_1 = k_2$. If the wave function $|in\rangle$ exhibits Bose enhancement, there is enhanced probability that the two gluons

have equal momenta. This excess in the initial state will then translate into final state correlations. Note that this effect is suppressed by the squared number of colors $1/N_c^2$, since Bose enhancement is only operational for bosons with identical quantum numbers.

We thus have to understand what is the nature of the projectile state $|in\rangle$, and in particular we need to calculate

$$D(k_1, k_2) \equiv \langle in | a_a^{\dagger i}(k_1) a_b^{\dagger j}(k_2) a_a^k(k_1) a_b^l(k_2) | in \rangle.$$
(2.10)

Averaging over the projectile state in the standard CGC approach involves two elements. One needs to calculate the average over the soft degrees of freedom, as well as that over the valence color charge density. Conventionally this is done in the spirit of the Born-Oppenheimer approximation, namely first one averages over the soft gluon degrees of freedom at fixed valence color charge density ρ , and subsequently averages over the valence density distribution.

The wave function of the soft fields for fixed valence color charge density for a dilute projectile is a simple coherent state

$$|in\rangle_{\rho} = \exp\left\{i\int_{k} b_{a}^{i}(k)\left[a_{a}^{\dagger i}(k) + a_{a}^{i}(-k)\right]\right\}|0\rangle, \qquad (2.11)$$

with the Weizsäcker-Williams field $b_a^i(k) = g\rho_a(k)\frac{ik^i}{k^2}$.

The averaging over the soft degrees of freedom leads to the well known expression for the observable in terms of the charge density:

$$D(k_1,k_2)_{\rho} = b_a^i(k_1)b_b^j(k_2)b_a^k(-k_1)b_b^l(-k_2).$$
(2.12)

Since at fixed ρ , the soft gluon state is a coherent state, this expression does not seem to exhibit Bose enhancement. This is however misleading, since averaging over ρ is part of the quantum averaging over the initial state wave function $|in\rangle$. It is therefore instructive to reverse the conventional order of averaging, and average over the valence degrees of freedom first. The result of such a procedure is a density matrix on the soft gluon Hilbert space. The subsequent averaging over this density matrix is a direct way to find out whether the projectile wave function exhibits Bose enhancement.

2.3 The soft gluon density matrix

The soft gluon density matrix of course depends on the weight for the valence color charge density. For illustrative purposes we choose the same Gaussian weight used in the glasma graph calculation, the McLerran-Venugopalan model [16],

$$\langle \cdots \rangle_{\rho} = \mathscr{N} \int D[\rho] \cdots e^{-\int_{k} \frac{1}{2\mu^{2}(k)} \rho_{a}(k) \rho_{a}(-k)},$$
(2.13)

where \mathcal{N} is the normalization factor.

Thus the density matrix of the soft gluons is given by

$$\hat{\rho} = \mathcal{N} \int D[\rho] e^{-\int_{k} \frac{1}{2\mu^{2}(k)} \rho_{a}(k) \rho_{a}(-k)}$$

$$\times e^{i \int_{q} b_{b}^{i}(q) \phi_{b}^{i}(-q)} |0\rangle \langle 0| e^{-i \int_{p} b_{c}^{j}(p) \phi_{c}^{j}(-p)}$$
(2.14)

where we have defined $\phi_a^i(k) = a_a^i(k) + a_a^{\dagger i}(-k)$. The integral over ρ can be performed with the result

$$\hat{\rho} = e^{-\int_{k} \frac{g^{2} \mu^{2}(k)}{2k^{4}} k^{j} \phi_{b}^{j}(k) \phi_{b}^{j}(-k)}}$$

$$\times \left\{ \sum_{n=0}^{+\infty} \frac{1}{n!} \left[\prod_{m=1}^{n} \int_{p_{m}} \frac{g^{2} \mu^{2}(p_{m})}{p_{m}^{4}} p_{m}^{i_{m}} \phi_{a_{m}}^{i_{m}}(p_{m}) \right] |0\rangle$$

$$\times \left\langle 0 | \left[\prod_{m=1}^{n} p_{m}^{j_{m}} \phi_{a_{m}}^{j_{m}}(-p_{m}) \right] \right\}$$

$$\times e^{-\int_{k'} \frac{g^{2} \mu^{2}(k')}{2k'^{4}} k'^{j'} \phi_{c}^{j'}(k') \phi_{c}^{j'}(-k')}.$$
(2.15)

The interesting correlator is given by

=

$$D(k_1, k_2) = tr[\hat{\rho} a_a^{\dagger i}(k_1) a_b^{\dagger j}(k_2) a_a^k(k_1) a_b^l(k_2)].$$
(2.16)

It is a matter of straightforward algebra to show that

$$tr[\hat{\rho}a_{a}^{\dagger i}(k)a_{b}^{j}(p)] = (2\pi)^{2}\delta_{ab}\,\delta^{(2)}(k-p)\,g^{2}\mu^{2}(p)\,\frac{p^{i}p^{j}}{p^{4}},$$

$$tr[\hat{\rho}a_{a}^{i}(k)a_{b}^{j}(p)] = tr[\hat{\rho}a_{a}^{\dagger i}(k)a_{b}^{\dagger j}(p)]$$

$$= -(2\pi)^{2}\delta_{ab}\,\delta^{(2)}(k+p)\,g^{2}\mu^{2}(p)\,\frac{p^{i}p^{j}}{p^{4}}$$
(2.17)

and then find

$$D(k_1, k_2) = S^2 (N_c^2 - 1)^2 \frac{k_1^i k_1^k k_2^j k_2^l}{k_1^2 k_2^2} \frac{g^4 \mu^2(k_1) \mu^2(k_2)}{k_1^2 k_2^2}$$

$$\times \left\{ 1 + \frac{1}{S(N_c^2 - 1)} \left[\delta^{(2)}(k_1 - k_2) + \delta^{(2)}(k_1 + k_2) \right] \right\}.$$
(2.18)

In order to get eq. (2.18), we have made substitutions of the type $(2\pi)^2 \delta^{(2)}(k_1 - k_1) \rightarrow S$, where *S* is the transverse area of the projectile. This regularization amounts to taking into account the discreteness of the transverse momentum spectrum of confined gluons.

3. Discussion

The first term in eq. (2.18) is the "classical" term equal to the square of the number of particles. The second term is the typical Bose enhancement term, suppressed with respect to the first "classical"' term by the total number of degrees of freedom (color and area). The third term is specific to the density matrix at hand and, as explained in [8], appears due to reality of the gluon field scattering amplitude. This establishes our point that the soft glue density matrix exhibits Bose enhancement, so that the likelihood of finding two gluons with the same transverse momentum is higher than average. Note that this effect is naturally subleading in N_c as the enhancement is only effective if both gluons are in the same color state.

As a typical Bose enhancement contribution, the second term in eq. (2.18) is nonvanishing only when the momenta of the two gluons are equal. Note however that k_1 and k_2 are *not* the

momenta of observed gluons, but rather the momenta of gluons in the wave function of the incoming projectile. The two gluons then scatter on the target and acquire momenta p and q with the probability $N(p-k_1)N(q-k_2)$, as indicated in eq. (2.8). Nevertheless it is clear that in favorable kinematics the initial state correlation of eq. (2.18) also appears as a correlation between the final state particles. Consider for example a situation where the incoming projectile wave function has an intrinsic saturation momentum Q_s , and the momenta p and q are chosen to be of the same order as Q_s i.e. $p^2 \sim q^2 \sim Q_s^2$. In such a situation the production amplitude is dominated by the contribution from $|k_1|, |k_2| \sim Q_s$, since the gluon density of the projectile is dominated by those gluons close to saturation momentum. The delta function in the Bose enhancement term in eq. (2.18) is then smeared when convoluted with the scattering probability $N(p-k_1)N(q-k_2)$, but positive angular correlations between the directions of \vec{p} and \vec{q} clearly survive. Thus the initial correlation is transmitted to the final state, provided fragmentation and final state effects in p-p and p-A collisions are small. On the other hand, when $|p|, |q| \gg Q_s$, the initial correlation is smeared out by the large momentum transfer from the target, and the correlation in the final state should disappear. These qualitative features are of course borne out by the numerical calculations of [11].

One interesting question naturally follows on from the above discussion. Fermions in the initial state wave function surely experience Pauli blocking. One therefore may expect negative correlation between final state hadrons that originate from quarks or antiquarks in the initial state. Such correlation should exhibit anticollimation rather than collimation, and therefore a valley rather than a ridge at $\Delta \phi = 0$. Whether such a valley extends to large relative rapidities between the observed particles is a question that should be explored. Quark-antiquark pairs are present in the hadronic wave function within the CGC approach at the next to leading order in α_s via splitting of gluons. Since the gluonic wave function is boost invariant, the same is true for the quark and antiquark distribution. However, the main question here is whether the fluctuations around some "mean field" are not too large to mask the correlations in rapidity event by event. Another way of saying it, is to recall that in our discussion of gluons only a single rapidity independent mode of the quantum gluon field was large in the CGC wave function. As a result any correlation extended over large intervals in rapidity. Whether a similar effect dominates the quark wave function has to be investigated. Work on these questions is ongoing [17].

Perhaps an even more pressing question to understand is whether such valleys can be observed experimentally, given that the quark contribution is suppressed by α_s relative to that of gluons. Here we see two possible avenues. One point is that, as opposed to gluon contribution to correlations, the quark contribution is not symmetric under $\Delta \phi \rightarrow -\Delta \phi$. It thus can generate a nonvanishing v_3 coefficient within the CGC approach. Such mechanism will be quite different from the one explored in [18] based on the idea of local anisotropy suggested in [8]. Another possibility is to trigger on final states which predominantly arise from quarks. For example it may be interesting to study correlations between two D-mesons (or B-mesons), since open charm (or beauty) should have a relatively larger component coming from fragmentation of quarks, rather than that of gluons [17].

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