

# Measurements of the top quark mass from the LHC and the Tevatron

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The mass of the top quark is a fundamental parameter of the standard model and has to be determined experimentally. In these proceedings, I review recent measurements of the top quark mass in  $pp$  collisions at  $\sqrt{s} = 7, 8, \text{ and } 13$  TeV recorded by the ATLAS and CMS detectors at the LHC, and in  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96$  TeV recorded by the CDF and D0 experiments at the Tevatron. The measurements are performed in final states containing two, one, and no charged leptons. A relative precision of down to 0.3% is attained. In addition, recent measurements aiming to determine the top quark mass in the well-defined pole scheme using both inclusive  $t\bar{t}$  and  $t\bar{t} + 1$  jet production are presented.

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## 1. Introduction

Since its discovery [1, 2], the determination of the top quark mass  $m_t$ , a fundamental parameter of the standard model (SM), has been one of the main goals of the CERN Large Hadron Collider (LHC) and of the Fermilab Tevatron Collider. Indeed,  $m_t$  and masses of  $W$  and Higgs bosons are related through radiative corrections that provide a consistency check of the SM [3, 4]. Furthermore,  $m_t$  dominantly affects the stability of the SM Higgs potential [4, 5]. With  $m_t = 173.34 \pm 0.76$  GeV, a world-average combined precision of 0.44% has been achieved [6].

In the SM, the top quark decays to a  $W$  boson and a  $b$  quark nearly 100% of the time. Thus,  $t\bar{t}$  events are classified according to  $W$  boson decays as “dileptonic” ( $\ell\ell$ ), “lepton+jets” ( $\ell$ +jets), or “all-jets”. Single top production contributes significantly at the LHC through the  $qg \rightarrow q't\bar{b}$  process. In the following, I will present representative measurements in the three channels; a full listing of  $m_t$  results from the LHC and the Tevatron can be accessed through Refs. [7, 8, 9, 10].

## 2. Standard measurements of the top quark mass

The most precise single measurement of  $m_t$  in the  $\ell\ell$  channel is performed by the ATLAS Collaboration using  $20.2 \text{ fb}^{-1}$  of  $pp$  collisions at  $\sqrt{s} = 8$  TeV [11]. The selection requires two isolated leptons ( $e$  or  $\mu$ ) of opposite charge, missing transverse momentum  $E_T^{\text{miss}}$  due to neutrinos, and  $\geq 2$  jets, where at least one of which is identified as originating from a  $b$  quark ( $b$ -tagged). A transverse momentum  $p_{T,lb} > 120$  GeV is required for the average of the two  $lb$  systems to reduce the dominant uncertainty from the jet energy scale (JES). The  $m_t$  is extracted with the “template method”, which in this case fits the distribution in the average invariant mass of the  $lb$  system to the expectations from Monte Carlo (MC) simulations for different  $m_t$ , shown in Fig. 1 (a). The best fit to data is shown in Fig. 1 (b), and results in  $m_t = 172.99 \pm 0.41$  (stat)  $\pm 0.74$  (syst) GeV. Tevatron’s most precise single measurement in the  $\ell\ell$  channel of  $m_t = 173.32 \pm 1.36$  (stat)  $\pm 0.85$  (syst) GeV is performed by the D0 Collaboration using  $9.7 \text{ fb}^{-1}$  of  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96$  TeV [12].

The most precise single measurement of  $m_t$  from the Tevatron is performed by the D0 Collaboration using  $9.7 \text{ fb}^{-1}$  of data in the  $\ell$ +jets channel [13] with a “matrix element (ME) method”. This approach determines the probability of observing a given event under both the  $t\bar{t}$  signal and

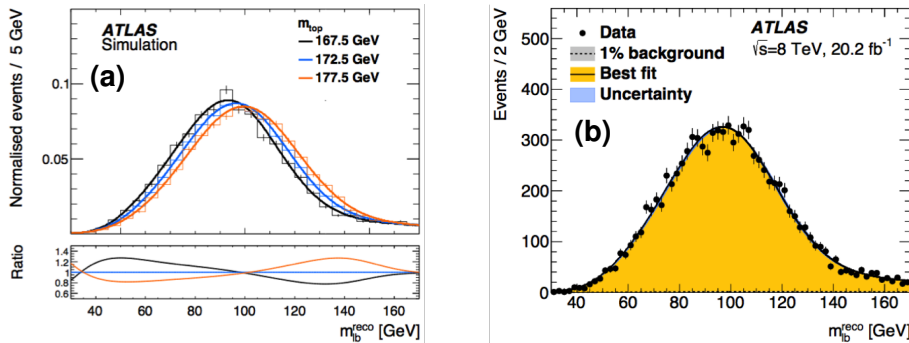


Figure 1: (a) Expected dependence of the  $m_{lb}$  distribution of processes involving top quarks on  $m_t$  from Monte Carlo simulations at  $\sqrt{s} = 8$  TeV with the ATLAS detector [11]. (b) The distribution in  $m_{lb}$  in  $20.3 \text{ fb}^{-1}$  of data at  $\sqrt{s} = 8$  TeV with the ATLAS detector. The predictions correspond to the best-fit values.

background hypotheses, as a function of  $m_t$ . This probability is calculated *ab initio* using the respective MEs of the  $t\bar{t}$  signal and dominant  $W$ +jets background, taking into account effects from parton showering (PS), hadronisation, and finite detector resolution. This selection requires the presence of one isolated lepton,  $E_T^{\text{miss}}$ , and exactly four jets with at least one  $b$ -tag. A new JES calibration from exclusive  $\gamma$ +jet,  $Z$ +jet, and dijet events is applied to account for differences in detector response to jets originating from a gluon, a  $b$  quark, and  $u, d, s$ , or  $c$  quarks. The overall JES  $k_{\text{JES}}$  is calibrated *in situ* by constraining the reconstructed invariant mass of the hadronically decaying  $W$  boson to  $M_W = 80.4$  GeV. The likelihood over all candidate events is maximised in  $(m_t, k_{\text{JES}})$  as shown in Fig. 2 (a), and  $m_t = 174.98 \pm 0.58(\text{stat}+\text{JES}) \pm 0.49(\text{syst})$  GeV is obtained. The most precise  $m_t$  result from the CDF Collaboration in the  $\ell$ +jets channel of  $m_t = 172.85 \pm 0.71(\text{stat}+\text{JES}) \pm 0.85(\text{syst})$  GeV [14] is obtained with the template method.

The most precise single measurement of  $m_t$  from the LHC is performed by the CMS Collaboration using  $19.7 \text{ fb}^{-1}$  of data at  $\sqrt{s} = 8$  TeV in the  $\ell$ +jets channel [15]. The analysis uses a similar selection to the D0 result and applies the “ideogram method” to extract  $m_t$ . Similar to the ME method, this approach calculates the probability to observe a given event as a function of  $(m_t, k_{\text{JES}})$ . However, this probability is not calculated *ab initio*, but is obtained from MC simulations, in analogy to the template method. The final result of  $m_t = 172.35 \pm 0.16(\text{stat}+\text{JES}) \pm 0.48(\text{syst})$  GeV is represented in Fig. 2 (b). The most precise  $m_t$  result from the ATLAS Collaboration is obtained with the template method using  $4.7 \text{ fb}^{-1}$  of data at  $\sqrt{s} = 7$  TeV and reads  $m_t = 172.33 \pm 0.75(\text{stat}+\text{JES}) \pm 1.02(\text{syst})$  GeV [16].

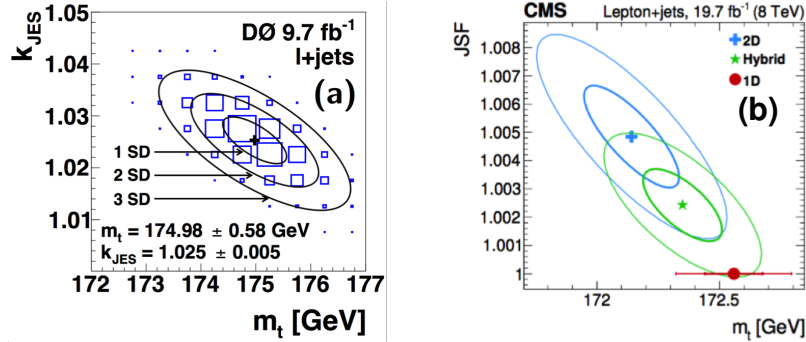


Figure 2: (a) The likelihood in  $(m_t, k_{\text{JES}})$  in  $9.7 \text{ fb}^{-1}$  of  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96$  TeV recorded with the D0 detector [13]. Fitted contours of equal probability are overlaid as solid lines. The maximum is marked with a cross. (b) Same as (a), but in  $19.5 \text{ fb}^{-1}$  of  $pp$  collisions at  $\sqrt{s} = 8$  TeV recorded with the CMS detector [15]. The central result corresponds to “Hybrid”, and  $k_{\text{JES}}$  is denoted as “JSF”.

The all-jets channel is particularly challenging due to very high background from QCD multijets. Tevatron’s most precise single  $m_t$  result in this channel comes from the CDF Collaboration using  $9.3 \text{ fb}^{-1}$  of data [17]. A neural network and  $b$ -tagging enhance the signal-to-background ratio from  $10^{-3}$  to about 1. The correct assignment of jets to partons is determined by minimising a  $\chi^2$ , which accounts for consistency of the two dijet systems with  $m_W$ , consistency of the two  $jjb$  systems with each other, and consistency of the individual fitted jet momenta with measured ones, within experimental resolutions. The measured value is  $m_t = 175.07 \pm 1.19(\text{stat}+\text{JES}) \pm 1.55(\text{syst})$  GeV. The most precise result in the all-jets channel at the LHC of  $m_t = 172.32 \pm 0.25(\text{stat}+\text{JES}) \pm 0.59(\text{syst})$  GeV comes from the CMS Collaboration [15].

An overview of recent  $m_t$  measurements at the LHC [18] is given in Fig. 3. A combination of  $m_t$  measurements from Run I and II of the Tevatron considering statistical and systematic correlations yields  $m_t = 174.30 \pm 0.35(\text{stat}) \pm 0.34(\text{syst})$  GeV [19].

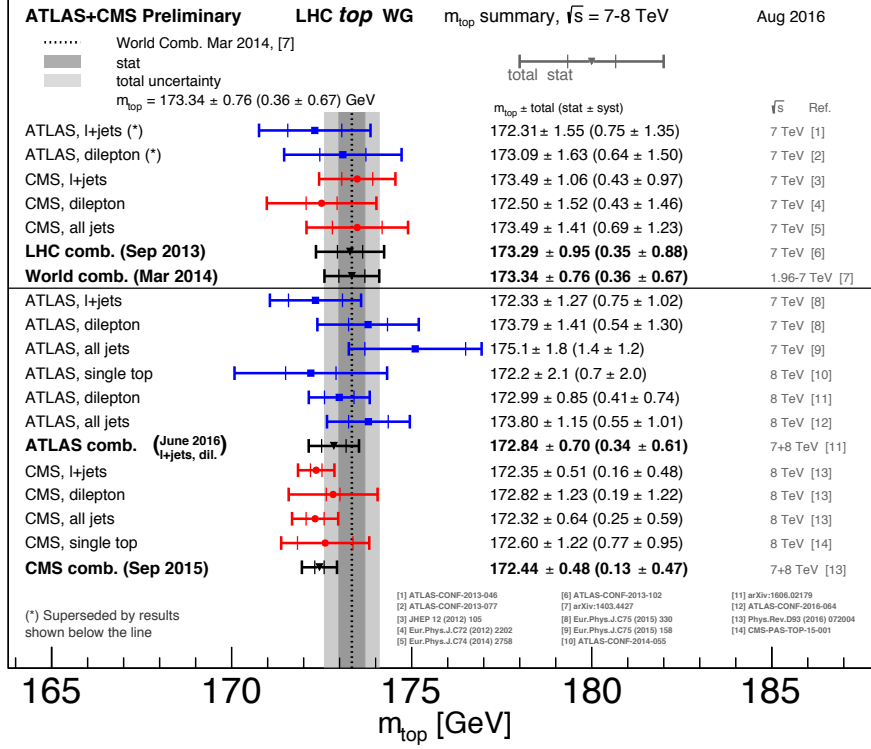


Figure 3: Overview of recent  $m_t$  measurements at the LHC [18]. References to the individual measurements are given at the bottom of the Figure.

### 3. Measurements of the top quark mass in the pole scheme

The *standard* measurements of  $m_t$  from Sect. 2 are experimentally the most precise ones. However, they extract an  $m_t$  parameter as implemented in MC generators, which is related to the pole mass scheme definition  $m_t^{\text{pole}}$  in the SM Lagrangian within an uncertainty of  $\leq 1$  GeV [20].

The first LHC result on  $m_t$  at  $\sqrt{s} = 13$  TeV is an extraction of  $m_t^{\text{pole}}$  from  $\sigma_{t\bar{t}}$  performed by CMS in the  $\ell$ +jets channel using  $2.3 \text{ fb}^{-1}$  of data [21]. This analysis exploits the dependence of  $\sigma_{t\bar{t}}$  on  $m_t^{\text{pole}}$ , which is now known with  $\approx 3\%$  precision at NNLO with NNLL corrections [22]. The input measurement of  $\sigma_{t\bar{t}}$  achieves a relative uncertainty of  $\approx 4\%$  by constraining the dominant  $W$ +jets background through sidebands in low jet and  $b$ -tag multiplicities, and using the difference in  $d\sigma/dm_{\ell b}$  dependence between signal and background. The final result is  $m_t^{\text{pole}} = 173.3^{+2.3}_{-2.0}(\text{stat} + \text{syst})^{+1.6}_{-1.1}(\text{theo})$  GeV.

The most precise  $m_t^{\text{pole}}$  measurement is performed by the ATLAS Collaboration in the  $\ell$ +jets channel using  $4.6 \text{ fb}^{-1}$  of data at  $\sqrt{s} = 7$  TeV [23]. The  $m_t^{\text{pole}}$  is extracted from the production cross section of a  $t\bar{t}$  system in association with a jet  $\sigma_{t\bar{t}+1 \text{ jet}}$ , since the radiation rate of a high- $p_T$  gluon off the  $t\bar{t}$  system is proportional to  $m_t^{\text{pole}}$ . More precisely, the differential production

cross section  $\mathcal{R}(m_t^{\text{pole}}, \rho_s) \equiv 1/\sigma_{t\bar{t}+1\text{jet}} \cdot d\sigma_{t\bar{t}+1\text{jet}}/d\rho_s$  is compared to NLO calculations [24], where  $\rho_s \equiv 2m_0/\sqrt{s_{t\bar{t}+1\text{jet}}}$ , and the arbitrary constant  $m_0$  is set to 170 GeV in this analysis. The selection is similar to other analyses in the  $\ell$ +jets channel discussed in Sect. 2, and the correct jet-parton assignment is determined through a  $\chi^2$  kinematic fit. To reduce the total uncertainty,  $p_T > 50$  GeV is required for the extra jet. The distribution in  $\rho_s$  is corrected for detector, PS, hadronisation effects, and the presence of background. The resulting distribution at parton level is given in Fig. 4 (a). The final result reads  $m_t^{\text{pole}} = 173.1 \pm 1.50(\text{stat}) \pm 1.43(\text{syst})_{-0.49}^{+0.93}(\text{theo})$  GeV.

The second most precise  $m_t^{\text{pole}}$  measurement is performed by the D0 Collaboration in the  $\ell$ +jets channel using  $9.7 \text{ fb}^{-1}$  of data [25]. This analysis extracts  $m_t^{\text{pole}}$  by relating measured  $d\sigma_{t\bar{t}}/dm_{t\bar{t}}(m_t)$  and  $d\sigma_{t\bar{t}}/dp_{T,t/\bar{t}}(m_t)$  to recent NNLO and NLO calculations [26]. *Differential* cross sections allow for a more complete use of kinematic information, and thus a notably higher statistical precision than the  $m_t^{\text{pole}}$  extraction from an inclusive  $\sigma_{t\bar{t}}$  measurement. The selection is similar to Ref. [13], and the correct jet-parton assignment is identified through a  $\chi^2$  kinematic fit. The resulting distributions are corrected for detector, PS, hadronisation effects, and the presence of background to obtain  $d\sigma_{t\bar{t}}/dm_{t\bar{t}}(m_t)$  and  $d\sigma_{t\bar{t}}/dp_{T,t/\bar{t}}(m_t)$ , which are then directly compared to theory calculations to extract  $m_t^{\text{pole}}$ . The final result reads  $m_t^{\text{pole}} = 169.1 \pm 2.5(\text{stat} + \text{syst}) \pm 1.5(\text{theo})$  GeV.

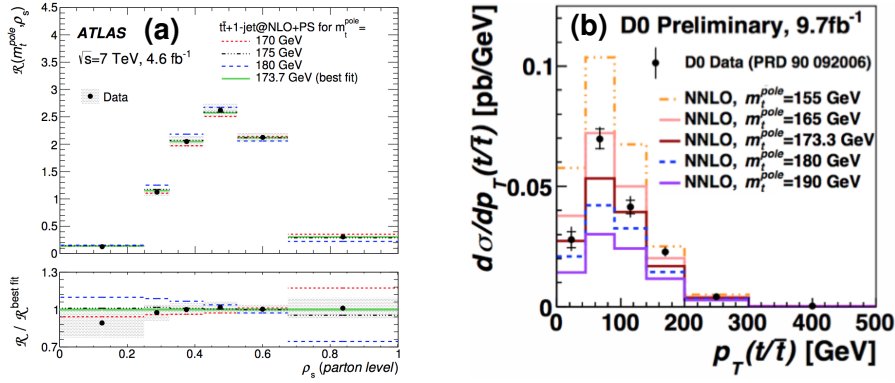


Figure 4: (a) The distribution  $\mathcal{R} \equiv 1/\sigma_{t\bar{t}+1\text{jet}} \cdot d\sigma_{t\bar{t}+1\text{jet}}/d\rho_s$  in  $pp$  collisions at  $\sqrt{s} = 7$  TeV with the ATLAS detector [23], compared to NLO predictions [24]. (b) The distribution of  $d\sigma_{t\bar{t}}/dp_{T,t/\bar{t}}(m_t)$  in  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96$  TeV with the D0 detector [25], compared to NNLO predictions [26]. Both distributions are shown at parton level, after corrections for detector, PS, and hadronisation effects.

## 4. Conclusions

I presented recent measurements of the top quark mass, a fundamental parameter of the SM. The most precise single measurements at the LHC and the Tevatron of respectively  $m_t = 172.35 \pm 0.16(\text{stat}+\text{JES}) \pm 0.48(\text{syst})$  GeV and  $m_t = 174.98 \pm 0.58(\text{stat}+\text{JES}) \pm 0.49(\text{syst})$  GeV are performed by the CMS and D0 Collaborations in the  $\ell$ +jets channel, corresponding to a relative precision of 0.30% and 0.43%. The precision of  $m_t$  measurements in the pole scheme is improved to 1.3% due to the advent of new theory calculations and experimental approaches.

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## References

- [1] S. Abachi *et al.* (D0 Coll.), Phys. Rev. Lett. **74** (1995) 2632.
- [2] F. Abe *et al.* (CDF Coll.), Phys. Rev. Lett. **74** (1995) 2626.
- [3] The ALEPH, CDF, D0, DELPHI, L3, OPAL, SLC Coll., [arXiv:1012.2367 \[hep-ex\]](https://arxiv.org/abs/1012.2367) (2010).
- [4] Rohini Godbole, these proceedings.
- [5] G. Degrossi *et al.*, J. High Energy Phys. **08** (2012) 098; F. Bezrukov *et al.*, Phys. Lett. B **659** (2008) 703; A. De Simone *et al.*, Phys. Lett. B **678** (2009) 1.
- [6] ATLAS, CDF, CMS, and D0 Coll., [arXiv:1403.4427 \[hep-ex\]](https://arxiv.org/abs/1403.4427) (2014).
- [7] <https://twiki.cern.ch/twiki/bin/view/AtlasPublic/TopPublicResults>.
- [8] [https://www-cdf.fnal.gov/physics/new/top/public\\_mass.html](https://www-cdf.fnal.gov/physics/new/top/public_mass.html).
- [9] <https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsTOP>.
- [10] [https://www-d0.fnal.gov/Run2Physics/top/top\\_public\\_web\\_pages/top\\_public.html#mass](https://www-d0.fnal.gov/Run2Physics/top/top_public_web_pages/top_public.html#mass).
- [11] ATLAS Coll., Phys. Lett. B **761** (2016) 350.
- [12] D0 Coll., Phys. Lett. B **752** (2016) 18.
- [13] D0 Coll., Phys. Rev. Lett. **113** (2014) 032002.
- [14] CDF Coll., Phys. Rev. Lett. **113** (2014) 032002.
- [15] CMS Coll., Phys. Rev. D **93** (2016) 072004.
- [16] ATLAS Coll., Eur. Phys. J. C **75** (2015), 330.
- [17] CDF Coll., Phys. Rev. D **90** (2014) 091101.
- [18] ATLAS and CMS Coll., [https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/CombinedSummaryPlots/TOP/mtopSummary\\_TopLHC/history.html](https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/CombinedSummaryPlots/TOP/mtopSummary_TopLHC/history.html)
- [19] CDF and D0 Coll., [arXiv:1608.01881 \[hep-ex\]](https://arxiv.org/abs/1608.01881).
- [20] A. H. Hoang and I. W. Stewart, Nucl. Phys. Proc. Suppl. **185** (2008) 220.
- [21] CMS Coll., [CMS-PAS-TOP-16-006](https://arxiv.org/abs/1606.006) (2016).
- [22] M. Czakon *et al.*, Phys. Rev. Lett. **110** (2013) 252004.
- [23] ATLAS Coll., J. of High Energy Phys. **10** (2015) 121.
- [24] S. Alioli *et al.*, Eur. Phys. J. C **73** (2013) 2438.
- [25] D0 Coll., [D0 CONF Note 6473](https://arxiv.org/abs/1606.006) (2016).
- [26] M. Czakon, P. Fiedler, D. Heymes and A. Mitov, J. of High Energy Phys. **05** (2016) 034.