

Comparison of γ production data from thermal neutron capture on gadolinium with the Monte Carlo simulation

Kaito HAGIWARA*

Department of Physics, Okayama University, Okayama 700-8530, Japan E-mail: k.hagiwara@s.okayama-u.ac.jp

T. TANAKA¹, P. K. DAS¹, T. YANO², Y. YAMADA¹, I. OU¹, T. MORI¹, T. KAYANO¹, M. S. REEN¹, R. DHIR¹, Y. KOSHIO¹, M. SAKUDA¹, A. KIMURA³, S. NAKAMURA³, N. IWAMOTO³ and H. HARADA³

¹Department of Physics, Okayama University, Okayama 700-8530, Japan

²Department of Physics, Kobe University, Kobe Hyogo 657-8501, Japan

³ Japan Atomic Energy Agency, 2-4 Shirakata Shirane, Tokai, Naka, Ibaraki 319-1195, Japan

The γ -ray spectrum produced from the thermal neutron capture on enriched gadolinium targets (¹⁵⁵Gd and ¹⁵⁷Gd) were measured using the ANNRI Germanium Spectrometer at J-PARC. We have also built a γ -ray emission model of ¹⁵⁸Gd decay, in which γ rays were classified into discrete prompt γ rays and continuum spectrum. We compared the data and our model, and found a fair agreement between them at the level of 26% over the γ -ray energy from 0.2 to 8.0 MeV. In this proceedings, the measured spectra and the model are described.

The 3rd International Symposium on "Quest for the Origin of Particles and the Universe" 5-7 January 2017 Nagoya University, Japan

*Speaker.

© Copyright owned by the author(s) under the terms of the Creative Commons Attribution-NonCommercial-NoDerivatives 4.0 International License (CC BY-NC-ND 4.0).

1. Introduction

Gadolinium-157 (¹⁵⁷Gd) has the largest thermal neutron capture cross section among all stable nuclei and Gadolinium-155 (¹⁵⁵Gd) also has large cross section since they have a resonance in the neutron capture in the thermal neutron energy region (26.8 meV for ¹⁵⁵Gd and 31.4 meV for ¹⁵⁷Gd) [1]. The neutron capture reaction Gd(n, γ) is expected to produce about four γ rays, which have the total energy of about 8 MeV. These Gd(n, γ) reactions are described as

$$\begin{split} &n + {}^{155}\,\text{Gd} \to {}^{156}\,\text{Gd}^* \to {}^{156}\,\text{Gd} + \gamma\,\text{rays} \quad (8.5\,\text{MeV in total}), \\ &n + {}^{157}\,\text{Gd} \to {}^{158}\,\text{Gd}^* \to {}^{158}\,\text{Gd} + \gamma\,\text{rays} \quad (7.9\,\text{MeV in total}). \end{split}$$

A new project (SK-Gd) for anti-electron-neutrino detection using Gd-loaded water Cherenkov detector was proposed for the Super-Kamiokande collaboration [2, 3]. In this project, the inverse beta decay reaction ($\bar{v}_e + p \rightarrow e^+ + n$) can be identified by the coincidence of a prompt positron signal and a delayed γ -ray signal from the neutron capture on Gd. The present experiment was performed at the J-PARC in order to measure the γ rays from the Gd(n, γ) reaction at high precision.

2. Experiment

The experiment (2014B0124) was conducted in December, 2014, using the ANNRI detector [4]. The ANNRI detector is located at the Beam Line No.4 (BL04) in the MLF [5]. The BL04 provides a neutron beam from 1 meV to 10 eV. The ANNRI detector is composed of two Ge clusters and BGO counters. A Ge cluster consists of seven hexagonal Ge crystals, each of which measures the energy and the arrival time of γ rays. The BGO counters surround the Ge clusters, which are used as anti-coincidence shields. The details of the detector can be found elsewhere [6].

We used two kinds of enriched gadolinium oxide powder, ${}^{155}\text{Gd}_2\text{O}_3$ and ${}^{157}\text{Gd}_2\text{O}_3$ (Table 1), attached to a target holder. The ANNRI detector was calibrated using γ rays from four radioactive sources (${}^{22}\text{Na}$, ${}^{60}\text{Co}$, ${}^{137}\text{Cs}$, and ${}^{152}\text{Eu}$) and prompt γ rays from ${}^{35}\text{Cl}(n,\gamma)$ reaction. We select events only when at least one Ge crystal has pulse height greater than 100 keV and no surrounding BGO counters have pulse height greater than 100 keV. Table 2 shows the summary of the data sets.

 Table 1: Isotopic composition (%) of the Gd oxide powder used in the experiment.

Target	¹⁵⁴ Gd	¹⁵⁵ Gd	¹⁵⁶ Gd	¹⁵⁷ Gd	¹⁵⁸ Gd	¹⁶⁰ Gd
¹⁵⁵ Gd ₂ O ₃	0.5	91.85	5.87	0.81	0.65	0.27
$^{157}\text{Gd}_2\text{O}_3$	0.05	0.30	1.63	88.4	9.02	0.60

Target	Time	Number of Events	Source	Time	Number of Events			
$^{155}\text{Gd}_2\text{O}_3$	38 hours	3.1×10^{9}	²² Na	5 minutes	$1.5 imes 10^7$			
$^{157}\text{Gd}_2\text{O}_3$	55 hours	4.6×10^{9}	⁶⁰ Co	18 hours	$8.8 imes 10^7$			
NaCl	4 hours	1.3×10^{8}	¹³⁷ Cs	30 minutes	$2.1 imes 10^6$			
Empty	6 hours	1.3×10^{7}	¹⁵² Eu	7 hours	$2.3 imes 10^7$			

Table 2: Data sets taken in the experiment.

Kaito HAGIWARA

We first show the energy spectrum of single γ -ray events in Figure 1. Single γ -ray events are those in which only one Ge crystal is hit in an event. The fraction of single γ -ray events out of the total events is 77%.

3. Modeling γ -ray Emission

We used two Geant4-Based Monte Carlo (MC) simulations for γ -ray emission from Gd(n, γ) reaction. One of them is the standard option of Geant4 [7, 8]. The other is a GLG4sim model [9] which is developed for KamLAND [10].

We have built our model following the GLG4sim scheme, where the γ rays were classified into two parts: discrete prompt γ rays and continuum spectrum. For the prompt γ rays, their photo-peak energies in the range from 5 to 8 MeV and the relative intensities were estimated from our data. We then select events where two Ge crystals are hit. Out of those events, we tag one prompt γ ray and look at the second γ ray (secondary γ ray). The secondary γ rays and their intensities are also estimated and are summarized in Table 3. The relative intensity (%) is normalized by total number of single γ rays. We have found that their intensities are consistent with the already published values within the errors [11]. The sum of intensities of discrete γ rays is 2.9%.

Di	Deletive Intensity (%)				
Prompt γ ray		Seconda	ary γray	Relative Intensity (%)	
7.937	-	-	-	-	0.0023 ± 0.0002
7.857	0.080	-	-	-	0.0097 ± 0.0006
6.960	-	-	-	-	0.0085 ± 0.0005
6.914	0.944	0.080	-	-	0.053 ± 0.03
6.750	1.187	-	-	-	0.51 ± 0.03
	1.107	0.080	-	-	0.51 ± 0.03
6.672	1.187	0.080	-	-	0.068 ± 0.007
	1.004	0.182	0.080	-	0.012 ± 0.002
	1.517	-	-	-	0.052 ± 0.006
6.420	1.438	0.080	-	-	0.058 ± 0.006
	1.256	0.182	0.080	-	0.027 ± 0.004
6.001	-	-	-	-	0.066 ± 0.003
	1.010	0.944	0.080	-	0.20 ± 0.01
5.903	0.875	0.898	0.182	0.080	0.12 ± 0.01
	0.769	1.186	0.080	-	0.11 ± 0.01
	0.676	1.097	0.182	0.080	0.064 ± 0.006
5.784	-	-	-	-	0.083 ± 0.003
5.669	-	-	-	-	0.26 ± 0.01
5.595	-	-	-	-	0.27 ± 0.01
5.543	-	-	-	-	0.099 ± 0.004
5.436	-	-	-	-	0.068 ± 0.003
5.167	-	-	-	-	0.251 ± 0.009

Table 3: Discrete γ -ray energies (MeV) and their relative intensities (%), normalized by the total number of single γ -rays observed in our data.

The continuum spectrum can be described in terms of the nuclear level density (NLD) and a set of photon strength functions (PSF). The transition probability $P(E_a, E_b)$ from the initial energy level E_a to the final energy level E_b , emitting the γ -ray energy E_{γ} (= $E_a - E_b$), can be written using Fermi Golden Rule as

$$P(E_a, E_b)\Delta E_b = \frac{T(E_{\gamma})\rho(E_b)\Delta E_b}{\int_{-a}^{E_a} T(E_{\gamma})\rho(E_b)dE_b}, \text{ with}$$
(3.1)

$$T(E_{\gamma}) = 2\pi E_{\gamma}^3 f(E_{\gamma}, T), \qquad (3.2)$$

where $T(E_{\gamma})$, $f(E_{\gamma},T)$, $\rho(E_b)$ and T are the gamma-ray transmission coefficient, PSF, NLD, and the nuclear temperature, respectively. Electromagnetic decay from the neutron resonances is dominated by dipole transitions. The PSFs for deformed nuclei like Gd are described by the sum of two Lorentzian terms [12]

$$f(E_{\gamma},T) = \sum_{i=1}^{2} \left[\frac{E_{\gamma} \Gamma_i(E_{\gamma},T)}{\left(E_{\gamma}^2 - E_i^2\right)^2 + E_{\gamma}^2 \Gamma_i^2(E_{\gamma},T=0)} + 0.7 \frac{\Gamma_i(E_{\gamma}=0,T)}{E_i^3} \right] \sigma_i \Gamma_i,$$
(3.3)

where E_i , $\Gamma_i(E_{\gamma}, T)$, and σ_i are the parameters of the giant electric dipole resonances which have two components (*i* = 1,2). Here, the γ -ray- and temperature-dependent width is given by

$$\Gamma_i(E_{\gamma},T) = \left[k_0 + \frac{E_{\gamma} - \varepsilon_0^{\gamma}}{E_i - \varepsilon_0^{\gamma}}(1 - k_0)\right] \frac{\Gamma_i}{E_i^2} \left(E_{\gamma}^2 + 4\pi^2 T^2\right),\tag{3.4}$$

and guarantees $\Gamma_i(E,0) = \Gamma_i$. We used the parameters from the database of RIPL-2 [13]; $E_{1,2} = 11.7$ and 14.9 MeV, $\Gamma_{1,2} = 2.6$ and 3.8 MeV, $\sigma_{1,2} = 165$ and 249 mb, $\varepsilon_0^{\gamma} = 4.5$ MeV, and $k_0 = 4.0$. The HFB model was also used for NLD in the database of RIPL-3 [14].

We compared the γ rays generated by the model with our data, as shown in Figure 1. We obtained the fraction of the continuum to be 97.1% and that of the discrete γ rays to be 2.9%. The γ rays below 5 MeV energy region is dominated by the continuum spectrum. We also note that the contribution (red color) of prompt γ rays (including their compton scattering) to the total spectrum is very small, except for the energy region above 5 MeV, as shown in Figure 1.



Figure 1: Energy spectrum of single γ rays from 157 Gd(n, γ) reaction. Shaded histogram stands for data, while colored histograms (red and blue) stand for discrete γ rays and continuum spectrum predicted by our MC model, respectively.

4. Result and Summary

The γ -ray emission model is implemented into our Geant4 detector simulation. Figure 2 shows the comparison between data and three models (Geant4 standard option, GLG4sim model, and our model). Our model agrees with the data within 26%, when data and MC are compared at every 0.5 MeV from 1 MeV to 9 MeV. Compared to GLG4sim model, the agreement of the data and our model in the energy region between 0.2 to 8.0 MeV was improved by a factor of three.



Figure 2: Energy spectrum of single γ rays from ¹⁵⁷Gd(n, γ) reaction. Shaded histogram stands for our data (same as those given in Figure 1), while colored histograms stand for predictions by GLG4sim (dotted blue), Geant4 standard option (dashed green), and our model (dashed red).

The 155 Gd(n, γ) data are also being analyzed [11]. Both 155 Gd and 157 Gd data will be published elsewhere soon. This work is supported by JSPS Grant-in-Aid for Scientific Research on Innovative Areas (Research in a proposed research area) No. 26104006.

References

- [1] S. F. Mughabghab: Atlas of Neutron Resonances (Elsevier, Amsterdam, 2006).
- [2] J. F. Beacom and M. R. Vagins: Phys. Rev. Lett 93 (2004) 171101.
- [3] H. Watanabe et al. (Super-K Collab.): Astropart. Phys. 31 (2009) 320.
- [4] A. Kimura et al.: J. Nucl. Sci. Technol. 49 [7] (2012) 708.
- [5] Y. K. M. Igasira and M. Oshima: Nucl. Instrum. Methods Phys. Res. A 600 (2009) 332.
- [6] I.Ou et al. AIP Conference Proceedings 1594, 351 (2014); doi: 10.1063/1.4874094.
- [7] S. Agostinelli et al.: Nucl. Instrum. Methods Phys. Res. A 506 (2003) 250.
- [8] Geant4 Physics Reference Manual: <http://geant4.cern.ch/G4UsersDocuments/UsersGuides/ PhysicsReferenceManual/html/PhysicsReferenceManual.html>.
- [9] GLG4sim page: <http://neutrino.phys.ksu.edu/~GLG4sim/>.
- [10] K. Eguchi et al.: Phys. Rev. Lett. 90 (2003) 021802.
- [11] P. K. Das et al.: In this proceedings.
- [12] J. Kopecky, M. Uhl and R. E. Chrien: Phys. Rev. C 47 (1993) 312.
- [13] T. Belgya et al.: IAEA-TECDOC-1506.
- [14] R. Capote et al.: Nucl. Data Sheets 110 (2009) 3107.