



On neutrino production of a charmed meson

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We calculate in the framework of the collinear QCD approach the amplitude for exclusive neutrino-production of a pseudoscalar charmed D meson. This process allows to access gluon and both chiral-odd and chiral-even quark generalized parton distributions (GPDs), which contribute in specific ways to the amplitude for different polarization states of the W boson. The energy dependence of the cross section allows to separate different contributions and the measurement of the azimuthal dependence helps to single out the transversity chiral-odd GPDs contributions. The flavor dependence, and in particular the difference between D^+ and D^0 production rates, allows to test the importance of gluonic contributions. The behaviour of the proton and neutron target cross sections enables to separate the u and d quark contributions. Planned medium and high energy neutrino facilities will thus allow some important progress in the realm of hadronic physics.

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Figure 1: Feynman diagrams for the factorized amplitude for the $v_l N \rightarrow l^- D^+ N'$ or the $v_l N \rightarrow l^- D^0 N'$ process involving the quark GPDs (left panel) or the gluon GPDs (right panel); the thick line represents the heavy quark.

Neutrino production is an interesting way to access (generalized) parton distributions [1, 2] since they allow to scrutinize the flavor content of the nucleon. In Ref.[3] we calculate the exclusive production of a pseudoscalar charmed D-meson in the scattering of a neutrino on a proton or a neutron target, in the kinematical domain where collinear factorization leads to a description of the scattering amplitude in terms of nucleon GPDs and the D-meson distribution amplitude (DA). The hard subprocesses at work are:

$$W^+d \to D^+d$$
 , $W^+d \to D^0u$, (1)

described by the handbag Feynman diagrams of the left panel of Fig. 1 convoluted with chiral-even or chiral-odd quark GPDs, and the hard subprocesses shown on the right panel of Fig. 1:

$$W^+g \to D^+g \,, \tag{2}$$

convoluted with gluon GPDs.

The new feature of charmed meson neutrino production is the non-zero contribution to the transverse amplitude of chiral-odd GPDs through the quark mass effects in the coefficient function [4] and the meson mass effect in the DA, which is defined as

$$\langle D^{+}(P_{D})|\bar{c}_{\beta}(y)d_{\gamma}(-y)|0\rangle = i\frac{f_{D}}{4}\int_{0}^{1}dz e^{i(z-\bar{z})P_{D}.y}[(\hat{P}_{D}-M_{D})\gamma^{5}]_{\gamma\beta}\phi_{D}(z),$$
(3)

with $z = \frac{k^+}{P_D^+}$ and where $\int_0^1 dz \ \phi_D(z) = 1$, $f_D = 0.223$ GeV. As usual, we denote $\bar{z} = 1 - z$ and $\hat{p} = p_{\mu} \gamma^{\mu}$ for any vector p; $\phi_D(z)$ is peaked around $z_0 = \frac{m_c}{M_D}$. The transverse amplitude reads $(\tau = 1 - i2)$:

$$T_T = \frac{-i2C_q\xi(2M_D - m_c)}{\sqrt{2}(Q^2 + M_D^2)}\bar{N}(p_2) \left[\mathscr{H}_T i\sigma^{n\tau} + \tilde{\mathscr{H}}_T \frac{\Delta^{\tau}}{m_N^2} + \mathscr{E}_T \frac{\hat{n}\Delta^{\tau} + 2\xi\gamma^{\tau}}{2m_N} - \tilde{\mathscr{E}}_T \frac{\gamma^{\tau}}{m_N}\right]N(p_1), \quad (4)$$

with $C_q = \frac{2\pi}{3} C_F \alpha_s V_{dc}$, in terms of transverse form factors that we define as :

$$\mathscr{F}_T = f_D \int \frac{\phi_D(z)dz}{\bar{z}} \int \frac{F_T^d(x,\xi,t)dx}{(x-\xi+\beta\xi+i\varepsilon)(x-\xi+\alpha\bar{z}+i\varepsilon)},\tag{5}$$

where F_T^d is any d-quark transversity GPD, $\alpha = \frac{2\xi M_D^2}{Q^2 + M_D^2}$, $\beta = \frac{2(M_D^2 - m_c^2)}{Q^2 + M_D^2}$.





Figure 2: The Q^2 dependence of the longitudinal (left panel) and transverse (right panel) contributions to the cross section $\frac{d\sigma(vn \rightarrow l^- pD^0)}{dy dQ^2 dt}$ (in pb GeV⁻⁴) for $y = 0.7, \Delta_T = 0$ and s = 20 GeV². The band corresponds to three plausible models [3] for the transversity GPDs.

The differential cross section for neutrino production of a pseudoscalar charmed boson is written as:

$$\frac{d^{4}\sigma(vN \to l^{-}N'D)}{dydQ^{2}dt\,d\varphi} =$$

$$\bar{\Gamma}\Big\{\frac{1+\sqrt{1-\varepsilon^{2}}}{2}\sigma_{--}+\varepsilon\sigma_{00}+\sqrt{\varepsilon}(\sqrt{1+\varepsilon}+\sqrt{1-\varepsilon})(\cos\varphi\operatorname{Re}\sigma_{-0}+\sin\varphi\operatorname{Im}\sigma_{-0})\Big\},$$
(6)

with $y = \frac{p \cdot q}{p \cdot k}$, $Q^2 = x_B y(s - m^2)$, $\varepsilon \approx \frac{1 - y}{1 - y + y^2/2}$ and $\overline{\Gamma} = \frac{G_F^2}{(2\pi)^4} \frac{1}{32y} \frac{1}{\sqrt{1 + 4x_B^2 m_N^2/Q^2}} \frac{1}{(s - m_N^2)^2} \frac{Q^2}{1 - \varepsilon}$, where the "cross-sections" $\sigma_{lm} = \varepsilon_l^{*\mu} W_{\mu\nu} \varepsilon_m^{\nu}$ are product of amplitudes for the process $W(\varepsilon_l) N \to DN'$, averaged (summed) over the initial (final) hadron polarizations. Integrating over φ yields the differential cross section :

$$\frac{d\sigma(\nu N \to l^- N'D)}{dy dQ^2 dt} = 2\pi \bar{\Gamma} \Big\{ \frac{1 + \sqrt{1 - \varepsilon^2}}{2} \sigma_{--} + \varepsilon \sigma_{00} \Big\}.$$
(7)

Gluon GPDs do not contribute to D^0 production since the flavor of the baryon is changed in this reaction. We show on Fig. 2 the longitudinal and transverse contributions to the cross section. The transverse contribution is noteworthy of the same order of magnitude as the longitudinal one and even dominates for *y* large enough. Accessing the chiral-odd transversity GPDs indeed seems feasible in this reaction.

 D^+ neutrino-production allows both quark and gluon GPDs to contribute. Neglecting the strange content of nucleons leads to selecting *d* quarks in the nucleon, thus accessing the *d* (resp. *u*) quark GPDs in the proton for the scattering on a proton (resp. neutron) target, after using isospin relation between the proton and neutron. The transverse contribution is plotted in Fig. 3 as a function of Q^2 for y = 0.7 and $\Delta_T = 0$. The cross section is reasonably flat in *y* and Q^2 so that an integration over the regions 0.45 < y < 1 and $0.5 < Q^2 < 3$ GeV² does not require much care.

The longitudinal cross sections dominate the transverse ones, mostly because of the larger values of the chiral-even GPDs, and specifically of the gluonic ones. The relative importance of quark and gluon contributions to the longitudinal cross sections is shown in Fig. 4 as a function of Q^2 for a specific set of kinematical variables. The y dependence may help to disentangle the longitudinal and transverse contributions since the longitudinal cross section vanishes as $y \rightarrow 1$ as is obvious from Eq. (6).



Figure 3: The Q^2 dependence of the transverse contribution to the cross section $\frac{d\sigma(vN \rightarrow l^-ND^+)}{dy dQ^2 dt}$ (in pb GeV⁻⁴) for $y = 0.7, \Delta_T = 0$ and s = 20 GeV² for a proton (dashed curve and lower band) and neutron (solid curve and upper band) target. The bands correspond to three plausible models [3] for the transversity GPDs.



Figure 4: The Q^2 dependence of the quark (dashed curve) contribution compared to the total (quark and gluon, solid curve) longitudinal cross section $\frac{d\sigma(vN \rightarrow l^-ND^+)}{dydQ^2dt}$ (in pb GeV⁻⁴) for D^+ production on a proton (left panel) and neutron (right panel) target for y = 0.7, $\Delta_T = 0$ and s = 20 GeV².

The interference term σ_{-0} is accessed through azimuthal moments such as

$$\langle \cos \varphi \rangle = \frac{\int \cos \varphi \, d\varphi \, d^4 \sigma}{\int d\varphi \, d^4 \sigma} \approx K_{\varepsilon} \frac{\mathscr{R}e\sigma_{-0}}{\sigma_{00} + K_{\varepsilon}^2 \sigma_{--}},\tag{8}$$

with $K_{\varepsilon} = \frac{\sqrt{1+\varepsilon}+\sqrt{1-\varepsilon}}{2\sqrt{\varepsilon}}$. This allows access to the transversity GPDs in a linear way but requires to consider $\Delta_T \neq 0$ kinematics. We show on Fig. $5 < \cos\varphi >$ and $< \sin\varphi >$ for the proton and neutron target, for the kinematical point defined as $y = 0.7, \Delta_T = 0.5$ GeV and s = 20 GeV².

In conclusion, let us stress that collinear QCD factorization has allowed us to calculate exclusive neutrino production of D-mesons in terms of GPDs. This reaction gives us a new experimental access to transversity GPDs which is quite different from the previous proposals [5, 6]. Planned medium and high energy neutrino facilities [7] and experiments such as Minerva [8] and MINOS+



Figure 5: The Q^2 dependence of the $\langle \cos \varphi \rangle$ (solid curves) and $\langle \sin \varphi \rangle$ (dashed curves) moments normalized by the total cross section, for $\Delta_T = 0.5$ GeV, y = 0.7 and s = 20 GeV² for a proton (left panel) and a neutron(right panel) target. The three curves correspond to the three models explained in [3], and quantify the theoretical uncertainty of our estimates.

[9] which have their scientific program oriented toward the understanding of neutrino oscillations will collect more statistics than presently available and should thus allow some important progress in the realm of hadronic physics.

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