



Finite mass effects in Higgs production in association with jets

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The production of a Higgs boson at the LHC suffers from large higher order corrections. This is true also when it is accompanied by further jets. The most precise results rely on computations in an effective theory where the heavy quark loops, mediating the coupling between the Higgs boson and the gluons, are integrated out. As the LHC is delivering more and more precise data, it is important to understand in detail the validity range of such effective theory predictions, in particular in view of boosted analyses. In this talk we will present detailed comparisons between effective theory results and predictions obtained in the full theory.

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1. Introduction

The production of a Higgs boson in gluon-gluon fusion is the leading Higgs production channel. Its production in association with jets is also very important, in particular for the determination of differential spectra. However, being a loop-induced process, increasing the multiplicity or the precision of the predictions becomes quickly very hard or beyond the possibilities of current computational techniques. When the mass of the fermions running in the loop is much larger than the Higgs boson mass, the heavy fermion can be integrated out and the coupling between gluons and the Higgs can be described by an effective vertex, simplifying the calculations considerably. The validity of this effective theory is however known to be limited, in particular when the momentum flow through the effective vertex becomes of the same order as the fermion masses. In this talk, based on the results presented in Ref. [1], we explore the range of validity and the breakdown of the effective theory approach at a more quantitative level.

2. Computational setup

In the following we will compare predictions for the production of a Higgs boson in association with up to three jets at Leading Order (LO) in the full Standard Model (SM) with Next-to-Leading Order (NLO) predictions in the effective theory presented in Refs. [2, 3]. All the one-loop amplitudes are computed with GOSAM[4], a publicly available package for the automated generation of one-loop amplitudes. For the generation of the amplitudes GOSAM employs QGRAF [5], FORM [6] and SPINNEY [7] whereas for the reduction it relies on NINJA [8], which implements an algorithm based on the Lauren expansion [9], SAMURAI [10], which uses the OPP reduction method [11] in *d* dimensions, or GOLEM95C [12], which is a tensor integral library. For the latter the reconstruction of the tensor structure is performed either using the method outlined in [13] or via derivation with respect to the loop momentum. The scalar loop integrals can be computed with QCDLOOP [14] or ONELOOP [15]. All the tree-level parts are computed with the multipurpose Monte Carlo (MC) program SHERPA [16], using COMIX [17], to which the 1-loop code is interfaced via the BLHA interface [18]. LO and NLO events are stored in form of ROOT Ntuples [19]. For more details about the calculation, the Ntuples format and the values of the physical parameters we refer to the original publication [1].

3. Results

We present results for H+1, 2 and 3 jets using the following set of baseline cuts at a center-ofmass energy of 13 TeV:

$$p_{T,jet} > 30 \,\text{GeV} \,, \qquad |y_{jet}| < 4.4 \,, \tag{3.1}$$

where jets are clustered with the anti- k_T algorithm [20] as implemented in the FASTJET package [21] with radial distance R = 0.4. For the 100 TeV results we increase the transverse momentum cut to $p_{T,jet} > 100$ GeV. The factorization and renormalization scales are set equal to

$$\mu_F = \mu_R \equiv \frac{\hat{H}'_T}{2} = \frac{1}{2} \left(\sqrt{m_H^2 + p_{T,H}^2} + \sum_i |p_{T,i}| \right) .$$
(3.2)





Figure 1: Inclusive cross sections for H+1 jet, H+2 jets and H+3 jets production at center-of-mass energies of 13 TeV and 100 TeV shown to the left and right, respectively. The width of the bands shows the associated scale uncertainty.

We start comparing the predictions for the total cross section for 13 and 100 TeV shown in Fig. 1. The height of the boxes represents the uncertainty due to renormalization and factorization scales variation by factors of 0.5 and 2. For each multiplicity we show the prediction at LO and NLO in the effective theory (labeled as $\sigma_{\text{LO,eff}}$ and $\sigma_{\text{NLO,eff}}$ respectively) and compare them with the full theory results at leading order when considering both top-quark and bottom-quark loops, called $\sigma_{LO, m_{t,b}}$, as well as with the case where only top-quark loops are taken into account, labeled σ_{LO,m_t} . In the lower plots we include the ratios to the leading order results in the effective theory. Focusing on the central values, we observe that the leading-order contribution in the effective theory agrees in general very well with the predictions based on the full theory. Taking bottom-quark loops into account leads to corrections, which are as small as one percent for all three final-state multiplicities we are considering, and, as expected, they become even smaller at 100 TeV. However, it is interesting to note the change in the sign of these corrections with increasing jet multiplicity. While for H+ 1 jet production at 13 TeV the cross section is reduced when bottom-quark loop contributions are included, for H+2jets and H+3jets the cross section increases instead. This is due to a destructive interference effect on the cross section in the low transverse momentum region caused by terms which scale like

$$\frac{1}{p_T^2} \frac{m_b^2}{m_H^2} \log^2 \left(\frac{m_b^2}{p_T^2}\right),\tag{3.3}$$

which for $m_b < p_T < m_H$ can become important in H+1 jet. For higher multiplicities the transverse momentum p_T is diluted among more jets, leading to a ratio in the logarithm closer to unity. Therefore $\sigma_{\text{LO},m_t} < \sigma_{\text{LO},m_{t,b}}$ for H+2 jets and H+3 jets. At 100 TeV the minimum jet transverse momentum is much harder, and the phase space region where terms of the form of Eq. 3.3 could become important are excluded. For this reason the hierarchy between σ_{LO,m_t} and $\sigma_{\text{LO},m_{t,b}}$ is the same in this case for H+1, 2 and 3 jets.

We now turn our attention to the observables displaying the breakdown of the effective theory prediction par excellence, which are the transverse momentum of the Higgs boson, $p_{T,H}$, and



Figure 2: Comparison of effective theory predictions at LO and NLO with LO predictions (indicated by the extra ' $m_{t,b}$ ' label) obtained in the full SM for the Higgs boson transverse momentum $p_{T,H}$ (left) and the leading jet transverse momentum, p_{T,j_1} (right). Note that the H+1 jet (green curves) and H+3 jets (red curves) predictions have been rescaled for better visibility. The smaller plots in the lower part of each panel show the ratios of the three different predictions normalized to the LO effective theory prediction. This is done separately for each of the H+1 jet, H+2 jets and H+3 jets processes.

the one of the leading jet, p_{T,j_1} , shown to the left and right in Fig. 2, respectively. These two distributions clearly show the expected behaviour of p_T -tail softening. In order to better quantify the scaling properties of the distributions at large transverse momenta we introduce the quantity $R_{m_t,b}(O)$ which is defined as

$$R_{m_{t,b}}(O) \equiv \frac{\frac{\mathrm{d}\sigma}{\mathrm{d}O}|_{m_{t,b}}}{\frac{\mathrm{d}\sigma}{\mathrm{d}O}|_{\mathrm{eff}}} \,. \tag{3.4}$$

We observe that the point at which the effective theory approach starts to break down occurs around Higgs boson or lead-jet values of $p_T = 200$ GeV and is to a good approximation independent of the jet multiplicity of the Higgs boson production processes. Above this scale, the deviation from the full SM predictions becomes sizeable very rapidly and it is therefore fair to say that the NLO corrections in the effective theory turn into a sub-leading effect, already at $p_T \sim 400$ GeV. Similar observations have already been made before [22, 23, 24], it is however interesting to see that the differential ratios associated with $p_{T,H}$ and p_{T,j_1} are strikingly similar in their characteristics even beyond the one-jet case. In addition, they are also very similar among the different jet bins, suggesting that the relative $1/p_T^2$ scaling between the effective and full theory at LO [25, 26] can be applied in a more universal manner. In fact if we concentrate on the $p_{T,H}$ predictions, we observe that the suggested scaling for the cross section ratio $R_{m_{t,b}}(p_{T,H}) \equiv R_{m_{t,b}}(p_{T,H}^2)$ holds to a fairly good extent. For example, at $p_{T,H} \approx 400$ GeV, the mass effects reduce the cross section to roughly 60% of the effective theory result. At $p_{T,H} > 1$ TeV, this reduction then turns into an one-order of magnitude effect, which fixes the related ratio at a value of

$$\frac{R_{m_{t,b}}(p_{T,H} = 1.0 \text{ TeV})}{R_{m_{t,b}}(p_{T,H} = 0.4 \text{ TeV})} \approx \frac{10\%}{60\%} = \frac{1}{6}.$$
(3.5)

The above number (as given by our computation) can be compared with the number one expects from exploiting the relative scaling property between the effective and full theory predictions. Based on the additional suppression of the full result by two powers of $p_{T,H}$, the expected value for the same cross section ratio amounts to $(400 \text{ GeV}/1000 \text{ GeV})^2 = 4/25$, which is very close to the value extracted from the theory data. This result for the scaling does not change much among the different jet bins [1].

The impact of finite mass effects can therefore be very dramatic when studying Higgs boson production in gluon-gluon fusion at transverse momenta above $p_{T,H} \approx 200$ GeV. As the LHC collects more and more statistics allowing for Higgs measurements also at large p_T , the inclusion of mass effects becomes more and more relevant in particular for boosted Higgs studies [27]. Many more observables and results, also including bottom mass effects at the differential level and the impact of vector boson fusion selection cuts can be found in [1].

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