

# Precision predictions for associated gluino-gaugino production at the LHC

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Now that the mass limits for gluinos have been pushed to the few-TeV range, they might only be visible at the LHC in associated production with lighter gauginos. We compute the corresponding cross section at next-to-leading logarithmic (NLL) and next-to-leading order (NLO) precision in the QCD coupling constant. The resulting expressions are implemented in the public code RESUMMINO and can be directly used in the corresponding experimental searches.

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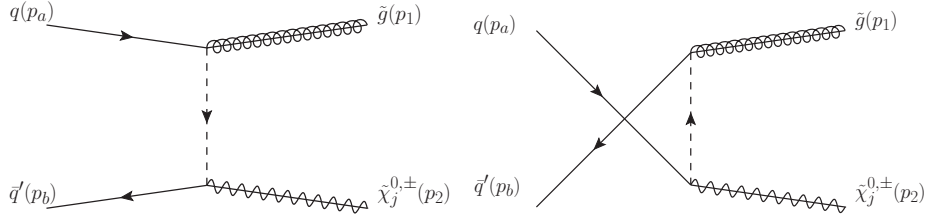
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## 1. Cross sections for supersymmetric particles at the LHC

Supersymmetry (SUSY), a long-standing, well-motivated and complete extension of the Standard Model (SM) of particle physics with a rich phenomenology, continues to be searched for at CERN's Large Hadron Collider (LHC). For many years, squarks and gluinos have been at the centre of this search due to their strong interactions and correspondingly large cross sections. However, the mass limits for these particles are now already in the few-TeV range, so that pair production of these particles might soon get out of reach at LHC energies of 13 or 14 TeV. Associated production of squarks and gluinos with an electroweak superpartner (a gaugino or higgsino, or equivalently a neutralino or chargino), that is still allowed to be light and that is motivated for its part by dark matter observations, might then be the only possibility to study them. The corresponding cross sections, which are, like the average produced final-state mass, of intermediate size and have been known for many years at next-to-leading order (NLO) of QCD, should then be known with the same up-to-date precision as those for strong and weak SUSY particle pair production, i.e. at next-to-leading logarithmic (NLL) accuracy [1] and beyond [2], so that they can be used by the ATLAS [3] and CMS [4] collaborations.

## 2. Analytical results

The tree-level Feynman diagrams for associated gluino-gaugino production are shown in Fig. 1.



**Figure 1:** Tree-level Feynman diagrams for associated gluino-gaugino production.

They lead to the squared matrix elements

$$\mathcal{M}_t \mathcal{M}_t^* = \frac{C_A C_F e g_s(\mu_r)}{(m_{\tilde{q}}^2 - t)(m_{\tilde{q}_c}^2 - t)} (\mathcal{L}' \mathcal{L}'_c + \mathcal{R}' \mathcal{R}'_c) (L L_c + R R_c) (m_{\tilde{g}}^2 - t)(m_{\tilde{\chi}}^2 - t), \quad (2.1)$$

$$\mathcal{M}_u \mathcal{M}_u^* = \frac{C_A C_F e g_s(\mu_r)}{(m_{\tilde{q}}^2 - u)(m_{\tilde{q}_c}^2 - u)} (\mathcal{L} \mathcal{L}_c + \mathcal{R} \mathcal{R}_c) (L' L'_c + R' R'_c) (m_{\tilde{g}}^2 - u)(m_{\tilde{\chi}}^2 - u), \quad (2.2)$$

$$\begin{aligned} \mathcal{M}_t \mathcal{M}_u^* &= \frac{C_A C_F e g_s(\mu_r)}{(m_{\tilde{q}}^2 - t)(m_{\tilde{q}_c}^2 - u)} \left[ \left( -s^2 + t^2 + u^2 + (m_{\tilde{\chi}}^2 + m_{\tilde{g}}^2)(s - t - u) + 2m_{\tilde{g}}^2 m_{\tilde{\chi}}^2 \right) \right. \\ &\quad \left. \times (L L_c \mathcal{L}' \mathcal{L}'_c + R R_c \mathcal{R}' \mathcal{R}'_c) + 2m_{\tilde{g}} m_{\tilde{\chi}} s (\mathcal{R} \mathcal{R}_c \mathcal{L}' L'_c + \mathcal{L} L_c \mathcal{R}' R'_c) \right], \quad (2.3) \end{aligned}$$

and consequently the partonic and hadronic cross sections

$$d\sigma_{ab}^{(0)} = \int_2 d\sigma^B = \int \frac{1}{2s} \frac{1}{4C_A^2} \sum_{\tilde{q}, \tilde{q}_c} (\mathcal{M}_t \mathcal{M}_t^* + \mathcal{M}_u \mathcal{M}_u^* - 2\text{Re}(\mathcal{M}_t \mathcal{M}_u^*)) d\text{PS}^{(2)} \quad (2.4)$$

and

$$\begin{aligned} \sigma_{AB} &= \int M^2 \frac{d\sigma_{AB}}{dM^2}(\tau) = \sum_{a,b} \int_0^1 dx_a dx_b dz [x_a f_{a/A}(x_a, \mu_f^2)] [x_b f_{b/B}(x_b, \mu_f^2)] \\ &\quad \times [z d\sigma_{ab}(z, M^2, \mu_r^2, \mu_f^2)] \delta(\tau - x_a x_b z). \end{aligned} \quad (2.5)$$

Here  $C_{A,F}$  denote QCD colour factors,  $e, g_s(\mu_r)$  electromagnetic and (scale-dependent) strong couplings,  $s, t, u$  Mandelstam variables,  $dPS^{(2)}$  the two-particle phase space,  $L, R$  and  $\mathcal{L}, \mathcal{R}$  gaugino and gluino coupling strengths, and  $\tau = M^2/S$  the ratio of the squared invariant mass of the produced SUSY particle pair to the hadronic centre-of-mass energy. The NLO corrections are computed with the Catani-Seymour dipole subtraction method [5]

$$d\sigma_{ab}^{(1)} = \sigma^{\{3\}} + \sigma^{\{2\}} + \sigma^C = \int_3 [d\sigma^R - d\sigma^A]_{\varepsilon=0} + \int_2 [d\sigma^V + \int_1 d\sigma^A]_{\varepsilon=0} + \sigma^C \quad (2.6)$$

in  $D = 4 - 2\varepsilon$  dimensions, and the final result agrees with our previous calculation [6].

Close to partonic threshold, when  $z = \frac{M^2}{s} \rightarrow 1$ , large logarithms  $\left(\frac{\alpha_s}{2\pi}\right)^n \left[\frac{\ln^n(1-z)}{1-z}\right]_+$  spoil the convergence of the perturbative series and must be resummed to all orders. This is most easily achieved in Mellin space, where the resummed cross section

$$d\sigma_{ab \rightarrow ij}^{(\text{res.})}(N, M^2, \mu^2) = \sum_I \mathcal{H}_{ab \rightarrow ij, I}(M^2, \mu^2) \Delta_a(N, M^2, \mu^2) \Delta_b(N, M^2, \mu^2) \Delta_{ab \rightarrow ij, I}(N, M^2, \mu^2) \quad (2.7)$$

factorises into soft-collinear and soft functions

$$\Delta_a \Delta_b \Delta_{ab \rightarrow ij, I} = \exp \left[ LG_{ab}^{(1)}(\lambda) + G_{ab \rightarrow ij, I}^{(2)}(\lambda, M^2/\mu^2) + \dots \right] \quad (2.8)$$

with leading and next-to-leading logarithms [7]

$$G_{ab}^{(1)}(\lambda) = g_a^{(1)}(\lambda) + g_b^{(1)}(\lambda), \quad (2.9)$$

$$G_{ab \rightarrow ij}^{(2)}(\lambda) = g_a^{(2)}(\lambda, M^2, \mu_r^2, \mu_f^2) + g_b^{(2)}(\lambda, M^2, \mu_r^2, \mu_f^2) + h_{ab \rightarrow ij, I}^{(2)}(\lambda). \quad (2.10)$$

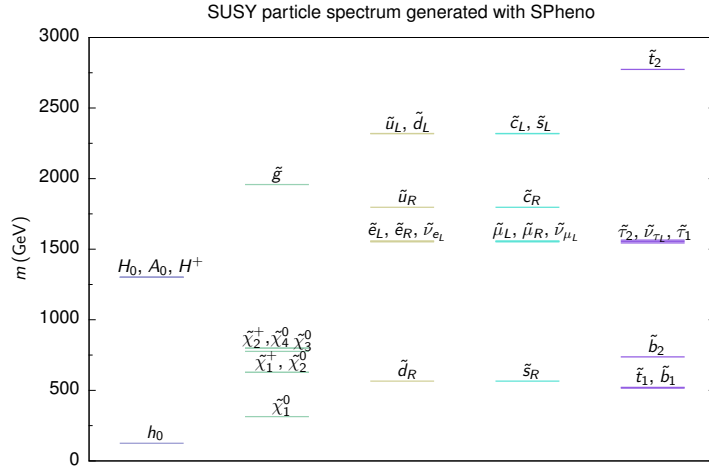
The soft anomalous dimension  $h_{ab \rightarrow ij, I}^{(2)}$  and hard matching coefficient  $\mathcal{H}_{ab \rightarrow ij, I}$  are process-dependent. The former reads in the present case

$$h_{ab \rightarrow ij, I}^{(2)}(\lambda) = \frac{2\pi \ln(1-2\lambda)}{\alpha_s} \frac{1}{2\beta_0} \text{Re} \left\{ \frac{\alpha_s}{2\pi} C_A \left[ \ln 2 + i\pi - 1 + \ln \left( \frac{m_{\tilde{g}}^2 - t}{\sqrt{2} m_{\tilde{g}} \sqrt{s}} \right) + \ln \left( \frac{m_{\tilde{g}}^2 - u}{\sqrt{2} m_{\tilde{g}} \sqrt{s}} \right) \right] \right\}, \quad (2.11)$$

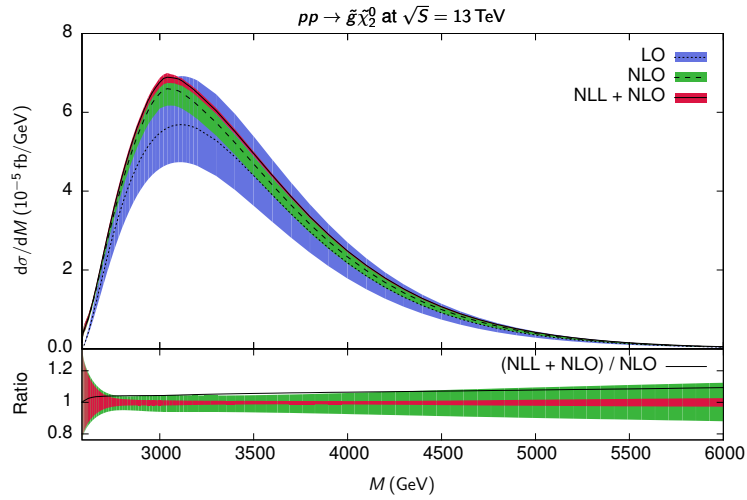
while the latter ( $\mathcal{H}_{ab \rightarrow ij, I}$ ) can be found in Ref. [8].

### 3. Numerical results

We study the impact of the NLL+NLO corrections in a phenomenological Minimal SUSY SM with 13 free parameters (pMSSM-13). Input parameters are in particular the bino and gluino soft SUSY-breaking masses  $M_1$  and  $M_3$ , with the wino mass fixed to  $M_2 \simeq 2M_1$ . The physical mass spectrum is then obtained with SPheno 3.37 [9] and shown for our example scenario in Fig. 2. Fig. 3 shows the invariant-mass distribution of the produced sparticles. Additional radiation shifts



**Figure 2:** Default pMSSM-13 scenario with light gauginos, a heavy gluino and the correct mass of the lightest Higgs boson.

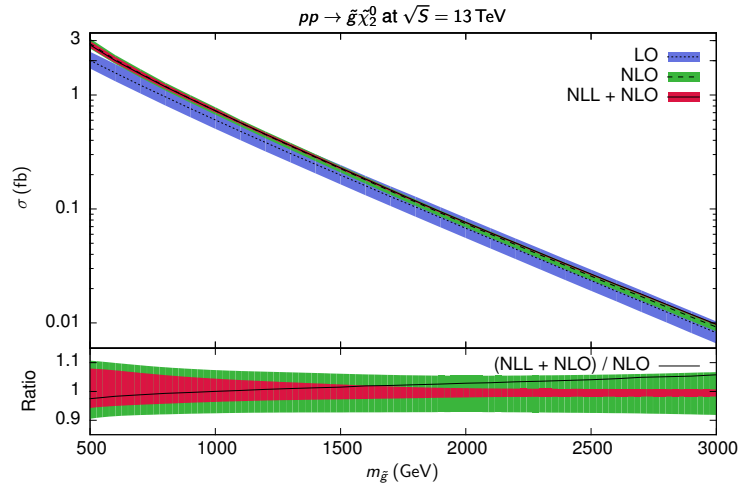


**Figure 3:** Invariant-mass distributions in LO, NLO and NLL+NLO at the LHC with its current centre-of-mass energy of 13 TeV.

the maximum to lower invariant masses and reduces the scale dependence. At large  $M$ , the NLL corrections increase the NLO cross section by up to 10%, and the total scale dependence is reduced there from 30% to 5% (lower panel). The variation of the gluino mass in Fig. 4 demonstrates that associated gluino-gaugino pairs in this class of SUSY scenarios will soon be observable at the LHC with an integrated luminosity of  $100 \text{ fb}^{-1}$  up to gluino masses of 3 TeV.

#### 4. Conclusion

The semi-weak associated production of gluinos and gauginos might soon become relevant, if



**Figure 4:** Total cross section as a function of the gluino mass in LO, NLO and NLL+NLO.

gluinos are too heavy to be pair-produced at the LHC. This would indeed be theoretically expected from the GUT relation  $M_1 = M_2/2 = M_3/6$  among the soft SUSY-breaking gaugino and gluino mass parameters. We have summarised the analytical calculations of the process-dependent pieces of a threshold-resummation calculation at NLL accuracy, i.e. of the soft anomalous dimension and the hard matching coefficient, before matching the result to a full NLO calculation and performing numerically an inverse Mellin transform. As we have seen, the NLL contributions can increase the NLO invariant mass distribution by up to 10% and reduce the total scale dependence from 30% to 5%. The parton density function (PDF) uncertainty should be reduced by including threshold-improved PDFs in the near future.

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