The flavour changing neutral current decays are interesting probes for new physics searches. The angular distributions of $b \to s \ell^+ \ell^-$ transition processes of both $B^0 \to K^0 \mu^+ \mu^-$ and $B^+ \to K^+ \mu^+ \mu^-$ decays are studied using a sample of proton-proton collisions at $\sqrt{s} = 8$ TeV collected with the CMS detector at the LHC, corresponding to an integrated luminosity of 20.5 fb$^{-1}$. Angular analyses are performed to determine the angular parameters $P_1$ and $P'_5$ for $B^0 \to K^0 \mu^+ \mu^-$ and $A_{FB}$ and $F_H$ parameters for $B^+ \to K^+ \mu^+ \mu^-$, as functions of the dimuon invariant mass squared. All the measurements are consistent with the standard model predictions.
1. Introduction

Phenomena beyond the Standard Model (SM) can be probed directly, via the production of new particles, or indirectly, by studying the production and decay of SM particles. The transitions of the type $b\to s \ell^+\ell^-$ are flavor-changing neutral currents (FCNCs). According to the SM, these transitions are forbidden at tree level and occur through higher-order processes penguin or box diagrams. For this reason, the measurement of these rare FCNC decays is very sensitive to physics phenomena beyond the SM.

The Compact Muon Solenoid Experiment (CMS) has analysed two FCNC decays: $B^0 \to K^{*0}\mu^+\mu^-$, where $K^{*0}$ indicates the $K^{*0}(892)$ meson, and $B^+ \to K^+\mu^+\mu^-$ [1, 3]. Both analyses use a data sample collected in proton-proton (pp) collisions at a centre-of-mass energy of 8 TeV with the CMS detector at LHC, corresponding to an integrated luminosity of 20.5 fb$^{-1}$.

2. The $B^0 \to K^{*0}\mu^+\mu^-$ decay

The angular distribution of the $B^0 \to K^{*0}\mu^+\mu^-$ decay can be described as a function of four kinematic variables: the dimuon invariant mass squared, $q^2$, the decay angle of the dimuon system, $\theta_d$, the decay angle of the $K^{*0}$, $\theta_K$, and the angle between these two decay planes, $\phi$.

Among several angular parameters used to describe the angular decay rate of the $B^0 \to K^{*0}\mu^+\mu^-$ process, the $P_S'$ parameter is of particular interest due to LHCb and Belle measurements [4, 5, 6] that indicate a potential discrepancy with the standard model. CMS performed a measurement of the $P_1$ and $P_S'$ angular parameters [1], trying to elucidate the situation.

In the measurement, the $q^2$ spectrum, ranging from 1 to 19 GeV$^2$, has been divided in 9 bins, and the values of $P_1$ and $P_S'$ angular parameters are determined by fitting the distribution of events as a function of the three angular variables, independently in each $q^2$ bin. The $q^2$ bins $8.68 < q^2 < 10.09$ GeV$^2$ and $12.90 < q^2 < 14.18$ GeV$^2$, contain the $B^0 \to K^{*0}J/\psi$ and $B^0 \to K^{*0}\psi(2S)$ decays, respectively, and are used as control channels to validate the analysis.

The angular distribution of $B^0 \to K^{*0}\mu^+\mu^-$ can be written as:

$$
\frac{d^4\Gamma}{d\ell^2 dq^2 d\cos\theta_d d\cos\theta_K d\phi} = \frac{9}{8\pi} \left\{ F_S + A_S \cos\theta_K \left( 1 - \cos^2\theta_d \right) \right\} + A_S' \sqrt{1 - \cos^2\theta_K} \sqrt{1 - \cos^2\theta_d} \cos\phi \\
+ \left( 1 - F_S \right) \left\{ 2 F_L \cos^2\theta_K \left( 1 - \cos^2\theta_d \right) \right\} + \frac{1}{2} (1 - F_L) \left( 1 - \cos^2\theta_K \right) \left( 1 + \cos^2\theta_d \right) \\
+ \frac{1}{2} P_1 (1 - F_L) (1 - \cos^2\theta_K) (1 - \cos^2\theta_d) \cos\phi \\
+ 2 P_S' \cos\theta_K \sqrt{F_L (1 - F_L)} \sqrt{1 - \cos^2\theta_K} \sqrt{1 - \cos^2\theta_d} \cos\phi \right\} \tag{2.1}
$$

where $F_L$ denotes the longitudinal polarisation fraction of the $K^{*0}$, $F_S$ represents the contamination fraction of spin 0 (S-wave) $B^0 \to K\pi^+\mu^+\mu^-$ decays, and $A_S$ and $A_S'$ encode the interference between S-wave and P-wave. This expression is an exact simplification of the full angular distribution, obtained by folding the $\phi$ and $\theta_d$ variables around zero and $\pi/2$, respectively.

For each $q^2$ bin, the observables of interest are extracted from an unbinned extended maximum-likelihood fit to four variables: the $K^-\pi^+\mu^+\mu^-$ invariant mass, $m$, and the three angular variables,
\[ \cos \theta_\ell, \cos \theta_K, \text{ and } \phi. \]  

The probability density function (pdf) used in the fit has the following expression:

\[
p.d.f.(m, \cos \theta_K, \cos \theta_\ell, \phi) = Y_C^C \cdot \left( S^R(m) \cdot S^S(\cos \theta_K, \cos \theta_\ell, \phi) \cdot e^R(\cos \theta_K, \cos \theta_\ell, \phi) + \frac{f_M}{1 - f_M} \cdot S^M(m) \cdot S^S(-\cos \theta_K, -\cos \theta_\ell, -\phi) \cdot e^M(\cos \theta_K, \cos \theta_K, \phi) \right) + Y_B \cdot B^R(m) \cdot B^{\cos \theta_K}(\cos \theta_K) \cdot B^{\cos \theta_\ell}(\cos \theta_\ell) \cdot B^B(\phi). \tag{2.2} \]

where the three lines correspond to correctly tagged signal events, mistagged signal events, and background events, respectively. The parameters \( Y_C^C \) and \( Y_B \) are the yields of correctly tagged signal events and background events, respectively, and are free parameters in the fit. The parameter \( f_M \) is the fraction of signal events in which the mass assignment to the kaon and pion candidates is wrong, and is determined from MC simulation. The signal mass shapes, \( S^R(m) \) and \( S^M(m) \), are each the sum of two Gaussian functions sharing the same mean, and describe the mass distribution for correctly tagged and mistagged signal events, respectively.

In the signal mass shapes, the mean, the four Gaussian \( \sigma \) parameters, and two fractions relating the contribution of each Gaussian, are determined from simulation. The function \( S^S(\cos \theta_K, \cos \theta_\ell, \phi) \) describes the angular decay rate of the signal and corresponds to Equation 2.1. The functions \( B^R(m) \cdot B^{\cos \theta_K}(\cos \theta_K) \cdot B^{\cos \theta_\ell}(\cos \theta_\ell) \cdot B^B(\phi) \) are obtained from \( B^0 \) sideband data and describe the background distributions, where the mass shape is an exponential function and the angular shapes are polynomials ranging from first to fourth degree, depending on the \( q^2 \) bin and on the angular variable. The three-dimensional functions \( e^R(\cos \theta_K, \cos \theta_\ell, \phi) \) and \( e^M(\cos \theta_K, \cos \theta_K, \phi) \) parametrise the efficiencies of signal events for correctly tagged and mistagged signal events, respectively. They have been built using a novel non-parametric algorithm based on kernel density estimators.

The fit is performed in two steps: the first step uses the data from the sidebands of the \( B^0 \) mass to obtain the parameters of the background components. These parameters are then kept fixed in the second step, in which the full mass range is fitted, using the whole pdf. The free parameters in this second step are the angular parameters \( P_1, P'_2, \text{ and } A_3 \), and the yields \( Y_C^C \) and \( Y_B \). The angular parameters \( F_1, F_2, \text{ and } A_3 \) are fixed to previous CMS measurements performed on the same data set with the same event selection criteria [2].

The fit algorithm is validated through fits to pseudo-experimental samples, MC simulation samples, and control channels. To ensure correct coverage for the uncertainties of the angular parameters, the Feldman-Cousins (FC) method is used to determine the statistical uncertainties of the measurements. Several sources of systematic uncertainties are evaluated, and included in the resulting uncertainty.

As an example, the projections of the fit result for the second \( q^2 \) bin, are shown in Figure 1. The fit results of \( P_1 \) and \( P'_2 \), for each \( q^2 \) bin, are shown in Figure 2, along with the SM predictions and the experimental results of other experiments. The results are consistent with the predictions based on the Standard Model.
Figure 1: Invariant mass and angular distributions of $K^-\pi^+\mu^+\mu^-$ events for $2 < q^2 < 4.3$ GeV$^2$. The projection of the results from the total fit, as well as for correctly tagged signal events, mistagged signal events, and background events, are also shown. The vertical bars indicate the statistical uncertainties.

Figure 2: CMS measurements of the $P_1$ and $P'_5$ angular parameters versus $q^2$ for $B^+ \rightarrow K^0\mu^+\mu^-$ decays, in comparison to results from the LHCb [5] and Belle [6] Collaborations. The statistical uncertainties are shown by the inner vertical bars, while the outer vertical bars give the total uncertainties. The horizontal bars show the bin widths. The vertical shaded regions correspond to the $J/\psi$ and $\psi(2S)$ resonances. The hatched region shows the predictions from two SM calculations described in the text, averaged over each $q^2$ bin.

3. The $B^+ \rightarrow K^+\mu^+\mu^-$ decay

The angular distribution of the process $B^+ \rightarrow K^+\mu^+\mu^-$ can be described as a function of the dimuon invariant mass, $q^2$, and the decay angle of the dimuon system, $\theta_\ell$. The $\theta_\ell$ dependence of the decay rate can be parametrized in terms of $A_{FB}$ and $F_H$ angular parameters, as:

$$
\frac{1}{d\Gamma/dq^2} \frac{d^3\Gamma}{dq^2 d\cos \theta_\ell} = \frac{3}{4} (1 - F_H) \left( 1 - \cos^2 \theta_\ell \right) + \frac{1}{2} F_H + A_{FB} \cos \theta_\ell
$$

The requirement for the decay rate to be positive in the whole phase space constrains the parameter values to satisfy $0 \leq F_H \leq 3$ and $|A_{FB}| \leq \min(1, F_H/2)$.
In this analysis, each event is reconstructed through the decay into the fully charged final state of one charged hadron and a pair of oppositely charged muons. Dimuon candidates are formed from two oppositely charged muons, that match the muon candidates that triggered the event read-out. To discriminate signal events from background contamination, selection criteria on kinematic variables are used. These criteria are determined through a maximization of the expected signal significance in the final $B^+$ meson invariant mass fitting region, $5.1 - 5.6$ GeV.

The $q^2$ spectrum, ranging from 1 to 22 GeV$^2$, has been divided in 9 bins; two of them containing the resonant $B^+ \rightarrow K^+ J/\psi$ and $B^+ \rightarrow K^+ \psi(2S)$ decays are used as control channels. In addition the analysis is repeated in two special bins: the first one ranges from 1 to 6 GeV$^2$ and includes the region with more robust theoretical predictions, and the second one includes the whole $q^2$ spectrum excluding the two bins of the control regions. The angular parameters $A_{FB}$ and $F_H$ are extracted from a two-dimensional unbinned extended maximum-likelihood fit to the $B^+$ candidate mass, $m$, and to the $\cos \theta_\ell$ distributions, in each $q^2$ range. The probability density function (pdf) used in the fit is:

$$p.d.f.(m, \cos \theta_\ell) = Y_S \cdot S(m) \cdot S'(\cos \theta_\ell) \cdot \epsilon(\cos \theta_\ell) + Y_B \cdot B^m(m) \cdot B^{\cos \theta_\ell}(\cos \theta_\ell)$$

(3.2)

where the two contributions correspond to the parametrization of the signal and background. The $Y_S$ and $Y_B$ parameters are the yields of signal and background events, respectively. The functions $S(m)$ and $S'(\cos \theta_\ell)$ describe the signal invariant mass and angular distributions, while $B^m(m)$ and $B^{\cos \theta_\ell}(\cos \theta_\ell)$ functions describe the background distributions. The function $\epsilon(\cos \theta_\ell)$ encodes the signal efficiency as a function of $\cos \theta_\ell$, and is parametrised as a sixth-order polynomial whose parameters are determined through a fit to MC simulations.

The signal mass shape $S(m)$ is modeled as the sum of two Gaussian functions with a common mean, and the angular shape $S'(\cos \theta_\ell)$ is given in Equation 3.1. The background mass shape $B^m(m)$ is modelled as a single exponential function, while the background angular shape $B^{\cos \theta_\ell}(\cos \theta_\ell)$ is parametrised as the sum of a Gaussian function and a third- or fourth-degree polynomial, depending on the $q^2$ bin. The free parameters of the fit are the yields, $Y_S$ and $Y_B$, the angular parameters, $A_{FB}$ and $F_H$, and the exponential decay parameter of $B^m(m)$.

To validate the efficiency description derived from simulation, the ratio of the branching fractions of the two control channels is compared with the world-average value. The fitting procedure has been validated using MC simulated samples. Several sources of systematic uncertainties are considered in this analysis, and included in the resulted uncertainty.

The projections of the fit results for the $K^+ \mu^+ \mu^-$ invariant mass and $\cos \theta_\ell$ distributions, for the special $q^2$ bin of $1 - 6$ GeV$^2$, are shown in Figure 3. To evaluate the statistical uncertainties of $A_{FB}$ and $F_H$, the profiled FC technique has been used. The systematic and statistical uncertainties are added in quadrature to obtain the total uncertainty.

The measured values of $A_{FB}$ and $F_H$ are shown in Figure 4. The results for $A_{FB}$ are consistent with the SM expectation of no asymmetry. The $F_H$ values are compared with the SM predictions and a good agreement is observed. The results of this analysis are also in agreement with the previous measurements from other experiments.
4. Conclusions

The results of the angular analyses performed for the decays of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ and $B^+ \rightarrow K^+ \mu^+ \mu^-$, using pp collision data recorded at $\sqrt{s} = 8$ TeV with the CMS detector corresponding to an integrated luminosity of 20.5 fb$^{-1}$, are presented here. In each region of the dimuon invariant mass squared, unbinned maximum-likelihood fits were applied to the distributions of the B meson invariant mass and the angular variables, to extract the values of the angular parameters. The results are consistent with previous measurements and with the predictions from the Standard Model.

References


[arXiv:1512.04442 [hep-ex]].

