We report the measurements of $CP$ violation in $B$ meson decays focusing on the recent studies obtained using a data sample of 772 million $B\bar{B}$ collected by the Belle detector running at the $\Upsilon(4S)$ resonance at the KEKB $e^+e^-$ collider. We measure the $\phi_1$ and $\phi_2$, that are angles of the unitary triangle of Cabibbo-Kobayashi-Maskawa (CKM) matrix. Obtained results are consistent with expectations from the Standard Model (SM). Further studies using more statistics in the upgraded $B$-factory experiment are needed for more precise verification and search for the contribution from the new physics.
1. Introduction

In the SM, CP violation of the quark sector is induced if the complex phase appearing in the CKM matrix which describes the quark mixing [1]. Considering the unitarity between the matrix components in the system containing the b-quark, \( V_{ub}V_{ub}^* + V_{cd}V_{cb}^* + V_{ud}V_{ud}^* = 0 \), the CP violation is parameterized as non-zero angles of the unitary triangle, \( \phi_1 = \text{arg}[-V_{ub}V_{ub}^*/V_{cd}V_{cb}^*] \), \( \phi_2 = \text{arg}[-V_{ud}V_{ud}^*/V_{ub}V_{ub}^*] \) and \( \phi_3 = \text{arg}[-V_{cd}V_{cb}^*/V_{ub}V_{ub}^*] \) [2]. Time-dependent CP violation is induced by quantum interference between two decay amplitudes. In the neutral \( B \) meson decay, one is box diagram of mixing of \( B^0 \) and \( \bar{B}^0 \), and another is that of the decay into the CP-eigenstate. For decays of \( B^0 \) and \( \bar{B}^0 \) mesons produced via \( \Upsilon(4S) \rightarrow BB \) transitions, the decay rate has a time dependence [3, 4]

\[
\mathcal{P} (\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \times \left( 1 + q \left[ \mathcal{S} \sin(\Delta m_s \Delta t) + \mathcal{A} \cos(\Delta m_s \Delta t) \right] \right),
\]

where \( \mathcal{S} \) and \( \mathcal{A} \) are CP-violating parameters; \( q = 1 \) for \( B^0 \) decays and \( -1 \) for \( \bar{B}^0 \) decays; \( \Delta t \) is the difference in decay times of the \( B^0 \) and \( \bar{B}^0 \) mesons; \( \Delta m_s \) is the mass difference between the two mass eigenstates of the \( B^0-\bar{B}^0 \) system; and \( \tau_{B^0} \) is the \( B^0 \) lifetime. In this report, we present the results of the CP violation measurement using \( 772 \times 10^6 BB \) pairs accumulated with the Belle detector [5] on the \( \Upsilon(4S) \) resonance at the asymmetric energy collision of 8.0 GeV \( e^- \) and 3.5 GeV \( e^+ \) at the KEKB storage ring [6].

2. Belle detector

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a super-conducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect \( K_S^0 \) mesons and to identify muons (KLM). The detector is described in detail elsewhere [5]. Two inner detector configurations were used. A 2.0 cm radius beampipe and a 3-layer silicon vertex detector was used for the first sample of \( 152 \times 10^6 BB \) pairs, while a 1.5 cm radius beampipe, a 4-layer silicon detector and a small-cell inner drift chamber were used to record the remaining \( 620 \times 10^6 BB \) pairs [7].

3. Analysis of the CP violation measurement

In the studies of the CP violation, we reconstruct the decay into the CP-eigenstate. Mother \( B^0 \) meson is selected by kinematic variables calculated using the information such as momentum, energy and particle identification from the Belle detector. For the kinematic variables, beam constrained mass \( M_{bc} \equiv \sqrt{(E_{\text{beam}}/c^2)^2 - |\vec{p}_B^{\text{CM}}/c|^2} \) and energy difference \( \Delta E \equiv E_{\text{beam}} - E_B^{\text{CM}} \) are used, where \( \vec{p}_B^{\text{CM}} \) and \( E_B^{\text{CM}} \) are \( B \) momentum and energy in the \( \Upsilon(4S) \) center-of-mass system (CMS), respectively. \( E_{\text{beam}} \) is a measured beam energy in CMS. To suppress \( e^+e^- \rightarrow q\bar{q} \) continuum background events, a likelihood ratio is calculated using modified Fox-Wolfram moments [8, 9] and the
The wrong tag fractions for six CP using a vertex reconstruction algorithm described in [13]. The PDF for the signal is set to take the form of Eq. 3.1 which is determined using the data sample from the sideband regions of B decays. For the background, a large number of B̅B̅ and q̅q̅ processes are simulated. Interactions of the particles in the Belle detector are reproduced using GEANT3 [11] with detector configuration information in each time period of the experiment.

Since the B̄0 flavor q is not specified from observed decay products of the CP-eigenstates, q is determined using the information of inclusive properties of particles that are not associated with the signal B̄0 candidate after the selection. For the determination, a multi-dimensional likelihood based method is used[12]. The quality of the flavor tagging result is expressed by r, where r = 0 for no flavor discrimination and r = 1, where r = 0 corresponds to no flavor discrimination, and r = 1 corresponds to unambiguous flavor assignment. Candidates with r ≤ 0.1 are not used for CP violation measurement. The wrong tag fractions for six r intervals, w_i (i = 1 − 6) and their difference between B̄0 and B̄0 decays, ∆w_i are determined from a large number of control sample B̄0 decay data in which the flavor is specified by itself. The total effective tagging efficiency defined as $\Sigma(f_i \times (1 - 2w_i)^2)$ is determined to be (29.8 ± 0.4)%, where f_i is the fraction of the events in the l-th interval.

Due to the asymmetric energies of the $e^+$ and $e^-$ beams, the $\Upsilon(4S)$ is produced with a Lorentz boost of $\vec{B}\gamma = 0.425$ nearly along the +z axis, which is defined as the direction opposite the $e^+$ beam. Since the $B^0\bar{B}^0$ pair is almost at rest in the $\Upsilon(4S)$ CMS, the decay time difference $\Delta t$ can be determined from the separation along z of the $B^0$ and $\bar{B}^0$ decay vertices: $\Delta t \approx \Delta z / (\beta \gamma c)$. The vertex positions of the CP and opposite-side are reconstructed from all charged tracks in the event using a vertex reconstruction algorithm described in [13].

To measure the CP violation parameters, an unbinned maximum likelihood fit is performed for $\Delta t$ and q using the signal fraction evaluated from the signal extraction fit for variables of kinematic and continuum suppression. The PDF for the signal is set to take the form of Eq. 3.1 which is obtained by modifying Eq. 1.1 for wrong-tagging and vertex resolution:

$$\mathcal{P}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left( 1 - q\Delta w + (1 - 2w)q \left[ s\sin(\Delta m_d\Delta t) + c\cos(\Delta m_d\Delta t) \right] \right) \otimes R(\Delta t), \quad (3.1)$$

where $R(\Delta t)$ is a convolved resolution function which consists of components of detector resolution for $z_{CP}$ and $z_{tag}$ vertices, the shift of $z_{tag}$ due to secondary tracks from long-lived particles, and kinematic approximation in the $\Delta t$ calculation from vertex positions. These are determined using a large CP-conserving sample of semi-leptonic and hadronic B decays. For the background, which includes both $q\bar{q}$ and $B\bar{B}$, the PDF is modeled as a combination of two Gaussian functions and a δ-function determined using the data sample from the sideband regions of $M_{bc}$ and $\Delta E$. In the PDF, $\tau_{B^0}$ and $\Delta m_d$ are fixed to the world average values [14] including modifications to account for the effect of an incorrect flavor assignment. In addition to the signal and background, a broad Gaussian function is included to represent a small outlier component.
4. \( \phi_1 \) measurement in \( B^0 \to D^{(*)} h^0 (D \to K_S^0 \pi^+ \pi^-) \) decays

Using the \( B^0 \) decaying into a charmonium meson and \( K^0 \) states, \( \sin 2\phi_1 \) is measured with good accuracy [15]. A \( \sin 2\phi_1 \) has two angular solutions for the \( \phi_1 \) so that we need to determine the sign of \( \cos \phi_1 \) for the validation of the SM by comparing \( \phi_1 \) and the other measurements in the unitary triangle. The solution is given by the time-dependent analysis for the \( B^0 \) decays into the multi-body final states. Among the decays, \( B^0 \to D^{(*)} h^0 (h = K \text{ or } \pi) \) followed by \( D \to K_S^0 \pi^+ \pi^- \) has been studied using the full data set of the BABAR and Belle experiments [16]. In this decay, \( \cos \phi_1 \) appears in the coefficient of sine term of the time-dependent decay rate together with the decay amplitude as function of the Dalitz plot variables \( M_{K_S^0}^2 \) and \( M_{K_S^0}^2 \). Those variables are determined using large number of flavor-specific decay of \( D^{(*)} \to D^0 \pi^+ \) in \( e^+e^- \to c\bar{c} \) continuum events.

Signal yields of 1129 ± 48 and 1567 ± 56 events are obtained from the data sample of 471 million \( B\bar{B} \) from the BABAR and 772 million \( B\bar{B} \) from the Belle, respectively as shown in Figure 1. From the fit to the \( \Delta t \) of the selected events, \( \sin 2\phi_1 = 0.80 \pm 0.14 (\text{stat.}) \pm 0.06 (\text{syst.}) \pm 0.03 (\text{model}) \) and \( \cos 2\phi_1 = 0.91 \pm 0.22 (\text{stat.}) \pm 0.09 (\text{syst.}) \pm 0.07 (\text{model}) \) are obtained. Distribution of proper-time intervals and their asymmetries are shown in Figure 2. Significances of the non-zero \( \cos \phi_1 \) and \( \sin 2\phi_1 \) are 3.7\( \sigma \) and 5.1\( \sigma \), respectively. Consequently, this is a first evidence of positive \( \cos \phi_1 \) and first observation of the \( CP \) violation in \( B^0 \to D^{(*)} h^0 \) decays. From this result, a solution of \( \phi_1 = (22.5 \pm 4.4 (\text{stat.}) \pm 1.2 (\text{syst.}) \pm 0.6 (\text{model}))^0 \) is favored and this is consistent with other measurements of the unitary triangle.

5. \( \sin 2\phi_1^{\text{eff}} \) measurement in \( CP \)-even states of \( B^0 \to \pi^0 \pi^0 K^0_S \) decay

A value of \( \sin 2\phi_1 \) measured in the decays induced by \( b \to sq\bar{q}(q = u, d, s) \) penguin diagram, \( \sin 2\phi_1^{\text{eff}} \), is sensitive to the new physics beyond the SM since the contribution from the new physics is expected to the loop in the diagram. We have measured several kinds of the \( CP \)-eigenstates [15] and most of the sensitivity is from the \( CP \)-odd eigenstates of \( (q\bar{q})K^0_S \). Time-dependent \( CP \) violation in the \( CP \)-even states is measured only in the decays \( B^0 \to \eta' K^0_L \) and \( B^0 \to \phi K^0_L \) since reconstruction of the \( B^0 \) decays including the \( K^0_L \) is difficult. \( B^0 \to \pi^0 \pi^0 K^0_S \) three-body decay proceeds mainly via a \( b \to s d\bar{d} \) “penguin” amplitude [17] and final state is \( CP \)-even followed by the \( K^0_S \). We note that there is a \( b \to u\bar{u}s \) tree amplitude that also contributes to \( B^0 \to K^0_S \pi^0 \pi^0 \) decays and can shift \( \phi_1^{\text{eff}} \) from \( \phi_1 \); however, this amplitude is doubly Cabibbo-suppressed, and thus the resulting shift is very small [19]. Previously, the BABAR experiment studied this decay and measured \( \sin 2\phi_1^{\text{eff}} = -0.72 \pm 0.71 \pm 0.08 \) [20]; the sign is opposite to the expectation from the SM although the statistic uncertainty is large.

Since no charged tracks from the decay point of the \( B^0 \) decaying into \( CP \) eigenstate, the vertex is determined from the direction of the \( K^0_S \) and constraint from \( e^+e^- \) interaction point. Signal yield with the vertex information of 146.7 ± 23.6 events are obtained from the three-dimensional fit to variables of kinematic and continuum suppression as shown in Figure 3. Using the selected sample, \( \sin 2\phi_1^{\text{eff}} = 0.92^{+0.27}_{-0.31} (\text{stat.}) \pm 0.11 (\text{syst.}) \) and \( \phi' = 0.28 (\text{stat.}) \pm 0.04 (\text{syst.}) \) are obtained as shown in Figure 4. This is first result from the Belle experiment and consistent with the SM expectation.
Figure 1: Distributions of $M_{BC}, \Delta E$ and transformed shape of modified Fox-Wolfram moments $C_{MMNN}$ for selected $B^0 \rightarrow D^{(*)}h^0$ candidates. Points with error bars show the data and solid curve shows the fit result for signal yield extraction. Dotted curves show the contributions from each component of the fit.

Figure 2: $\Delta t$ and asymmetry distributions of $B^0 \rightarrow D^{(*)}h^0$ candidates. Points with errors show the data together with the fit curves. In the left plot, events are subdivided based on the sign of the sine term in the $\Delta t$ PDF: filled and open circles correspond to positive and negative sign, respectively. In the right plot, filled circle shows the $\Delta t$ of the events in which tagged flavor of the $B$ mesons are different and open circle shows that of the event in which the tagged flavor of the $B$ mesons are same.

6. Measurement of branching fraction and direct CP violation in $B^0 \rightarrow \pi^0\pi^0$ decay and update of $\phi_2$ constraint using isospin relation between $B \rightarrow \pi\pi$ system

As in the case of $\phi_1$, the $\phi_2$ is measured from the time-dependent decay rate of the decays induced by the $b \rightarrow u\bar{d}d$ tree diagram. On the other hand, measured $\phi_2$ contains additional CP phase due to contribution of penguin diagram. Therefore we need to eliminate the additional phase to obtain the $\phi_2$. One idea is to use isospin relations between the decay amplitudes of $B \rightarrow \pi\pi$ or $B \rightarrow \rho\rho$ decays [21]. Combining the measurements of branching fractions and CP violations, $\phi_2$ is determined with four-fold ambiguity. In the Belle experiment, measurements using 772 million $B\bar{B}$ have been performed for the $B^0 \rightarrow \pi^+\pi^-$ [22] and $B^+ \rightarrow \pi^+\pi^0$ [23].

Branching fraction and direct CP violation in the $B^0 \rightarrow \pi^0\pi^0$ are recently updated using full data set. In this decay mode, signal efficiency becomes lower since a photon is lost by the materials installed in front of the ECL in the Belle detector with probability of about 10% To recover that, remainders detected in the ECL are considered as photon candidates for the $B^0$ reconstruction.
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Figure 3: Distributions of $M_{bc}$, $\Delta E$ and modified Fox-Wolfram moments $R_{sb}$ for selected $B^0 \to \pi^0 \pi^0 K^0_S$ candidates. Points with error bars show the data and solid curve shows the fit result for signal yield extraction. Dashed and dotted curves show the contribution of total and $B\bar{B}$ background, respectively.

Figure 4: $\Delta t$ distribution of $B^0 \to \pi^0 \pi^0 K^0_S$ candidates. Points with errors show the data and events tagged as $q = +1$ and $q = -1$ are shown with filled and open circles together with the fit curves of solid and dashed lines, respectively.

From the extracted signal yields of $217 \pm 32$ event as shown in Figure 5. Branching fraction and direct $CP$ violation parameter are obtained as $(1.31 \pm 0.19(\text{stat.}) \pm 0.19(\text{syst.})) \times 10^{-6}$ and $0.14 \pm 0.36(\text{stat.}) \pm 0.10(\text{syst.})$, respectively. The significance of the branching fraction is $6.4\sigma$. By including these result to the isospin relation of $B \to \pi \pi$ decays, constraint on the $\phi_2$ is calculated to $9.5^\circ < \phi_2 < 81.6^\circ$ (68% confidence level) and $15.5^\circ < \phi_2 < 75.0^\circ$ (95% confidence level) as shown in Figure 6.

Figure 5: Distributions of $M_{bc}$, $\Delta E$ and transformed shape of modified Fox-Wolfram moments $T_C$ for selected $B^0(\bar{B}^0) \to \pi^0 \pi^0$ candidates. Points with error bars show the data and solid curve shows the fit result for signal yield extraction. Dashed, dotted and dot-dashed curves show the contribution of signal, $q\bar{q}$ continuum and $B\bar{B}$ background, respectively.

Figure 6: Confidence level vs. $\phi_2$ calculated using isospin relation between $B \to \pi \pi$ decays. This result is based on the measurements in the Belle experiment only. Solid curve shows current bound and dashed curve shows the previous result using $B^0 \to \pi^0 \pi^0$ analysis with the data sample of 275 million $B\bar{B}$. Dot-dashed and dotted lines show the confidence levels of 68% and 95%, respectively.
7. Summary

In summary, we present recent measurements of the CP violation in the decays of $B^0 \to D^* h^0$, $B^0 \to \pi^0 \pi^0 K^0_S$ and $B^0 \to \pi^0 \pi^0$. Statistical uncertainties are still dominant in most of those analysis and they are expected to be updated using the data from the Belle II [24] experiment in the future.

References

[2] Another naming convention, $\alpha(=\phi_2)$, $\beta(=\phi_1)$ and $\gamma(=\phi_3)$ are also used in the literature.