

## Charm quarks are more hydrodynamic than light quarks in $v_2$

Hanlin Li<sup>\*1</sup>, Zi-Wei Lin<sup>2,3</sup> and Fuqiang Wang<sup>4,5</sup>

<sup>1</sup>Hubei Province Key Laboratory of Systems Science in Metallurgical Process, Wuhan University of Science and Technology, Wuhan 430081, China

<sup>2</sup>Department of Physics, East Carolina University, Greenville, North Carolina 27858, USA

<sup>3</sup>Key Laboratory of Quarks and Lepton Physics (MOE) and Institute of Particle Physics, Central China Normal University, Wuhan 430079, China

<sup>4</sup>School of Science, Huzhou University, Huzhou, Zhejiang 313000, China

<sup>5</sup>Department of Physics and Astronomy, Purdue University, West Lafayette, Indiana 47907, USA

E-mail: [lihl@wust.edu.cn](mailto:lihl@wust.edu.cn), [linz@ecu.edu](mailto:linz@ecu.edu), [fqwang@purdue.edu](mailto:fqwang@purdue.edu)

Charm quark  $v_2$  is a useful tool for studying the properties of quark-gluon plasma because charm quarks experience almost the entire evolution history of relativistic heavy ion collisions. Recent studies with transport models suggest that the majority of the overall quark  $v_2$  at RHIC energies comes from the anisotropic escape of partons, not from the hydrodynamic flow. To address whether this is also true for the charm quark  $v_2$ , we trace the charm quark  $v_2$  as a function of the number of collisions the charm quark suffers with other quarks in a multi-phase transport model. We find that the common escape mechanism is at work for both the charm and light quark  $v_2$ . However, contrary to the naive expectation, the hydrodynamic collective flow contributes more to the charm  $v_2$  than the light quark  $v_2$ . Our finding thus highlights the importance of charm  $v_2$  in the study of hydrodynamic properties of the quark-gluon plasma.

*International Conference on Hard and Electromagnetic Probes of High-Energy Nuclear Collisions*  
30 September - 5 October 2018  
Aix-Les-Bains, Savoie, France

\*Speaker.

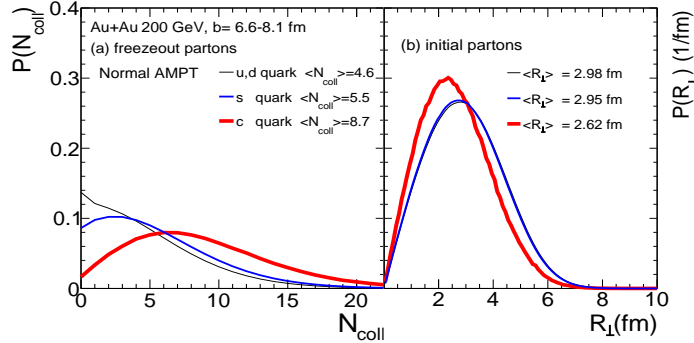
## 1. Introduction

Collective anisotropic flow is a valuable probe to study the properties of quark-gluon plasma (QGP) in the heavy ion collisions [1, 2, 3, 4]. Large elliptic flow  $v_2$  has been observed and is considered to reflect the hydrodynamic features of the QGP. In the hydrodynamics picture, the pressure gradient would generate an anisotropic expansion resulting in final-state anisotropic flows in momentum space, whose leading term is elliptical [5]. Recent studies within a multi-phase transport (AMPT) model indicate that the large parton  $v_2$  comes mainly from the escape mechanism, where the partons have a larger probability to escape along the shorter axis of the overlap volume and the hydrodynamic contribution is not a major source at RHIC energies [6, 7]. It is further shown in AMPT that the mass splitting of identified hadron elliptic anisotropies mainly comes from hadronic scatterings and thus is not a unique signature of hydrodynamics as naively perceived [8, 9].

In these proceedings, we study the whole evolution history of charm quark  $v_2$  [10, 11] and investigate the flavor dependence of the escape mechanism within the AMPT model. We consider three collision systems:  $p + Pb$  collisions at 5 TeV with impact parameter  $b=0$  fm,  $Au + Au$  collisions at 200 GeV with  $b \in (6.6, 8.1)$  fm, and  $Pb + Pb$  collisions at 2.76 TeV with  $b=8$  fm. We use the string melting version of AMPT [12] with the same parameters as in our earlier studies.

## 2. AMPT Results

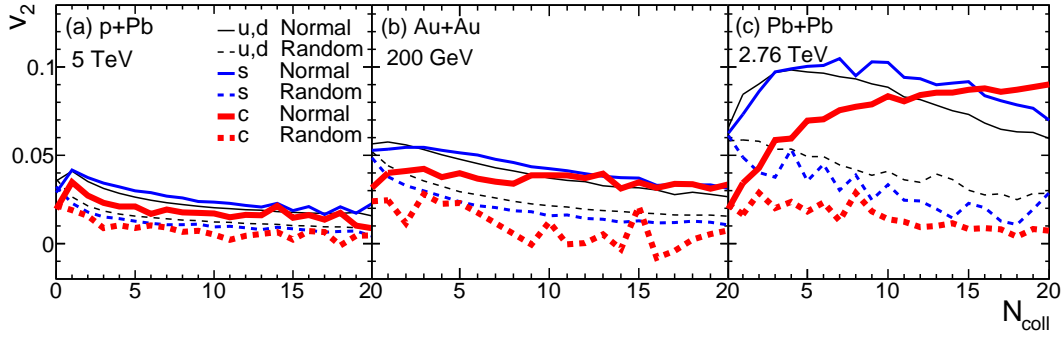
To trace the complete collision history of quarks with different flavors, we define  $N_{coll}$  as the number of collisions suffered by a parton. Fig. 1(a) shows the normalized  $N_{coll}$  distribution and the average number of collisions for each quark flavor. It indicates that charm quarks have larger  $\langle N_{coll} \rangle$



**Figure 1:** AMPT simulations of  $Au + Au$  collisions at  $\sqrt{s_{NN}} = 200$  GeV with impact parameter  $b \in 6.6$ - $8.1$  fm: (a) normalized  $N_{coll}$ -distributions of different quark flavors; (b) normalized probability distributions of the initial transverse radius  $R_{\perp}$  for different quark flavors.

than light quarks. Part of the reason is because charm quarks are produced by hard scatterings at earlier times so having longer time to interact with other partons. The other reason is because charm quarks are produced more in the inner region of the collision volume than light quarks as shown in Fig. 1(b). We find that these features are similar in all three collision systems considered in our study [10, 11].

Figure 2 shows the freezeout parton  $v_2$  of different flavors in both normal AMPT and azimuth-randomized AMPT calculations. We combine the quarks and antiquarks of the same flavor since they have almost identical  $v_2$ . In the randomized case, the parton azimuthal angles are randomized after each collision and hence their  $v_2$  comes purely from the anisotropic parton escape. The freezeout partons still have positive  $v_2$  but the values are reduced from those in the normal case due to the lack of the additional hydrodynamic contribution. Fig. 2 indicates that the escape mechanism contributes to both charm and light quarks  $v_2$ . At  $N_{coll} = 0$ , the parton  $v_2$  comes only from the escape mechanism because no collision has happened, and the charm  $v_2$  is smaller than the light quarks  $v_2$ . It implies that the charm  $v_2$  is less sensitive to the anisotropic escape than the light  $v_2$ , particularly in large collision systems.



**Figure 2:** Freezeout parton  $v_2$  within  $|\eta| < 1$  as a function of  $N_{coll}$  in (a)  $p + Pb$  collisions with  $b = 0$  fm at  $\sqrt{s_{NN}} = 5$  TeV, (b)  $Au + Au$  collisions with  $b \in 6.6-8.1$  fm at  $\sqrt{s_{NN}} = 200$  GeV, and (c)  $Pb + Pb$  collisions with  $b = 8$  fm at  $\sqrt{s_{NN}} = 2.76$  TeV in normal (solid curves) and  $\phi$ -randomized (dashed curves) AMPT.

We further calculate  $\langle N_{coll} \rangle$  and the ratios of  $v_2$  from azimuth-randomized AMPT to that from normal AMPT as shown in Table 1. The  $\langle N_{coll} \rangle$  value of freezeout partons of a given flavor increases with the collision system size and beam energy as expected. The ratio of  $v_2$  from  $\phi$ -randomized AMPT to that from normal AMPT represents the fraction of  $v_2$  that comes from the escape mechanism. It shows that the escape mechanism contribution to the light quark  $v_2$  is larger than that to charm quark  $v_2$  for the same collision system. Consequently, the hydrodynamic contribution to the light quark  $v_2$  is more important for charm quarks. This result suggests that the charm  $v_2$  better reflects the hydrodynamic properties of the quark-gluon plasma, especially for large systems at high energies. Similar conclusions have been reached by other authors [13, 14].

Quark flavor	pPb ( $b = 0$ fm)			AuAu ( $b \in 6.6-8.1$ fm)			PbPb ( $b = 8$ fm)		
	u,d	s	c	u,d	s	c	u,d	s	c
$\langle N_{coll} \rangle$	2.0	2.5	4.2	4.6	5.5	8.7	9.8	11.	15.
$v_{2,Random} / v_{2,Normal}$	73%	59%	57%	66%	47%	22%	43%	27%	8.5%

**Table 1:**  $\langle N_{coll} \rangle$  and the ratio of  $v_2$  from  $\phi$ -randomized AMPT to that from normal AMPT for freezeout partons of different flavors within  $|\eta| < 1$  in three collision systems.

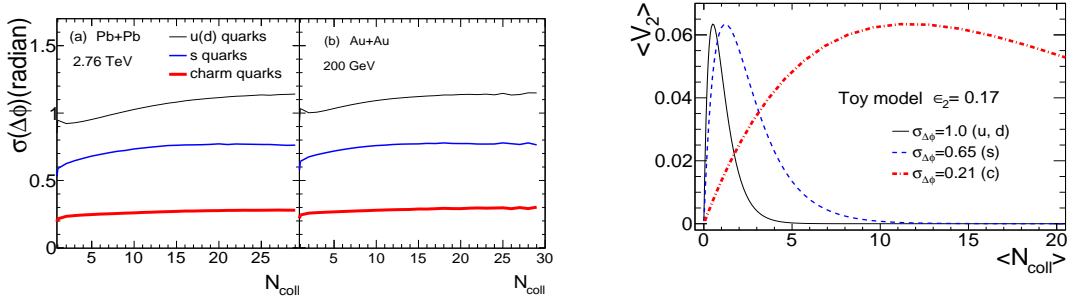
### 3. Toy model study

To further understand the hydrodynamic contribution to charm  $v_2$  and light quark  $v_2$  in the large systems, we evaluate the root-mean-square (rms) change of the azimuth angle ( $\sigma_{\Delta\phi}$ ) as a function of  $N_{\text{coll}}$  for different quark flavors in  $Au + Au$  and  $Pb + Pb$  collisions as shown in Fig. 3(left panel). The rms change is approximately  $\sigma_{\Delta\phi}=1.0, 0.65, 0.25$  for light, strange, and charm quarks, respectively; it is significantly smaller for heavier quarks [15]. To gain insights, we construct a toy model where partons start from the center  $(x, y) = (0, 0)$  and propagate out to the boundary of an ellipse that has an eccentricity  $\varepsilon_2 = 0.17$  (corresponding to semi-central  $Au + Au$  collisions). The number of collisions a parton suffers, assuming a straightline propagation (i.e. assuming a small total deflection angle), can be written as

$$N_{\text{coll}}(\phi_i) = \langle N_{\text{coll}} \rangle (1 - 2\varepsilon_2 \cos 2\phi_i),$$

where  $\phi_i$  is the initial azimuthal angle of the parton. Note that  $\langle N_{\text{coll}} \rangle$  reflects the size of system. Assuming that the deflection angle from each scattering follows a Gaussian distribution, the cumulative deflection in the azimuth angle after the parton leaves the elliptical area is then Gaussian-distributed with the width of  $\sigma_{\Delta\phi} \sqrt{N_{\text{coll}}(\phi_i)}$ . The parton average elliptic flow  $\langle v_2 \rangle$  can be calculated as

$$\langle v_2 \rangle = \frac{1}{(2\pi)^{3/2} \sigma_{\Delta\phi} \sqrt{\langle N_{\text{coll}} \rangle}} \int \frac{\cos 2(\phi_i + \delta\phi)}{\sqrt{1 - 2\varepsilon_2 \cos 2\phi_i}} \exp\left(-\frac{\delta\phi^2}{2\sigma_{\Delta\phi}^2 \langle N_{\text{coll}} \rangle (1 - 2\varepsilon_2 \cos 2\phi_i)}\right) d\phi_i d\delta\phi.$$



**Figure 3:** (left panel) The rms change of azimuth due to the  $N_{\text{coll}} - th$  collision for different quark flavors in normal AMPT calculations of (a)  $Pb + Pb$  and (b)  $Au + Au$  collisions. (right panel) The freezeout partons  $\langle v_2 \rangle$  as a function of  $\langle N_{\text{coll}} \rangle$  for quarks with different flavors from a toy model calculation for a transverse geometry at a given  $\varepsilon_2$ .

The  $\langle v_2 \rangle$  of light quarks is larger than that of charm quarks at small  $\langle N_{\text{coll}} \rangle$  but becomes smaller at large  $\langle N_{\text{coll}} \rangle$  as shown in Fig. 3 (right panel). Partons along the longer y-axis suffer more collisions than those along the x-axis, and each collision deflects the parton from its original direction to a range of directions. As a result, more y-going partons will be deflected towards an isotropic distribution. Since  $\sigma_{\Delta\phi}$  is large for light quarks, a small number of collisions is already strong enough to reshuffle the  $\phi$  directions to produce a large  $v_2$ . However, also because  $\sigma_{\Delta\phi}$  is large, light quarks easily forget their original direction, so the light quark  $v_2$  quickly drops to zero at modest  $\langle N_{\text{coll}} \rangle$  in this toy model calculation. For charm quarks, on the other hand, it takes many collisions

to build up a sizable  $v_2$  because each collision can hardly deflect the charm quark direction. Moreover,  $\langle v_2 \rangle$  only depends on the variable  $\sigma_{\Delta\phi} \sqrt{\langle N_{\text{coll}} \rangle}$ , therefore the average elliptic flow  $\langle v_2 \rangle$  has the same peak value for all flavors while the peak occurs at a larger  $\langle N_{\text{coll}} \rangle$  value for heavier quarks. Note that the  $v_2$  from the toy model basically represents the  $v_2$  generated by the escape mechanism, and after a large number of collisions partons of all flavors will be randomized and reach zero  $\langle v_2 \rangle$ . Our toy model calculation helps to illustrate the importance of the average scattering deflection angle, thus also the importance of quark mass, for the generation of  $v_2$  by parton scatterings.

#### 4. Summary

We have followed the entire parton collision history in the AMPT model to study the flavor dependence of parton  $v_2$  in small and large collision systems from RHIC to LHC energies. We find that the escape mechanism contributes to both charm and light quark  $v_2$ . However, our results indicate that the charm  $v_2$  mainly comes from the hydrodynamic collective flow for large systems. We further find that the fraction of the hydrodynamic contribution to the final partons  $v_2$  is closely related to the parton average deflection angle from each collision. Our results suggest that the charm  $v_2$  contains more information about the hydrodynamic properties of the QGP.

This work is supported in part by Hubei Province Key Laboratory of Systems Science in Metallurgical Process (Wuhan University of Science and Technology) No. Y201710, the National Natural Science Foundation of China under Grants Nos. 11628508, 11647306, and 11747312, and US Department of Energy Grant No. DE-SC0012910. ZWL thanks the Institute for Nuclear Theory at the University of Washington for its kind hospitality and stimulating discussions about part of this work. HL also acknowledges financial support from the China Scholarship Council.

#### References

- [1] I. Arsene et al. BRAHMS Collaboration, Nucl. Phys. A **757**, 1 (2005).
- [2] B. Back et al. PHOBOS Collaboration, Nucl. Phys. A **757**, 28 (2005).
- [3] J. Adams et al. STAR Collaboration Nucl. Phys. A **757**, 102 (2005).
- [4] K. Adcox et al. PHENIX Collaboration, Nucl. Phys. A **757**, 184 (2005).
- [5] J.-Y. Ollitrault, Phys.Rev. D **46**, 229 (1992).
- [6] L. He, T. Edmonds, Z.-W. Lin, F. Liu, D. Molnar, and F. Wang, Phys. Lett. B **735**, 506 (2016).
- [7] Z. -W. Lin, L. He, T. Edmonds, F. Liu, D. Molnar, and F. Wang, Nucl. Phys. A **956**, 316 (2016).
- [8] H. Li, L. He, Z. W. Lin, D. Molnar, F. Wang and W. Xie, Phys.Rev. C **93**, 051901(R) (2016).
- [9] H. Li, L. He, Z. W. Lin, D. Molnar, F. Wang and W. Xie, Phys.Rev. C **96**, 014901 (2017).
- [10] Z.-W. Lin, H. Li, and F. Wang, EPJ Web of Conferences, **171** 19005 (2018).
- [11] H. Li, Z. W. Lin and F. Wang, arXiv:1804.02681 (2018).
- [12] Z.-W. Lin, C. M. Ko, B.-A. Li, B. Zhang and S. Pal, Phys.Rev. C **72**, 064901 (2005).
- [13] R.Esha, M. Nasim, and H. Z. Huang, J. Phys. G **44**, 045109 (2017).
- [14] V. Greco, Nucl. Phys. A **967**, 200 (2017).
- [15] B. Svetitsky, Phys. Rev. D **37**, 2484 (1988).