

Single-spin asymmetry $A_{UUT}^{\sin \phi_{S_h}}$ of proton and Λ production in SIDIS at subleading twist

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We investigate the single-spin asymmetry with a sin ϕ_{S_h} modulation for the transversely polarized proton and Λ production in semi-inclusive inelastic scattering process, where ϕ_{S_h} is the azimuthal angle of the transverse spin of the final hadron. Theoretically, the spin asymmetry can be interpreted by the convolution of the twist-3 transverse momentum dependent distributions and twist-2 fragmentation functions. In this work, three different origins in terms of the hH_1 term, the $f^{\perp}D_{1T}^{\perp}$ term and the $g^{\perp}G_{1T}$ term are taken into account simultaneously for this asymmetry. We calculate the twist-3 quark transverse momentum dependent distributions h, f^{\perp} and g^{\perp} by using the quark spectator diquark model, and we investigate the role of the fragmentation functions H_1 , D_{1T}^{\perp} and G_{1T} in the sin ϕ_{S_h} asymmetry as well. We also predict the numerical results of the asymmetries for the proton and the Λ production at JLab with a 12 GeV beam and at COMPASS with a 160 GeV beam, separately. From the comparison of the different sources for the asymmetry, we find that, the distribution h and the fragmentation function H_1 give the dominant contribution to the sin ϕ_{S_h} asymmetry for proton production, while the distribution f^{\perp} might be probed by the convolution with D_{1T}^{\perp} in the Λ production at JLab 12 GeV.

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1. Introduction

In this work, we extend the phenomenological study of the polarized hadron production in SIDIS at the twist-3 level within the transverse momentum dependent (TMD) framework. We focus on the single spin asymmetry (SSA) with a $\sin \phi_{S_h}$ modulation in the transversely polarized hadron production in SIDIS off an unpolarized nucleon: $\ell + N \longrightarrow \ell' + h^{\uparrow} + X$, where ϕ_{S_h} is the azimuthal angle of the transverse spin S_{hT} with respect to the lepton plane. Following Ref. [1, 2], there are several contributions to this asymmetry from the convolutions of the twist-2 TMD fragmentation functions with twist-3 TMD distribution functions. We calculate the involved distributions and the fragmentation functions in a spectator diquark model [3, 4]. Using the model results, we investigate the roles of the hH_1 , $g^{\perp}G_{1T}$ and $f^{\perp}D_{1T}^{\perp}$ couplings in the SSA $A_{UUT}^{\sin\phi_{S_h}}$ for the transversely polarized proton and the Λ hyperon production in SIDIS at the JLab 12 GeV and at COMPASS.

2. Twist-3 TMD distribution functions in a spectator model

The three involved twist-3 TMD distributions in this work are the T-odd distribution g^{\perp} , the T-even distribution f^{\perp} and the T-odd distribution h, respectively. We have presented the calculation on the T-odd distribution g^{\perp} in a spectator model with both the scalar and the axial-vector diquark in Ref. [5, 6]. Therefore, following the same method, we can calculate the other two twist-3 TMD distribution functions h and f^{\perp} from the quark-quark correlator $\Phi(x, p_T; S)$ via the traces

$$\frac{1}{4}\operatorname{Tr}[(\Phi(x, \boldsymbol{p}_T; S) + \Phi(x, \boldsymbol{p}_T; -S))i\sigma^{\alpha\beta}\gamma_5] = -\frac{M}{P^+}\varepsilon_T^{\alpha\beta}h, \qquad (2.1)$$

$$\frac{1}{4}\operatorname{Tr}[(\Phi(x, \boldsymbol{p}_T; S) + \Phi(x, \boldsymbol{p}_T; -S))\gamma^{\alpha}] = \frac{p_T^{\alpha}}{P^+}f^{\perp}.$$
(2.2)

The corresponding expressions of *h* and f^{\perp} from the scalar component are

$$h(x, \mathbf{p}_T^2)_s = -\frac{N_s^2 (1-x)^3}{16\pi^3 M} \frac{e_s e_q}{4\pi} \frac{(m+xM)(L_s^2 - \mathbf{p}_T^2)}{L_s^2 (\mathbf{p}_T^2 + L_s^2)^3},$$
(2.3)

$$f^{\perp}(x, \boldsymbol{p}_T^2)_s = -\frac{N_s^2(1-x)^2}{16\pi^3} \frac{(\boldsymbol{p}_T^2 - 2mM(1-x) - (1-x^2)M^2 + m_s^2)}{(\boldsymbol{p}_T^2 + L_s^2)^4}, \qquad (2.4)$$

and the ones that from the axial-vector diquark component are

$$h(x, \mathbf{p}_T^2)_a = 0,$$
 (2.5)

$$f^{\perp}(x, \boldsymbol{p}_T^2)_a = \frac{N_a^2(1-x)}{16\pi^3} \frac{(x\boldsymbol{p}_T^2 + 2mM(1-x)^2 + (x-1)m^2 + (x^3 - 2x^2 + 1)M^2 - m_a^2)}{L_a^2(\boldsymbol{p}_T^2 + L_a^2)^3}.$$
 (2.6)

The detailed calculation of the distributions h and f^{\perp} has been performed in Ref. [7]. To construct the distributions for the u and d quarks, we adopt the following relation between the flavors and isospins of the diquark $f^u = c_s^2 f^s + c_a^2 f^a$, $f^d = c_{a'}^2 f^{a'}$ [3]. c_s , c_a and $c_{a'}$ are the free parameters of the model, a and a' denote the isoscalar and isovector states of the axial-diquark, respectively.

In Fig. 1, we show the dependence of the distributions f^{\perp} and h on the flavors, Bjorken x and the active quark transverse momentum $p_T = 0.3$ GeV. As we can see, the distributions $f^{\perp u}$ and $f^{\perp d}$ are in similar sizes in the specified kinematic region (x = 0.3 or $p_T = 0.25$ GeV). While



Figure 1: Model results for $xf^{\perp u}(x, p_T^2)$, $xh^u(x, p_T^2)$ (solid line) and $xf^{\perp d}(x, p_T^2)$, $xh^d(x, p_T^2)$ (dashed line).

for the T-odd distribution h, its size is smaller compared to those of the T-even distributions f^{\perp} . Particularly, we can verify that h^{u} vanishes when one integrates out the transverse momentum $\int d^2 p_T h^{u}(x, \mathbf{p}_T^2) = 0$, which is an expected result from the time-reversal invariance.

3. Twist-2 TMD fragmentation functions in spectator model

In this section, we will perform the model calculation on the relevant twist-2 TMD polarized fragmentation functions H_1 , G_{1T} and D_{1T}^{\perp} . Since D_{1T}^{\perp} has been calculated for the Λ hyperon by the same spectator diquark model in Ref. [8], we will focus on the proton fragmentation function $D_1^{p/q}$. The calculation on the left two TMD fragmentation functions H_1 and G_{1T} can be performed from the fragmentation correlation function $\Delta(z, \boldsymbol{k}_T; \boldsymbol{S}_{hT})$ by the traces

$$S_T^{\alpha} H_1(z, \boldsymbol{k}_T^2) = \frac{1}{4} \operatorname{Tr}[(\Delta(z, \boldsymbol{k}_T; \boldsymbol{S}_{hT}) - \Delta(z, \boldsymbol{k}_T; -\boldsymbol{S}_{hT}))i\sigma^{\alpha} \gamma_5], \quad (3.1)$$

$$S_{hL}G_{1L}(z,\boldsymbol{k}_T^2) + \frac{\boldsymbol{k}_T \cdot \boldsymbol{S}_{hT}}{M_h} G_{1T}(z,\boldsymbol{k}_T^2) = \frac{1}{4} \operatorname{Tr}[(\Delta(z,\boldsymbol{k}_T;\boldsymbol{S}_{hT}) - \Delta(z,\boldsymbol{k}_T;-\boldsymbol{S}_{hT}))\gamma^{-}\gamma_5].$$
(3.2)

The spin vector of the outgoing hadron S_h has the form $S_h^{\mu} = S_{hL} \frac{(P_h \cdot n_+)n_-^{\mu} - (P_h \cdot n_-)n_+^{\mu}}{M_h} + S_{hT}^{\mu}$. Assuming the SU(6) spin-flavor symmetry for the final state hadron [9, 10], the relations be-

Assuming the SU(6) spin-flavor symmetry for the final state hadron [9, 10], the relations between quark flavors and diquark types for the proton and the Λ hyperon can be established as

$$D^{u \to p} = \frac{3}{2}D^{(s)} + \frac{1}{2}D^{(v)}, \quad D^{d \to p} = D^{(v)}, \quad D^{s \to p} = 0$$
(3.3)

$$D^{u \to \Lambda} = D^{d \to \Lambda} = \frac{1}{4} D^{(s)} + \frac{3}{4} D^{(v)}, \ D^{s \to \Lambda} = D^{(s)}.$$
(3.4)

Following the method and settings in Ref. [11], the modeling expression of the twist-2 TMD unpolarized fragmentation function D_1 can be obtained as

$$D_1^{(s)}(z, \boldsymbol{k}_T^2) = D_1^{\nu}(z, \boldsymbol{k}_T^2) = \frac{g_D^2}{2(2\pi)^3} \frac{1}{z^2} e^{\frac{-2k^2}{\Lambda^2}} \frac{(1-z)[z^2k_T^2 + (M+zm)^2]}{z^4(k_T^2 + L^2)^2},$$
(3.5)

which has already been calculated in Ref. [8]. According to Eq. (3.3) and Eq. (3.5), the unpolarized fragmentation function D_1 for proton satisfies the relation $D_1^{u \to p} = 2D_1^{d \to p}$, which is consistent with the HKNS parametrization of D_1^p presented in Ref. [12].

Similarly, we can get the model results of the TMD fragmentation functions H_1 and G_{1T} [7]

$$H_1^R(z, \boldsymbol{k}_T^2) = a_R \frac{g_D^2}{2(2\pi)^3} \frac{1}{z^2} e^{\frac{-2k^2}{\Lambda^2}} \frac{(1-z)[(zm+M_h)^2]}{z^4 (\boldsymbol{k}_T^2 + L_f^2)^2}, \qquad (3.6)$$

$$G_{1T}^{R}(z, \boldsymbol{k}_{T}^{2}) = a_{R} \frac{g_{D}^{2}}{(2\pi)^{3}} \frac{1}{z^{2}} e^{\frac{-2k^{2}}{\Lambda^{2}}} \frac{M_{h}(zm + M_{h})(1 - z)}{z^{3}(\boldsymbol{k}_{T}^{2} + L_{f}^{2})^{2}}, \qquad (3.7)$$



Figure 2: Model results of zH_1^u and zH_1^d (solid line), zG_{1T}^u (dotted line) and zG_{1T}^d , $zD_{1T}^{\perp u}$ and $zD_{1T}^{\perp d}$ (dashed line) for the proton.

with $L_f^2 = \frac{1-z}{z^2} M_h^2 + m^2 + \frac{m_D^2 - m^2}{z}$. From Eqs. (3.3), (3.4) and (3.6), (3.7), one can find that for the fragmentation functions H_1 and G_{1T} , both the *u* and *d* quark fragmenting to the Λ hyperon will vanish in our model, while the *u* and *d* quark fragmenting to the proton will be nonzero. That is, for the Λ production, we only need to consider the contribution from D_{1T}^{\perp} .

In Fig. 2, we present our model results of the twist-2 TMD fragmentation functions H_1 , G_{1T} and D_{1T}^{\perp} for the *u* and *d* quark fragmenting to the proton. As one can see, H_1 and G_{1T} decrease but D_{1T}^{\perp} increases with increasing *z*; the magnitude of H_1 is lager than that of G_{1T} , while D_{1T}^{\perp} is nonzero only in the large *z* region. From the view of the flavors, H_1^u and G_{1T}^u are positive in the model, while H_1^d and G_{1T}^d are negative. As for D_{1T}^{\perp} , only $D_{1T}^{\perp d}$ becomes sizable at large *z*.

4. Prediction on the SSA of transversely polarized proton and Λ hyperon in SIDIS

The differential cross section of the process for the transverse polarized hadron in SIDIS off the unpolarized proton is generally expressed as [13]

$$\frac{d\sigma}{dxdydzd\phi d\psi dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} (1+\frac{\gamma^2}{2x}) \bigg\{ F_{UUU} + |S_{hT}| \sin\phi_{S_h} \sqrt{2\varepsilon(1+\varepsilon)} F_{UUT}^{\sin\phi_{S_h}} + \cdots \bigg\}.$$
(4.1)

Here F_{UUU} and $F_{UUT}^{\sin \phi_{S_h}}$ are structure functions that contributes to the $\sin \phi_{S_h}$ azimuthal asymmetry, which $P_{h\perp}$ -dependent expression can be defined as

$$A_{UUT}^{\sin\phi_{S_h}}(P_{h\perp}) = \frac{\int dx \int dy \int dz \frac{1}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \sqrt{2\varepsilon(1+\varepsilon)} F_{UUT}^{\sin\phi_{S_h}}}{\int dx \int dy \int dz \frac{1}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) F_{UUU}}$$
(4.2)

The *x*-dependent and the *z*-dependent asymmetries can be given in a similar way.

To perform the estimate, we adopt a more phenomenological approach by using the factorization at the tree-level [14] to give the expression for the structure function $F_{UUT}^{\sin\phi_{S_h}}$:

$$F_{UUT}^{\sin\phi_{S_h}} \approx \frac{2M}{Q} \mathscr{I}[-xhH_1 + \frac{\mathbf{k_T} \cdot \mathbf{p_T}}{2MM_h}(-xf^{\perp}D_{1T}^{\perp} - xg^{\perp}G_{1T})].$$
(4.3)

where we introduce the convolution integral

$$\mathscr{I}[\boldsymbol{\omega}fD] = x\sum_{q} e_{q}^{2} \int d^{2}\boldsymbol{p}_{T} \int d^{2}\boldsymbol{k}_{T} \delta^{2}(\boldsymbol{p}_{T} - \frac{\boldsymbol{P}_{h\perp}}{z} - \boldsymbol{k}_{T})w(\boldsymbol{p}_{T}, \boldsymbol{k}_{T})f^{q}(x, \boldsymbol{p}_{T}^{2})D^{q}(z, \boldsymbol{k}_{T}^{2}), \quad (4.4)$$



Figure 3: Predictions on the asymmetry $A_{UUT}^{\sin\phi_{S_h}}$ for proton and Λ in SIDIS at JLab 12 GeV.

and the Wandzur-Wilczek approximation [15] to ignore the contribution from the twist-3 TMD fragmentation functions \tilde{D}_T , \tilde{H}_T^{\perp} and \tilde{H}_T to $F_{UUT}^{\sin\phi_{S_h}}$.

Considering the following constraints on the transverse momenta of the initial quarks [16]

$$\begin{cases} \boldsymbol{p}_T^2 \le (2-x)(1-x)Q^2, & \text{for } 0 < x < 1; \\ \boldsymbol{p}_T^2 \le \frac{x(1-x)}{(1-2x)^2}Q^2, & \text{for } x < 0.5; \end{cases}$$
(4.5)

and the kinematical cuts adopted at JLab 12 GeV

$$0.1 < x < 0.6, \ 0.3 < z < 0.7, \ Q^2 > 1 \text{GeV}^2, \ W^2 > 4 \text{GeV}^2, P_{h\perp} > 0.05 \text{GeV},$$
 (4.6)

we estimate the SSA $A_{UUT}^{\sin\phi_{S_h}}$ of proton and Λ hyperon production in SIDIS. The numerical results are shown in Fig. 3. For proton production, the magnitude of the asymmetry $A_{UUT}^{\sin\phi_{S_h}}$ is sizable and negative, and the size is around 4% at the kinematics of JLab. While for the Λ hyperon production, the size is smaller than 1%, since it gets contribution only from the $f^{\perp}D_{1T}^{\perp}$ term in our model.

We also estimate this same asymmetry for proton and Λ at COMPASS with the kinematics [17]

$$0.004 < x < 0.7, \ 0.1 < y < 0.9, \ z > 0.2, \ Q^2 > 1 \,\text{GeV}^2,$$

$$P_{h\perp} > 0.1 \,\text{GeV}, \ W > 5 \,\text{GeV}, \ E_h > 1.5 \,\text{GeV}.$$
(4.7)

The responding asymmetries $A_{UUT}^{\sin \phi_{S_h}}$ for proton and Λ hyperon are shown in Fig. 4. Interestingly, the size of the *hH*₁ contribution at COMPASS is clearly smaller than that of JLab. This is because the twist-3 effect is suppressed by a factor of 1/Q, while *Q* at COMPASS is larger than that at JLab.

5. conclusion

In this work, we predicted the contributions from three twist-3 terms to the SSA $A_{UUT}^{\sin\phi_{S_h}}$ in the transversely polarized proton as well as Λ production in SIDIS at the kinematics of JLab 12





Figure 4: Predictions on the asymmetry $A_{UUT}^{\sin\phi_{S_h}}$ for proton and Λ in SIDIS at COMPASS.

GeV and COMPASS. The estimated contributions to the asymmetry for the proton is sizable and negative. Specifically, the magnitude is around 4% at JLab 12 GeV, but about 1% at COMPASS. The sin ϕ_{S_h} asymmetry from the $f^{\perp}D_{1T}^{\perp}$ term for the Λ hyperon production is much smaller.

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