

# 1 Systematic studies of di-jet imbalance 2 measurements at STAR

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STAR has previously reported significant transverse momentum imbalance of a specific set of di-jets selected with “hard cores”, i.e. with a constituent cut of 2 GeV/ $c$ . After reclustering these same di-jets with a lower constituent cut of 200 MeV/ $c$ , the di-jet balance is restored to the level of  $pp$  collisions within the original cone size of  $R = 0.4$ .

The interpretation of these observations as resulting from tangential bias with restricted in-medium path lengths promised *Jet Geometry Engineering* of jet production vertices through systematic variations of parameters such as centrality, the constituent  $p_T$  cutoff, and the initial imbalance between the hard cores. We examine the sensitivity of the di-jet imbalance observable to variations in the di-jet definition, and explore the possibility of using Jet Geometry Engineering to study the path length dependence of jet energy loss in the QGP.

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### 3 1. Introduction

4 The properties of the quark-gluon plasma (QGP) formed in heavy-ion collisions can be studied  
 5 via highly energetic partons produced in high- $Q^2$  scatterings early on in the collision evolution.  
 6 These high-energy partons lose energy as they propagate through the medium, before fragmenting  
 7 and hadronizing into collimated sprays of energetic particles called jets. Measurements of partonic  
 8 energy loss (also known as jet quenching) via interactions with the medium can be used to infer  
 9 properties of both the medium and the jet itself. The effects of jet quenching can be extracted  
 10 from jet measurements by comparing heavy-ion (A+A) collisions to similar measurements made in  
 11 proton-proton ( $pp$ ) collisions, which are expected to exhibit minimal medium formation, and are  
 12 well described by perturbative QCD (pQCD) [1].

13 Gold nuclei are collided at  $\sqrt{s_{\text{NN}}} = 200$  GeV/ $c$  at the Relativistic Heavy-Ion Collider (RHIC)  
 14 at Brookhaven National Laboratory (BNL). At this center-of-mass energy, certain jet quenching  
 15 models predict a significant in-medium path length bias for the initiating parton of a jet when  
 16 requiring a trigger during jet-finding, such as a high transverse momentum ( $p_T$ ) leading hadron, or  
 17 a minimum jet  $p_T$  [2]. This is in contrast to the much larger  $\sqrt{s_{\text{NN}}}$  at the Large Hadron Collider  
 18 (LHC), where no such bias is observed in the same models.

19 If the magnitude of such a bias can be systematically controlled via trigger selections, the path  
 20 length dependence of partonic energy loss can be studied differentially. In these proceedings we  
 21 present the first systematic attempt at this procedure - which we call *jet geometry engineering* - by  
 22 differentially varying the jet definition in Au+Au and  $pp$  collisions, and comparing the difference  
 23 between systems using the di-jet imbalance ( $A_J$ ).

### 24 2. Di-jet imbalance measurements at STAR

25 STAR has previously measured the di-jet imbalance [3], defined as

$$A_J = \frac{p_T^{\text{lead}} - p_T^{\text{sublead}}}{p_T^{\text{lead}} + p_T^{\text{sublead}}}, \quad (2.1)$$

26 where “lead” and “sublead” signify the jets with the highest and second-highest, respectively, trans-  
 27 verse momenta in the event, in central (0-20%) Au+Au and  $pp$  collisions. Event selection is per-  
 28 formed using a “hard-core” (HC) jet definition, by clustering only the hard constituents in the event;  
 29 in this case, selecting all constituents with  $p_T > 2.0$  GeV/ $c$ , and requiring back-to-back leading  
 30 and subleading jets with  $p_T^{\text{lead}} > 20$  GeV/ $c$  and  $p_T^{\text{sublead}} > 10$  GeV/ $c$ , respectively, while requiring  
 31 at least one calorimeter hit in the event with  $E_T > 5.4$  GeV. Charged tracks and calorimeter hits  
 32 are clustered with the anti- $k_t$  algorithm [4] with a resolution parameter ( $R$ ) of 0.4 using the FastJet  
 33 package [5]. This hard-core selection eliminates the need for background subtraction and reduces  
 34 the background jet rate to approximately zero. If a suitable hard-core di-jet pair is found, all tracks  
 35 and calorimeter hits with  $p_T > 0.2$  GeV/ $c$  in the event are then clustered and the resulting jets are  
 36 radially matched to the hard-core leading and subleading jets such that  $\Delta R = \sqrt{\Delta\phi^2 + \Delta\eta^2} < R$ ,  
 37 where  $\Delta\phi = \phi^{\text{HC}} - \phi^{\text{match}}$  and  $\Delta\eta = \eta^{\text{HC}} - \eta^{\text{match}}$ . Both the hard-core and matched  $A_J$  are then  
 38 measured, and the resulting distributions are compared to a  $pp$  reference. The original measure-  
 39 ment from STAR found that the hard-core di-jets were significantly imbalanced compared to the  $pp$

40 hard-core reference, implying significant jet quenching. However, the matched di-jet  $A_J$  was bal-  
 41 anced to the level of the  $pp$  reference, suggesting that any quenched energy was recovered within  
 42 the relatively narrow jet radius. The measurement was repeated for  $R = 0.2$ , but the matched di-jets  
 43 showed significant imbalance with respect to the  $pp$ , suggesting some intra-jet broadening between  
 44  $R = 0.2$  and  $0.4$ .

45 In these proceedings, we show an extension of the earlier measurement, by varying the param-  
 46 eters of the jet-finding algorithm. We hold  $p_T^{\text{lead}}$  and  $p_T^{\text{sublead}}$  constant, and systematically vary the  
 47 jet resolution parameter for both hard-core and matched di-jets from 0.2 to 0.4 in five steps of 0.05,  
 48 as well as the hard-core constituent  $p_T$  cut ( $p_T^{\text{const}}$ ) from 1.0 to 3.0 GeV/c in five steps of 0.5 GeV/c.  
 49 The di-jet imbalance is calculated for the resulting 25 unique di-jet definitions for both hard-core  
 50 and matched di-jets and compared to a  $pp$  reference.

### 51 3. Analysis details

52 The 200 GeV/c Au+Au and  $pp$  data shown were collected in 2007 and 2006, respectively,  
 53 by the STAR detector at the RHIC accelerator complex at BNL. STAR is a large general-purpose  
 54 detector [6] built around a solenoidal magnet with detectors for triggering, tracking, particle iden-  
 55 tification and calorimetry.

56 Charged tracks are measured in the STAR Time Projection Chamber (TPC) [7]. Tracks se-  
 57 lected for analysis are required to have a minimum of 20 fit points (out of 46 maximum), and a  
 58 minimum fraction of fit points over the maximum possible fit points (determined by detector and  
 59 track geometry) of 0.52. Tracks are required to have a maximum distance of closest approach  
 60 (DCA) to the primary vertex of 1 cm, and a maximum pseudorapidity  $|\eta|$  of 1.0. Neutral energy is  
 61 recorded in the STAR Barrel Electromagnetic Calorimeter (BEMC) [8].

62 Events are selected by an online BEMC trigger calibrated to require a single calorimeter tower  
 63 hit of  $E_T$  larger than approximately 5.4 GeV/c. The primary vertex of the event is reconstructed  
 64 from global tracks in the TPC, and this vertex is required to be within 30 cm of the nominal  
 65 center of the detector along the beam line. Only the most central 20% of Au+Au collisions are  
 66 considered, where centrality is determined by the raw track multiplicity of the collision within the  
 67 pseudorapidity range  $|\eta| < 0.5$ .

68 Jet-finding is done similarly to the original STAR  $A_J$  measurement, using the FastJet imple-  
 69 mentation of the anti- $k_t$  algorithm [4, 5] with a resolution parameter varied from 0.2 to 0.4. Charged  
 70 tracks and neutral energy depositions are initially clustered into hard-core jets using a  $p_T^{\text{const}}$  varied  
 71 from 1.0 to 3.0 GeV/c. If a hard-core di-jet pair is identified with  $p_T^{\text{lead}} > 16$  GeV/c and  $p_T^{\text{sublead}} > 8$   
 72 GeV/c and  $|\Delta\phi| > \pi - 0.4$ , then the tracks and calorimeter hits are reclustered with all constituents  
 73 such that  $p_T^{\text{const}} > 0.2$  GeV/c - STAR's nominal acceptance - and geometrically matched to the  
 74 hard-core jets as described above. Due to  $p_T^{\text{const}}$  being varied down to 1 GeV/c there can still be  
 75 significant background energy density. Therefore, all jets (both hard-core and matched) are back-  
 76 ground subtracted using the FastJet area-based subtraction method [9], as described in the original  
 77 STAR  $A_J$  measurement [3], giving a corrected  $p_T^{\text{jet}} = p_T^{\text{measured}} - \rho^{\text{event}} A^{\text{jet}}$ , where  $\rho^{\text{event}}$  is the me-  
 78 dian transverse energy density of the event, and  $A^{\text{jet}}$  is the jet area. The absolute di-jet imbalance  
 79  $|A_J|$  is calculated for both the hard-core and matched di-jets.

		jet-finder R							jet-finder R				
		0.2	0.25	0.3	0.35	0.4			0.2	0.25	0.3	0.35	0.4
$p_T^{\text{const}}$ [GeV/c]	3.0	$10^{-13}$	$10^{-15}$	$10^{-15}$	$10^{-17}$	$10^{-13}$	$p_T^{\text{const}}$ [GeV/c]	3.0	$10^{-14}$	$10^{-11}$	$10^{-9}$	$10^{-9}$	$10^{-9}$
	2.5	$10^{-13}$	$10^{-13}$	$10^{-19}$	$10^{-20}$	$10^{-17}$		2.5	$10^{-17}$	$10^{-14}$	$10^{-13}$	$10^{-10}$	$10^{-12}$
	2.0	$10^{-8}$	$10^{-9}$	$10^{-13}$	$10^{-14}$	$10^{-11}$		2.0	$10^{-22}$	$10^{-18}$	$10^{-21}$	$10^{-18}$	$10^{-18}$
	1.5	$10^{-8}$	$10^{-7}$	$10^{-9}$	$10^{-12}$	0.00015		1.5	$10^{-19}$	$10^{-22}$	$10^{-24}$	$10^{-28}$	$10^{-30}$
	1.0	0.00079	$10^{-6}$	$10^{-8}$	$10^{-8}$	$10^{-10}$		1.0	$10^{-23}$	$10^{-27}$	$10^{-34}$	$\approx 0$	$\approx 0$

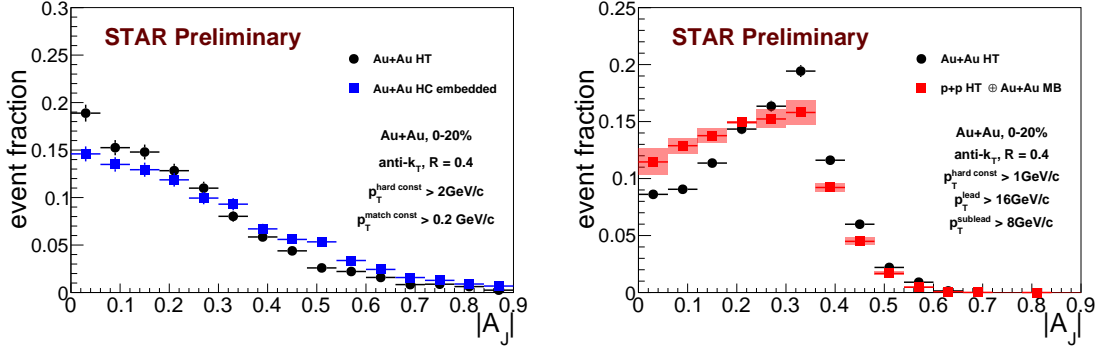
**Table 1:** Left: Kolmogorov-Smirnov test values for matched di-jet  $|A_J|$  comparison between Au+Au and embedded Au+Au (RC). Right: Kolmogorov-Smirnov test values for hard-core Au+Au and embedded  $pp$  di-jets. See text for details.

80 To make a meaningful comparison between Au+Au and  $pp$ , the large background fluctuations  
81 in Au+Au and relative detector performance must be taken into account. To model the effect of  
82 the underlying Au+Au event on the measurement, we embed the  $pp$  reference into minimum-bias  
83 (MB) Au+Au data in the same centrality (0-20%) as our triggered data. The performance of TPC  
84 track reconstruction degrades as the number of tracks increases. To account for this, the relative  
85 tracking efficiency ( $90\% \pm 7\%$  at  $p_T > 1.0$  GeV/c) and relative tower energy scale ( $100\% \pm 2\%$ )  
86 are applied to the  $pp$  during embedding. Systematic uncertainty on the relative tracking efficiency  
87 and tower energy scale is estimated by varying these values in the embedded  $pp$ .

88 The Au+Au and  $pp$  distributions are compared quantitatively using the binned Kolmogorov-  
89 Smirnov (KS) two-sample test of similarity [10], where  $N_{\text{bins}} \gg N_{\text{di-jets}}$ , to minimize over-estimation  
90 due to binning effects. For two datasets sampled from the same PDF, the KS test returns a number  
91 uniformly distributed between 0 and 1, and for two datasets sampled from differing distributions,  
92 the test returns a value  $\ll 1$ . In the tables summarizing the test results, we use colors to aid in  
93 visualizing the patterns: green when the test score is greater than 0.05, yellow for results between  
94  $10^{-4}$  and 0.05, and red for anything below  $10^{-4}$ .

#### 95 4. Quantifying sensitivity to jet-like correlations

96 The background energy density and the corresponding region-to-region energy density fluc-  
97 tuations increase when reducing the constituent  $p_T$  cut from  $p_T^{\text{const}}$  to 0.2 GeV/c for the matched  
98 jets. In the limit of  $\sigma A^{\text{jet}} \gg p_T^{\text{jet}}$ , where  $\sigma$  is an estimation of the intra-event transverse energy  
99 density fluctuations, the  $A_J$  distribution could be insensitive to physical balancing due to correlated  
100 jet yield, and instead be dominated by background fluctuations. To estimate the effect of these fluc-  
101 tuations on the  $|A_J|$  distribution, Au+Au hard-core di-jets are embedded into uncorrelated Au+Au  
102 minimum-bias events of the same centrality. The hard-core and matching procedure is repeated  
103 for these random cone (RC) events for the reported di-jet definitions, and compared to the Au+Au  
104 matched di-jets. An example is shown on the left side of Fig. 1. The KS test results are shown  
105 on the left side of Table 1, and their resultant values are much less than 1 for all di-jet definitions.  
106 From this we conclude that our measurement of  $|A_J|$  is sensitive to the soft constituent correlated  
107 jet yield measured in the matched di-jets.



**Figure 1:** Left:  $|A_J|$  distributions for Au+Au and embedded Au+Au hard-core di-jets, with  $p_T^{\text{const}} > 2.0$  GeV/c and  $R = 0.4$ . Right:  $|A_J|$  distributions for Au+Au and embedded  $pp$  hard-core jets, with  $p_T^{\text{const}} > 1.0$  GeV/c and  $R = 0.4$ . See text for details.

		jet-finder R				
		0.2	0.25	0.3	0.35	0.4
$p_T^{\text{const}}$ [GeV/c]	3.0	$10^{-8}$	$10^{-7}$	0.0035	0.51	0.61
	2.5	$10^{-9}$	$10^{-7}$	0.031	0.99	0.47
	2.0	$10^{-13}$	$10^{-8}$	0.0023	0.066	0.17
	1.5	$10^{-12}$	$10^{-12}$	$10^{-7}$	0.035	0.00059
	1.0	$10^{-18}$	$10^{-16}$	$10^{-12}$	$10^{-13}$	$10^{-16}$

**Table 2:** Kolmogorov-Smirnov test values for matched di-jet  $|A_J|$  comparison between Au+Au and embedded  $pp$ . See text for details.

## 108 5. Results

109 We calculate  $|A_J|$  for hard-core jets in Au+Au and embedded  $pp$  while varying both the hard-  
 110 core  $p_T^{\text{const}}$  and jet resolution parameter ( $R$ ), as described above; example shown in the right panel  
 111 of Fig. 1. For each of the 25 di-jet definitions, the KS test is performed, and the results are shown  
 112 on the right side in Table 1. For all di-jet definitions, the KS test value is much less than 1, showing  
 113 significant differences between the two data sets. This shows that there is significant modification of  
 114 the hard-core di-jets in Au+Au for all di-jet definitions examined in the kinematic range explored in  
 115 this analysis. We then calculate the  $|A_J|$  for all matched di-jets ( $p_T^{\text{const}} > 0.2$  GeV/c) for the same di-  
 116 jet definitions. Such distributions for both Au+Au and  $pp$  are in Fig. 2. There is a relatively smooth  
 117 transition from statistically different distributions at small  $p_T^{\text{const}}$  and small jet radius to statistically  
 118 similar distributions at large  $p_T^{\text{const}}$  and large jet radius, as shown in Table 2. This evolution of the  
 119 KS value indirectly shows the radial distribution of “lost” energy, and the evolution of the energy  
 120 loss as a function of the hard-core  $p_T$  cut.

## 121 6. Summary

122 We have demonstrated the ability to choose more or less modified di-jet pairs in Au+Au colli-  
 123 sions compared to  $pp$  collisions by varying the parameters of the di-jet definition. This systematic

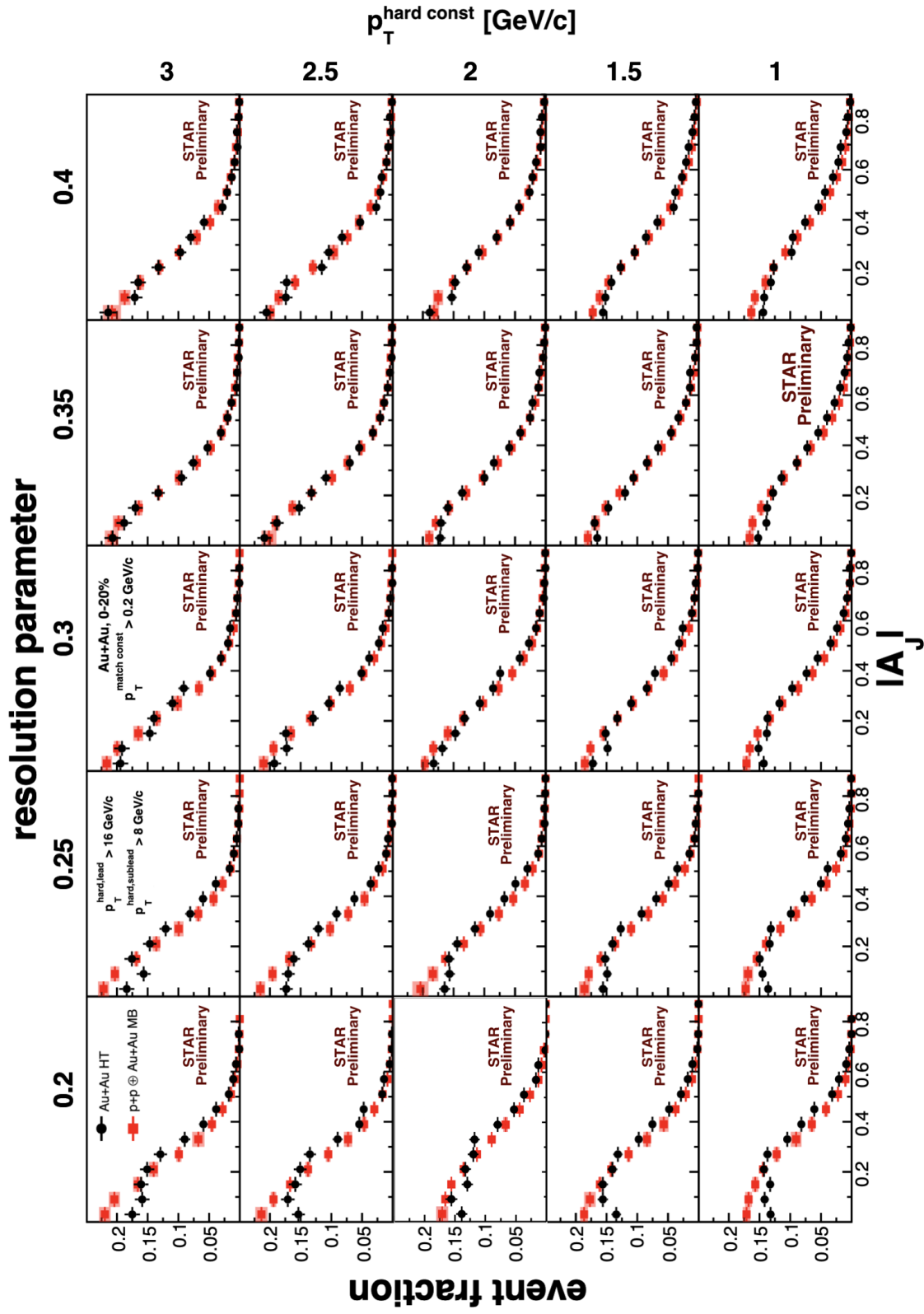


Figure 2:  $|A_J|$  distributions for Au+Au and embedded  $pp$  matched di-jets for all di-jet definitions. See text for details.

124 control of the energy loss opens up the possibility of jet geometry engineering, and may help to  
125 constrain the path length dependence of partonic energy loss in the QGP at RHIC energies. Further  
126 analysis with increased statistics to increase kinematic reach in jet  $p_T$ , as well as expanding the  
127 centrality selections is planned, along with comparison to jet quenching models, to examine the  
128 model predictions for path-length dependence bias due to tuning of the di-jet definition.

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