

New Venues in Formation and Detection of Primordial Black Holes

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Primordial black holes (PBHs) are not as exotic as once thought and constitute a compelling non-particle dark matter (DM) candidate. We present a novel general PBH formation mechanism from scalar field fragmentation, which does not suffer from the inflaton potential fine-tuning that plagues many of the standard PBH formation models. We discuss how interactions of compact stars with very small PBHs, which reside in the open window of parameter space where PBHs can constitute all of DM, allow for a slew of new astrophysical signatures that could shed light on PBH DM and are particularly interesting in the era of multi-messenger astronomy.

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1. Introduction

Standard astrophysical black holes arise at the end of stellar evolution as a result of star collapse, occurring at relatively late cosmological times after the star formation epoch. In contrast, black holes could also appear in the early Universe [1, 2, 3]. These “primordial” black holes (PBHs) can constitute part or all of the dark matter (DM) (see Ref. [4, 5, 6] for review). Such non-particle DM candidates are particularly intriguing in light of lack of any convincing signals from particle DM searches, despite extensive experimental efforts [7]. Further, PBHs have been associated with the recently observed (e.g. [8, 9, 10]) gravitational waves (e.g. [11, 12, 13, 14]) and can assist with resolution of major puzzles in astronomy, such as formation of supermassive black holes (e.g. [15]).

Primordial black holes are more generic than once thought and can form in a large variety of scenarios associated with physics beyond the Standard Model (BSM), including different models of inflation, axion-curvaton models, baryogenesis, phase transitions as well as collapse of cosmic string loops, among others (see Ref. [4, 5, 6] for an overview). In a typical setup, BHs form in the early Universe when an $\delta \sim \mathcal{O}(1)$ overdensity perturbation enters the horizon after the end of inflation and subsequently collapses. This allows to simply estimate the size of the resulting BHs to be $M_{\text{PBH}} \sim M_{\text{H}} \sim 10^{15}(t/10^{-23} \text{ s}) \text{ g}$, where M_{H} is the horizon mass at the formation time t . Interestingly, PBHs can already occur within “standard cosmology”, albeit with an extremely suppressed probability. The usual perturbations arising from inflation are nearly scale-invariant and must agree with measurements from Cosmic Microwave Background (CMB) observations [16] on large scales. Hence, a significant degree of inflaton potential fine-tuning is expected within typical models of PBH formation [17]. Formation associated with metastability of the Standard Model Higgs has been also suggested [18], however, a full model becomes more complicated.

We present a novel general mechanism of PBH formation based on scalar field fragmentation [19, 20, 21]. Aside from the recently observed Higgs, scalar fields are generic in BSM constructions. In particular, presence of moduli and axion fields are a defining feature of models based on extra dimensions and string theories [22]. Analogously, phenomenological models based on supersymmetry (SUSY) are accompanied by a slew of complex scalar fields with nearly vanishing potentials, “flat directions” [23]. In the early Universe and in the presence of self-interactions, such scalar fields can often undergo fragmentation into solitonic lumps, Q-balls [24] or oscillons (e.g. [25]). Since the process is stochastic, some of the resulting sub-horizon overdensities arising from collection of field lumps are expected to collapse and form BHs. As the relevant perturbations are not related to inflation, this mechanism does not suffer from the usual fine-tuning of the inflaton potential associated with many standard PBH-formation scenarios. Further, within this general setup, PBH formation can occur either before or after reheating and originate from inflaton or some other, unrelated, spectator field.

Formed primordial black holes can contribute to DM if their size is $M_{\text{PBH}} \gtrsim 10^{15} \text{ g}$, sufficient to survive Hawking evaporation until present day. While it is difficult to realize all of DM to reside in PBHs over most of the PBH parameter space, there remains an unconstrained open window in the $\sim 10^{17} - 10^{22} \text{ g}$ sub-lunar PBH mass range. Such very small PBHs can be efficiently captured by compact stars (neutron stars and white dwarfs) in DM-rich environments [26]. As captured PBHs evolve consuming the host star, they will eventually destroy it. We discuss [27, 28, 29] how these PBH-star systems can result in a variety of novel astrophysical signatures, including

solar-mass black holes as well as “orphaned” kilonovae or gamma-ray bursts without associated merger gravity waves. This allows for potential novel insights into the open PBH parameter space window that is difficult to probe otherwise. Further, PBH-star systems can help with resolving long-standing astronomical puzzles, such as the origin of r -process nucleosynthesis [27].

2. Primordial black holes from scalar field lumps

2.1 Scalar field evolution and fragmentation in the early Universe

Consider a light complex scalar field ϕ in a potential $V(\phi)$, charged under some global U(1) symmetry, which does not dominate the energy-density in the early Universe. This setup is typical of flat directions appearing within supersymmetric models, many of which are charged under U(1) baryon or lepton number [23]. Analogously to the Standard Model Higgs, such spectator field will experience random quantum jumps during the inflation (de Sitter) phase [30]. The field, off-set from its minimum of $\phi = 0$ to ϕ_0 , can hence develop a large vacuum expectation value (VEV) as determined by $V(\phi_0) \sim H_I^4$. Here, H_I is the Hubble parameter value associated with the scale of inflation Λ_I via $H_I = \sqrt{8\pi/3}(\Lambda_I^2/M_{\text{pl}})$, where $M_{\text{pl}} \simeq 2.45 \times 10^{18}$ GeV is the reduced Planck mass.

After inflation, the scalar field will roll back down relaxing to the potential minimum and coherently oscillate. In the presence of self-interactions, growing instabilities can develop in the field’s oscillation modes. Parametrizing the complex field as a real field with a rotating phase $\phi = R(x, t)e^{i\Omega(x, t)}$, it can be shown through dispersion relations that unstable growing oscillation modes appear under simple and very general condition [31]

$$V''(R) - \dot{\Omega} < 0. \quad (2.1)$$

For the special case of $\dot{\Omega} = 0$, the above reduces to the popular “tachyonic resonance”. Growing instability modes will eventually result in scalar condensate fragmenting into solitonic lumps, Q-balls [24]. The evolution of instabilities associated with the scalar field self-interactions are analogous to gravitational Jeans instability of self-gravitating gas, often appearing in astrophysics and cosmology. The attractive self-interactions of gravity make homogeneous distribution of particles unstable with respect to formation of dense matter clumps, leading to collapse of gas clouds and subsequent star formation. Another way to see that in the presence of self-interactions lump formation will be generally expected is by looking at the pressure(p)-density(ρ) relations. In particular, for field potential effectively rising slower than quadratic, i.e. $V(\phi) \sim |\phi|^n$ with $n < 2$, the pressure of a system $p \propto (-\rho)$ is negative and hence leads to condensate collapse [32].

Field perturbations $\delta\phi$ associated with the instability and growing faster than the expansion rate of the Universe will eventually enter the non-linear regime (i.e. $\delta\phi \gtrsim \bar{\phi}$, where $\bar{\phi}$ is the average background field value) and can subsequently fragment. Existence of spherical solitonic Q-ball configurations in the spectrum of a theory with self-interacting scalar fields charged under U(1) can be rigorously proven from energetics [24]. Long-term stability of Q-balls is ensured by charge conservation. The size of the resulting Q-ball lumps can be determined by analyzing growing oscillation modes that become non-linear the earliest, denoted k_{nl} . From numerical simulations [31, 33, 34] the size of a typical field fragment R_Q constitutes a few percent of the horizon size at fragmentation

$$R_Q \sim k_{\text{nl}}^{-1} \sim f_Q H^{-1}, \quad (2.2)$$

where $f_Q \sim 10^{-1} - 10^{-2}$. The resulting number density of solitons is then approximately $\bar{n} \sim (k_{\text{nl}}/2\pi)^3 \sim 10 - 10^6$. Generally, the Q-ball mass and radius are given by

$$M_Q = \Lambda Q^\alpha \quad , \quad R_Q = \frac{Q^\beta}{\Lambda} \quad (2.3)$$

where Λ is a scale associated with scalar field potential, with $0 < \alpha$ and $\beta < 1$ being model-dependent parameters. For gauge-mediated SUSY, $\Lambda = M_{\text{SUSY}}$ parametrizes the SUSY breaking scale and $\alpha = 3/4$, $\beta = 1/4$ [31]. While Q-balls are stable with respect to decays into ϕ -quanta, they could decay e.g. due to higher-dimensional operators that break the U(1) symmetry. These effects can be phenomenologically parametrized by the Q-ball lifetime $\tau_Q = 1/\Gamma_Q$, with Γ_Q being the total decay width.

The discussion above can be readily extended to the case of real scalar field fragmenting into pseudo-solitonic lumps, oscillons (e.g. [25]). While the stability of oscillons is not guaranteed by a U(1) symmetry, they could be long lived due to an approximate adiabatic invariant that can be related to particle number [25]. In fact, oscillons can be identified with the real projection of the Q-ball solution in non-relativistic field theory limit [35].

2.2 Primordial black hole formation

After the end of inflation, inflaton decays onset radiation-dominated era. Subsequent fragmentation of a spectator scalar field results in population of solitonic lumps of matter. Since matter redshifts as a^{-3} , compared to radiation a^{-4} , with a being the cosmological scale factor, at some later time Q-balls come to matter-dominate the energy-density of the Universe. As the fragmentation process is stochastic and the resulting lumps are sizable, some sub-horizon regions could contain sufficiently large overdensities that will subsequently collapse and form black holes.

At fragmentation time t_f , the resulting PBH-mass function can be obtained via [19, 20, 21]

$$\frac{d\langle \rho_{\text{PBH}} \rangle}{dM} \Big|_{t_f} = \int \frac{dV}{V^2} P(M|V) B(M, V) M \quad , \quad (2.4)$$

where $P(M|V)$ is the probability of finding a soliton cluster of mass M within volume V and $B(M, V)$ is the probability of cluster of mass M to collapse to a BH. Assuming the most general model-independent and uncorrelated distribution of soliton lumps, we take $P(M|V)$ to be Poisson. The BH collapse condition is approximately of the form $B(M, V) \sim K\theta[\delta_0 - \delta_c]$, with the step function θ selecting original soliton cluster overdensities δ_0 that lie above a critical threshold for collapse $\delta_c \sim \mathcal{O}(0.1)$. The phenomenological constant prefactor K parametrizes any additional complex effects that play a role in the collapsing set of solitons, including angular momentum, anisotropy, etc. (see Ref. [36, 37, 38] for related treatment of collapsing dust in matter-dominated era). Since Q-ball charge is conserved, additional corresponding condition is imposed on resulting fragments.

In order to obtain the present-day contribution, results of Eq. (2.4) must be redshifted through the initial radiation-dominated and subsequent Q-ball matter-dominated eras. The Q-ball matter-dominated era starts at t_Q and finishes at t_R , when the Q-balls that have not collapsed to BHs decay away and reheat the Universe to temperature T_R . In order not to spoil the Big Bang Nucleosynthesis, we impose $T_R \gtrsim 5$ MeV. The evolution through above cosmological phases is captured in a

multiplicative scale factor

$$a_t = \left(\frac{t_Q}{t_f}\right)^{1/2} \left(\frac{t_R}{t_Q}\right)^{2/3} \left(\frac{g_{*S}(T_R)}{g_{*S}(T_0)}\right)^{1/3} \frac{T_R}{T_0}, \quad (2.5)$$

where $T_0 = 2.7$ K is the present-day temperature and $g_{*S}(T)$ denotes the relevant number of temperature-dependent relativistic degrees of freedom.

The final resulting differential fraction of dark matter in PBHs can be obtained from

$$\frac{df_{\text{DM}}}{dM} = \frac{1}{\rho_{\text{DM}}} \frac{1}{a_t^3} \left. \frac{d\langle\rho_{\text{PBH}}\rangle}{dM} \right|_{t_f}, \quad (2.6)$$

where ρ_{DM} the observed DM abundance. The above analysis is general and readily applicable to oscillons, which could originate directly from the inflaton fragmentation [21], or to any other possible solitonic configurations with any number of conserved quantities beyond just the scalar field charge.

In Fig. 1 we illustrate the typical cosmological timelines for PBHs forming from the inflaton fragmenting into oscillons (left panel), without an intermediate radiation-dominated era (i.e. $t_f = t_Q$), and from a spectator scalar field fragmenting into Q-balls (right panel).

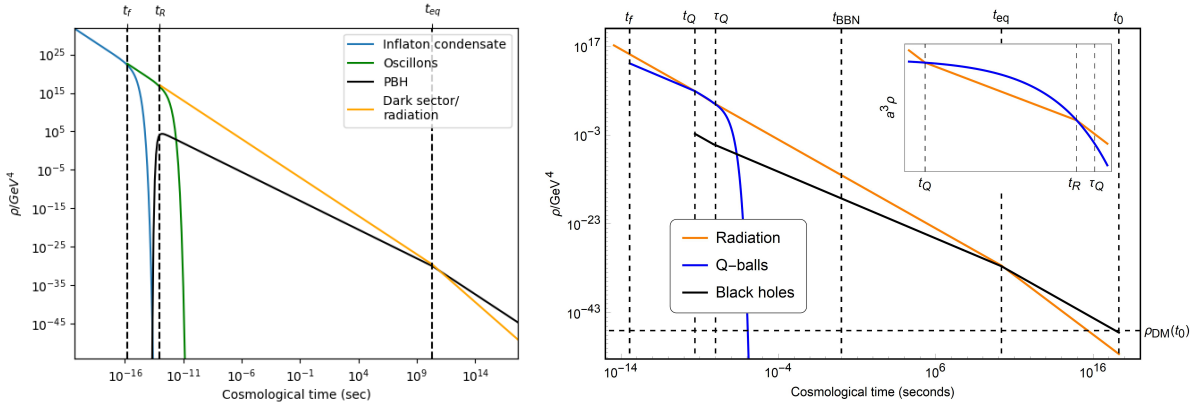


Figure 1: Two examples of a typical timeline. In the model from Ref. [21] (left panel), oscillon scalar lumps formed directly from the inflaton dominate the energy density for a limited time creating a temporary matter-dominated era, during which PBHs form. In the case of a spectator field [19, 20], it can fragment into Q-balls during the radiation-dominated era (right panel). Since the gas of Q-balls has the energy density that scales as matter, it comes to dominate at time t_Q , creating a matter dominated era that lasts until the Q-balls decay at time τ_Q . PBHs form during this matter-dominated era.

3. Compact stars as primordial black hole laboratories

PBHs whose masses lie within the open parameter space window of $\sim 10^{17} - 10^{22}$ g and that constitute a significant fraction of DM can efficiently interact with compact stars within DM rich environments, such as Galactic Center (GC) or Ultra-faint Dwarf Spheroidal (UFD) galaxies. A small PBH can become gravitationally captured by a neutron star (NS) or a white dwarf (WD) if it

loses sufficient energy through dynamical friction and accretion as it passes through the star [26]. For typical parameter values and optimistic DM density consistent with observations, the base capture rate of PBHs on NS can be estimated to be $F_0^{\text{GC}} \simeq 10^{-11}/\text{yr}$ within the GC and an order better for UFDs [27]. The full capture rate depends on the PBH fraction constituting DM as $F = (\Omega_{\text{PBH}}/\Omega_{\text{DM}})F_0$, with Ω denoting the respective abundance. The total number of captured PBHs within time t is just Ft . Due to significantly lower density, the capture rate on WDs is smaller by several orders compared to NS. After capture, PBH will settle inside the star and consume it through accretion [39]. For a typical NS, with mass of $M_{\text{NS}} \sim 1.5M_{\odot}$ and radius of $R_{\text{NS}} \sim 10$ km, the time for a captured PBH to settle within star is $t_{\text{set}}^{\text{NS}} \simeq 9.5 \times 10^3 (M_{\text{PBH}}/10^{-11}M_{\odot})^{-3/2}$ yrs. After settling, the time for BH to consume the star from the inside is $t_{\text{con}}^{\text{NS}} \simeq 5.3 \times 10^{-3} (10^{-11}M_{\odot}/M_{\text{PBH}})$ yrs. The resulting star's lifetime is determined by the combination of above time-scales.

Anticipating the role of angular momentum, it is particularly interesting to investigate interactions of PBHs with pulsars that are rotating extremely rapidly with a millisecond period [27]. It can be shown that within the age of the Galaxy of $\sim 10^{10}$ yrs, up to $\sim 10\%$ of $\sim 10^7$ millisecond pulsars (MSPs) residing within GC would have been consumed by PBHs if they constitute a significant fraction of DM. This is consistent with the ‘‘missing pulsar problem’’, denoting under-abundance of observed pulsars in the center of the Galaxy compared to predictions from population synthesis models [40]. A recently discovered very young magnetar located right near the GC is consistent with our the scenario outlined above and its unusual emission activity [41] might be a sign of a PBH destruction in progress. Assuming that angular momentum, originally associated with material in-falling into the growing by accretion central black hole within the star, is efficiently transferred to the star's outer layers, a full analytic analysis predicts that more than $\sim 0.1M_{\odot}$ of neutron-rich material can be ejected [27]. Heuristically, MSPs are already rotating near mass-shedding limit and conservation of angular momentum during contraction of the star as it is being consumed by PBH will result in spin up. With further additional angular momentum transferred from within, matter on the star's surface will start to exceed the escape velocity.

The material ejected as a result of PBH-NS destruction is neutron rich and can be an excellent source of r -process nucleosynthesis, which is a key astrophysical process for production of heavy elements such as gold and uranium [27]. Here, neutrons are rapidly captured on a seed nuclei before they can decay, allowing to build up an element with a large atomic number. While supernovae and neutron-star mergers have been historically suggested as the beacons of r -process element production (e.g. [42]), a definitive confirmation of production sites is still lacking. Around $\sim 10^4 M_{\odot}$ of r -process material is observed within Milky Way. Recently, it has been noted that 1 out of 10 UFDs shows strong r -process abundance, consistent with a singular rare historic event [43]. Heavy element production associated with PBHs destroying neutron stars can consistently explain abundance of r -process elements in Milky Way as well as UFDs simultaneously [27].

In addition to the r -process nucleosynthesis, PBHs interacting with compact stars can result in a variety of novel astrophysical signatures [27, 28, 29]. We give a brief overview of these signals, displaying some of them in Fig. 2 along with experimental constraints on PBH abundance in DM. In particular, electromagnetic afterglow originating from expanding nuclear material ejecta will result in a ‘‘kilonova’’. However, in contrast to the standard kilonova signals as expected from neutron star mergers, ‘‘orphan kilonova’’ from PBH-NS systems will be without an associated gravity wave merger signal. As neutron stars are highly magnetized, the energy associated with

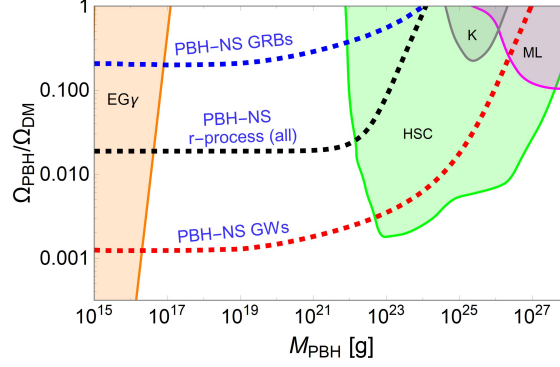


Figure 2: Signals from PBH-compact star interactions along with experimental constrains. [blue dashed] Allowed parameter space for PBH-NS gamma-ray bursts to significantly contribute to the observed positron excess at high energies [29]. [black dashed] Allowed parameter space where heavy element nucleosynthesis associated with PBH-NS systems can account for all of r -process element abundance in Milky Way as well as UFDs simultaneously [27]. [red dashed] Allowed parameter space where gravity waves from transmuted binaries from PBH-NS interactions can be within observation reach of Advanced LIGO, assuming a lower signal-to-noise threshold than design [28]. Dashed lines correspond to the maximum reach for each signal, assuming the most optimistic input parameter choice for the fits. Observational constraints from extragalactic γ -rays from BH evaporation (EG γ) [44], Kepler star milli/microlensing (K) [45], MACHO/EROS/ OGLE micro-lensing (ML) [46] as well as Subaru Hyper Suprime-Cam micro-lensing (HSC) [47] are shown.

NS magnetic fields will be released during the final stages of PBH consumption and can result in a *non-repeating fast radio burst* (FRB). A slew of FRB signals have been recently detected, with an unknown origin [48]. The ejecta is heating through nuclear interactions, and aside the kilonova, thermal positrons will be produced and leaking out. These positrons will annihilate, producing 511 keV emission. Simple estimates show that the strength of the expected associated 511 keV signal from PBH-NS systems is consistent with the observed long-standing 511 keV excess from the GC (see Ref. [49] for review). Interestingly, recent observations [50] of strong 511 keV emission signal from the same UFDs showing enhanced r -process element abundance suggests a natural link between the two, both occurring due to a singular rare event. This can be readily incorporated within the PBH-NS scenario (or a neutron star merger [51]). As captured PBH consumes the host compact star (WD or NS), most of the original star material will end up swallowed by the BH. Hence, there will remain a population of $\sim 0.5 - 1.5M_{\odot}$ solar-mass BH remnants, not expected from standard astrophysics. A binary that originally contained a compact star that was later “transmuted” into a solar-mass BH could result in associated novel signals (e.g. double kilonova signals - one from merger and one from PBH-star interaction). Such solar-mass BH can be potentially distinguishable from a NS with future observations via higher order gravity wave effects. If some of the material from PBH-NS system forms an accretion disk surrounding the resulting solar-mass BH, this will be a natural setup for an “*orphan short gamma-ray burst*”, without an accompanying merger gravity wave signal. While accreting WDs can emit jets, due to large radius of the WD they are non-relativistic, with luminosity approximately scaling as $L \sim 1/R_{\text{star}}$. A PBH captured by a WD will eventually consume it, resulting in a compact BH remnant. Due to significant decrease in radius of the accretor, the associated jet can suddenly become relativistic, resulting in

a novel *solar-mass microquasar*. Interestingly, jet emission from a local population of orphaned gamma-ray bursts and solar-mass microquasars can contribute to the positron excess observed in AMS-02 [52] as well as several other experiments.

4. Conclusions

PBHs constitute compelling non-particle DM candidates. We have presented a novel general PBH formation mechanism from scalar field fragmentation that can be implemented within a broad range of models and that avoids the issue of inflaton potential fine-tuning associated with many of the standard PBH formation scenarios. Interactions of compact stars with tiny PBHs, which reside in the open window of parameter space where PBHs can constitute all of DM, can be a rich source of novel astrophysical signals that could shed light on PBH DM.

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